



# Using machine learning to unlock Gaia's full potential to determine the dark matter halo

Bryan Ostdiek

LBL, September 26, 2018

with Timothy Cohen, Marat Freytsis, Phillip Hopkins, Mariangela Lisanti,  
Lina Necib, and Andrew Wetzel

First Gaia skymap in color [[https://www.cosmos.esa.int/web/gaia/gaiadr2\\_gaiaskyincolor](https://www.cosmos.esa.int/web/gaia/gaiadr2_gaiaskyincolor)]

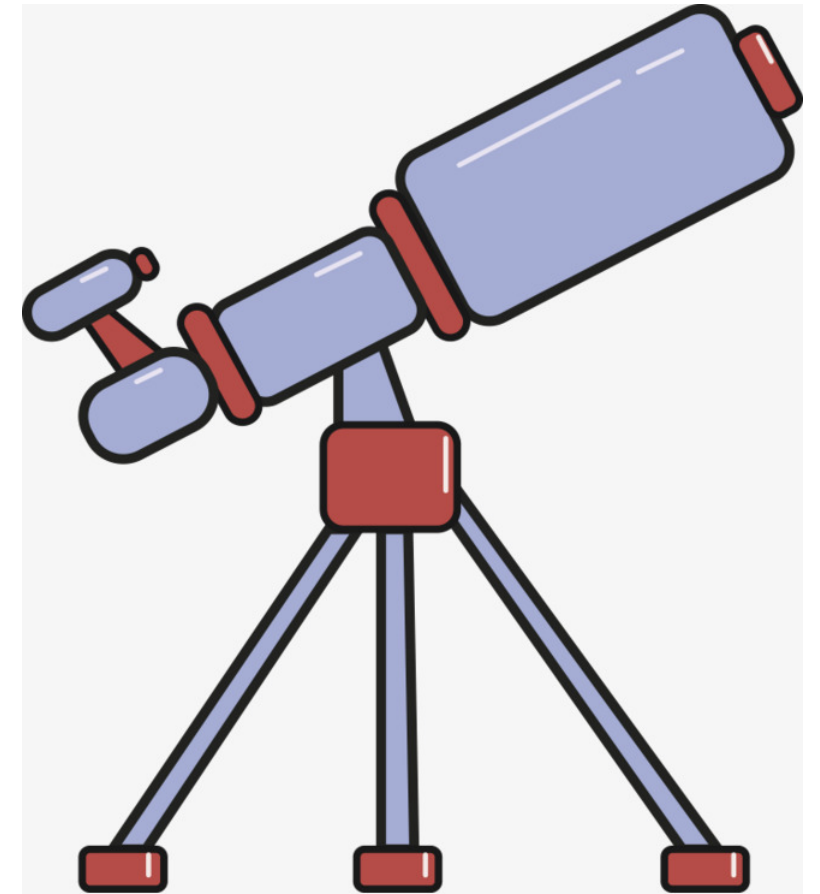


# Introduction

Goal: Use data from the Gaia satellite to make measurements about the halo of the Milky Way

Why (Astronomers): How galaxies form

Why (Particle physicists): Dark matter makes up the halo

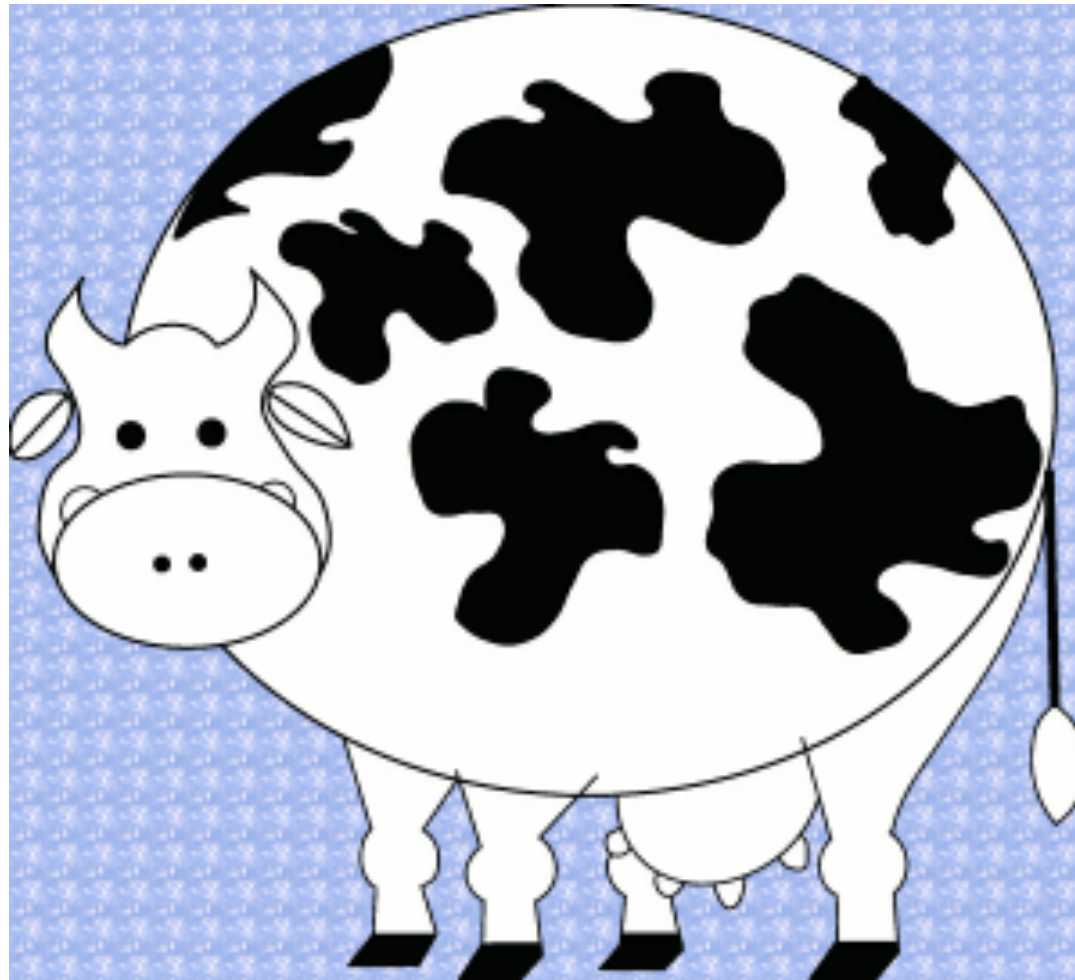


How: Old stars act as tracers for dark matter

Challenges: Identifying old stars with limited information



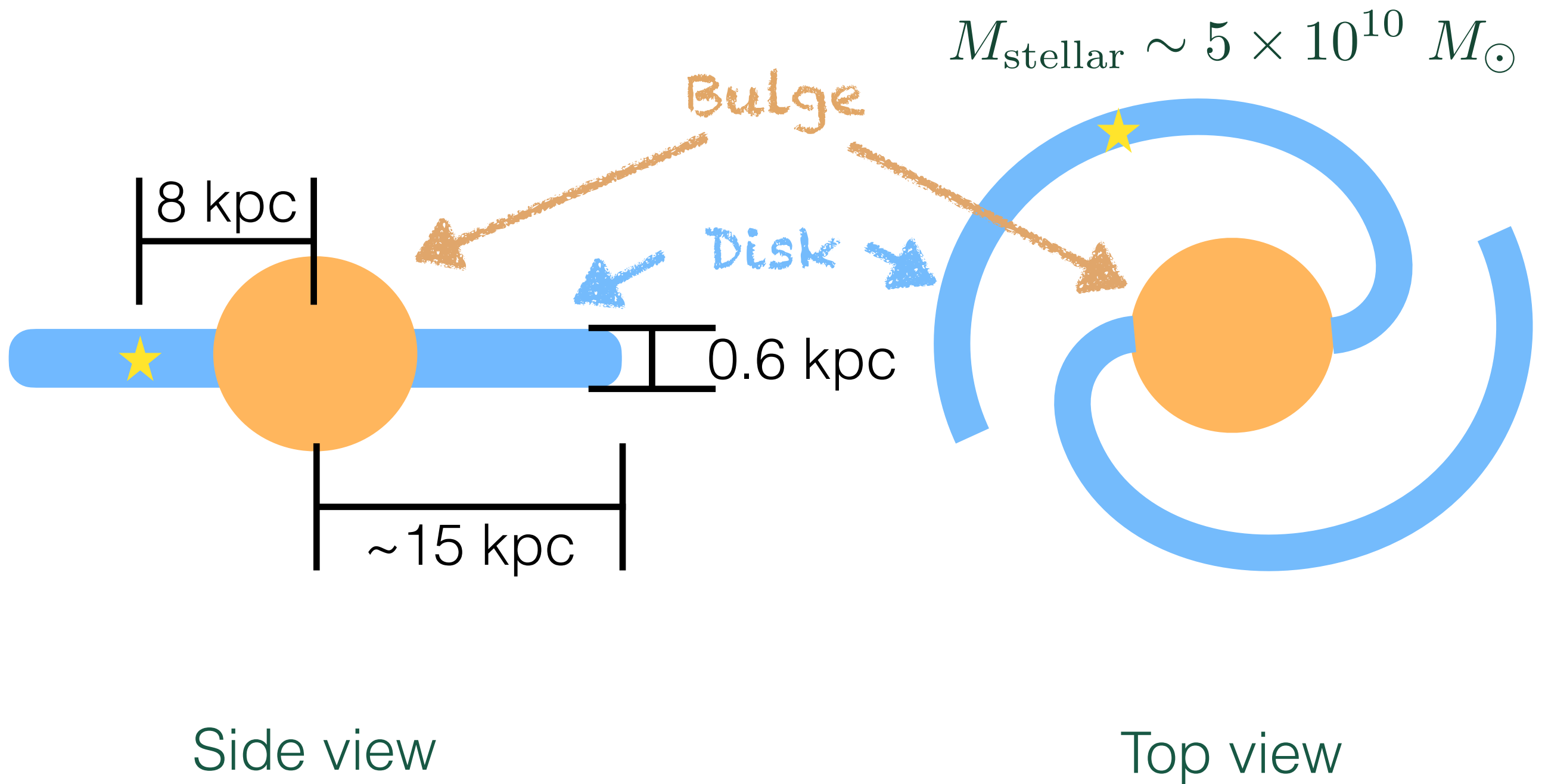
# Spherical cow model of a galaxy



[http://www.physics.csbsju.edu/stats/WAPP2\\_cow.html](http://www.physics.csbsju.edu/stats/WAPP2_cow.html)

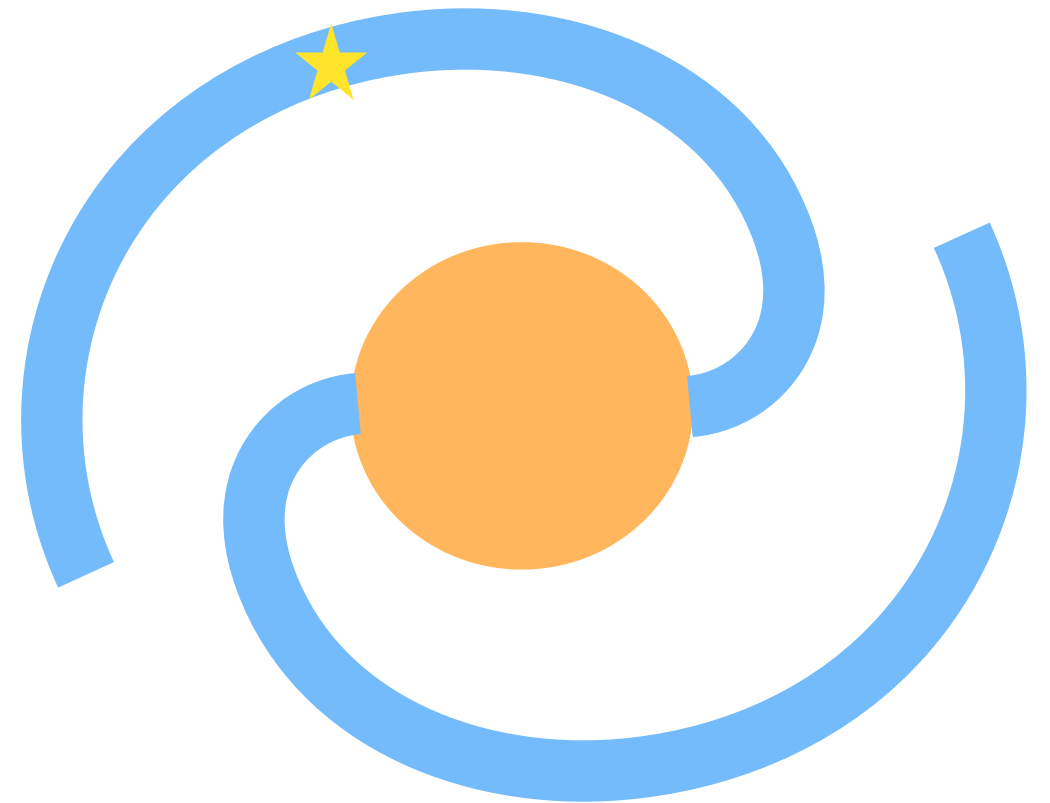
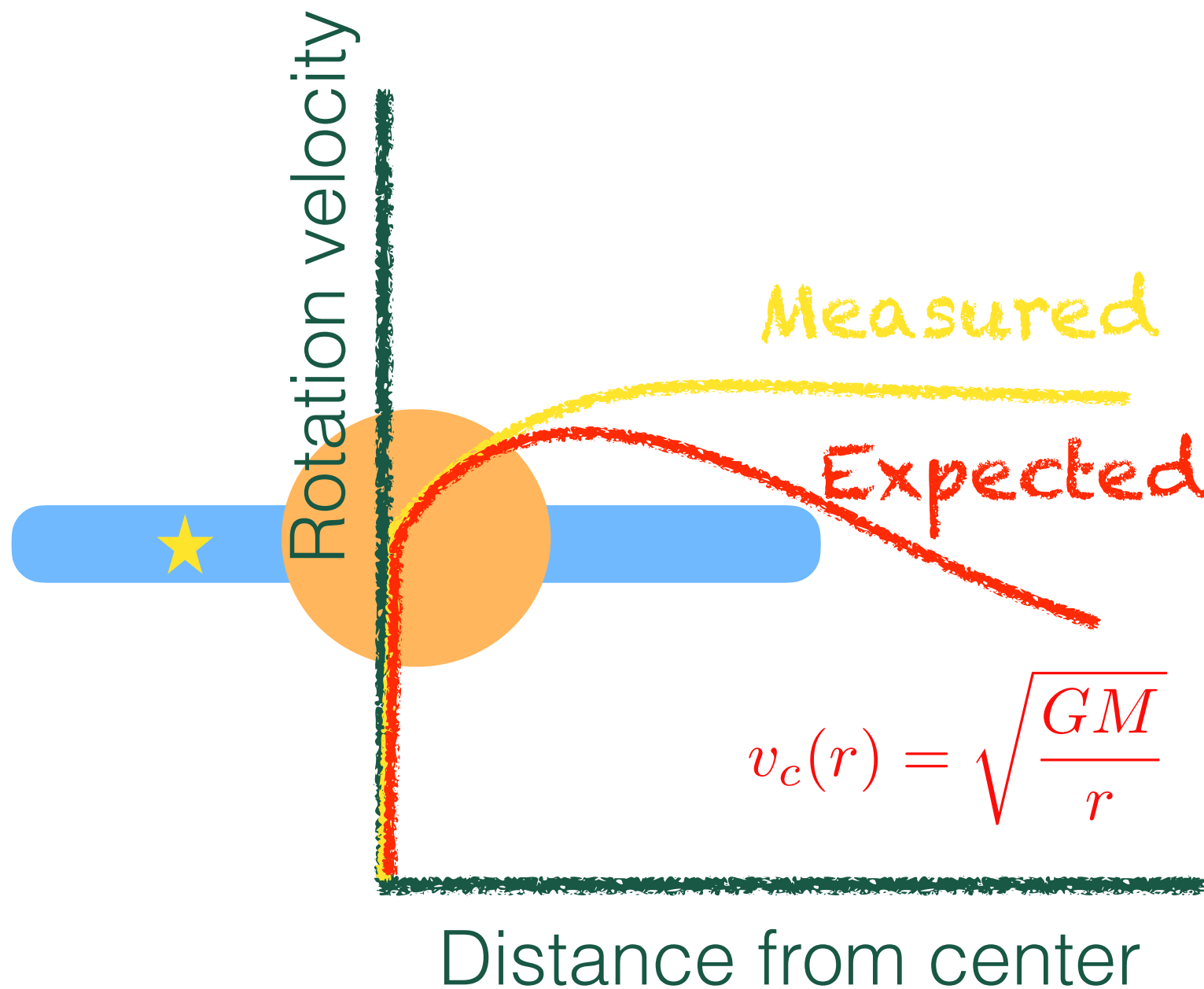


# Toy model of spiral galaxy



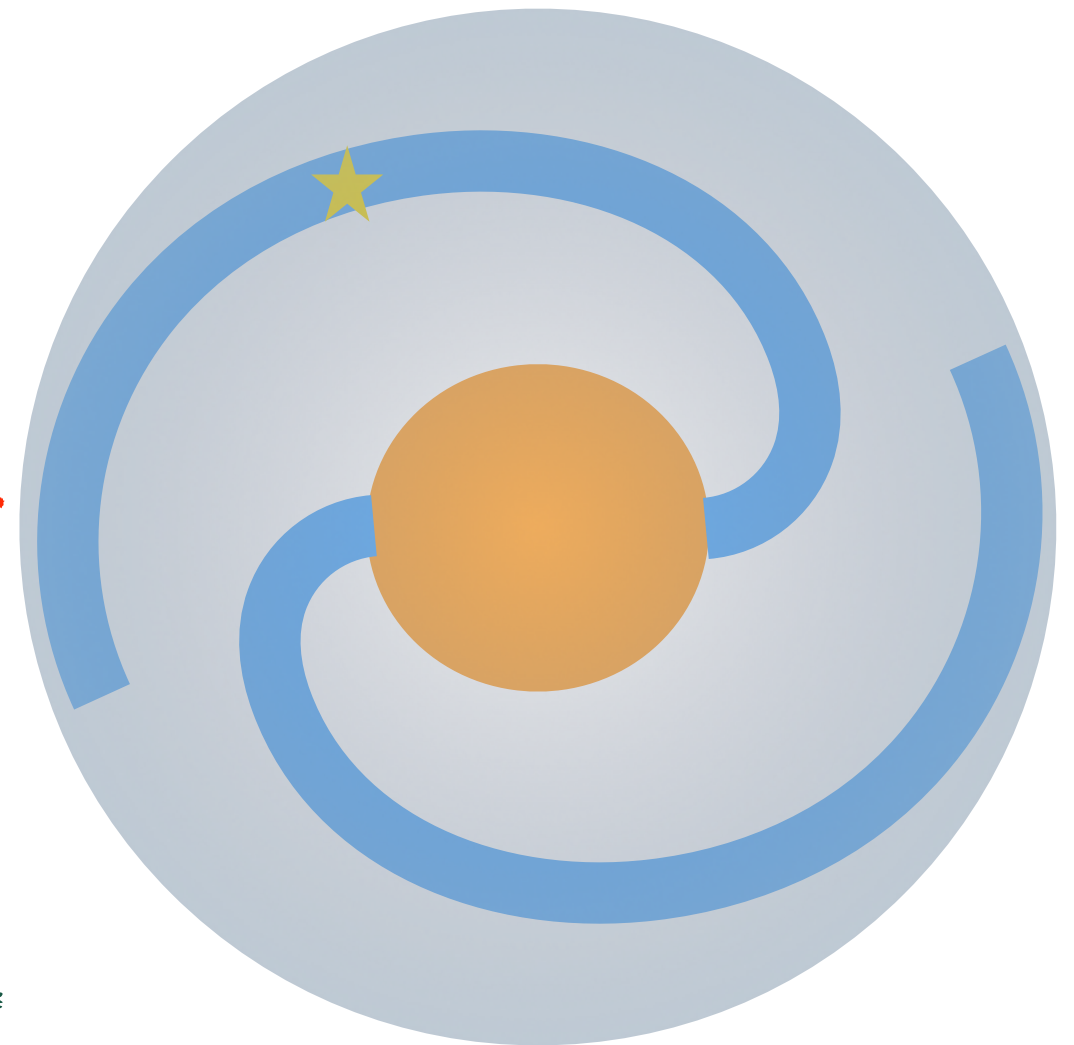
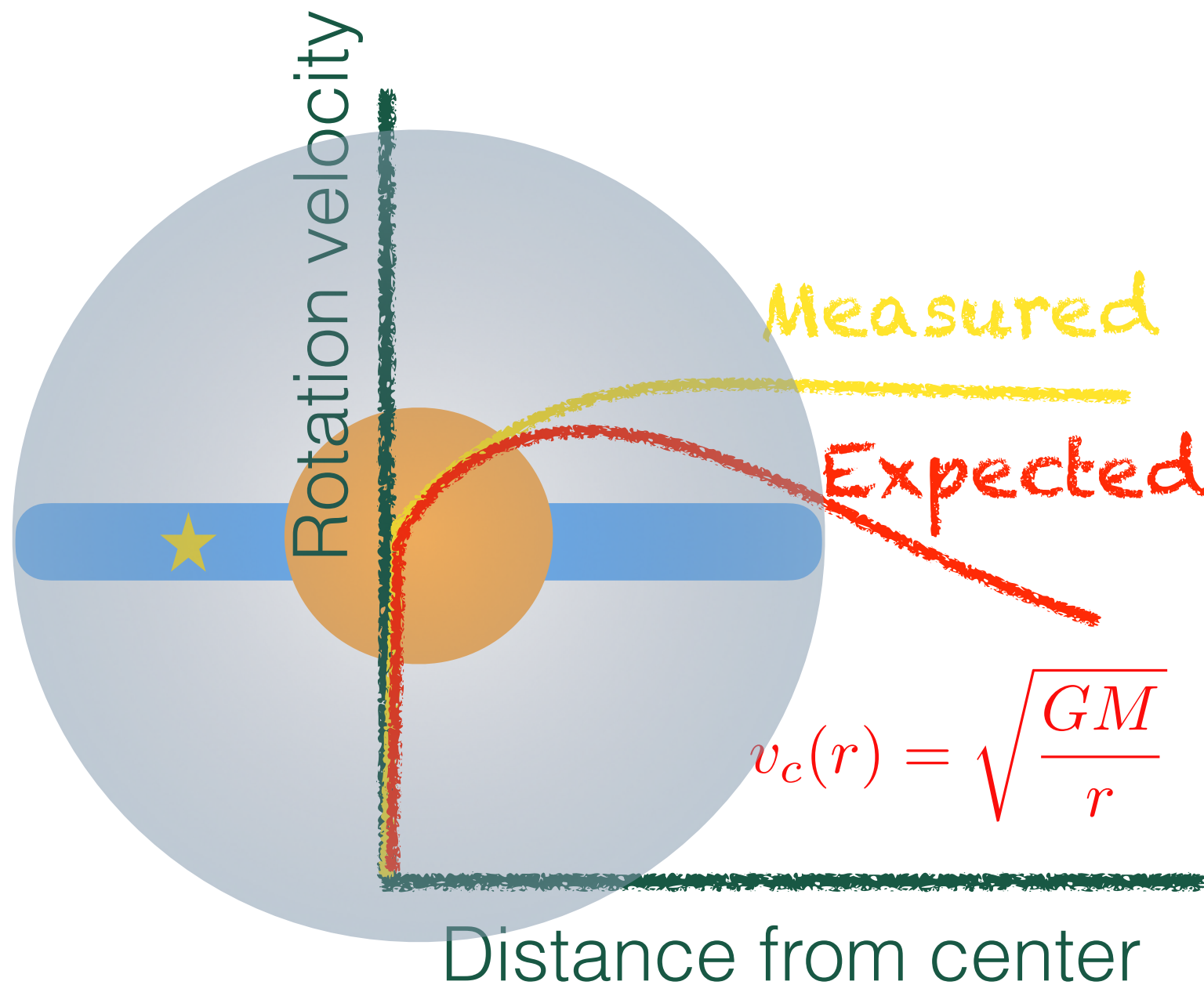


# Toy model of spiral galaxy





# Toy model of spiral galaxy





# Toy model of spiral galaxy

Flat rotation curve implies

$$M(r) \propto r$$

Assuming spherical symmetry

$$\rho(r) \propto \frac{1}{r^2}$$

$$M_{\text{Halo}} \sim 10^{12} M_{\odot}$$

$$R_{\text{Halo}} \sim 100 \text{ kpc}$$



$$\sim 15 \text{ kpc}$$

$$M_{\text{stellar}} \sim 5 \times 10^{10} M_{\odot}$$

$$\langle v \rangle \sim \sqrt{\frac{GM_{\text{Halo}}}{R_{\text{Halo}}}} \sim 200 \text{ km/s}$$



# Toy model of spiral galaxy

Flat rotation curve implies

$$M(r) \propto r$$

Assuming spherical symmetry

$$\rho(r) \propto \frac{1}{r^2}$$

$M_{\text{Halo}} \sim 10^{12} M_{\odot}$

$R_{\text{Halo}} \sim 100 \text{ kpc}$

$\sim 15 \text{ kpc}$

$M_{\text{stellar}} \sim 5 \times 10^{10} M_{\odot}$

$\langle v \rangle \sim \sqrt{\frac{GM_{\text{Halo}}}{R_{\text{Halo}}}} \sim 200 \text{ km/s}$

- Collisionless
- Nonrelativistic
- Self-gravitating
- Isotropic
- Isothermal gas

# Hierarchical Merger Model

---

- 1) Density fluctuations after big bang lead to proto-galactic fragments of order  $10^6 - 10^8 M_{\odot}$
- 2) Fragments evolve in isolation creating stars / globular clusters
- 3) Collisions and tidal disruptions lead to distribution of halo (stars and DM)
- 4) Gas in the mergers interact and collapse to disk
- 5) Young and metal rich stars produced in the disk

Last major merger  
~10 Gyr ago

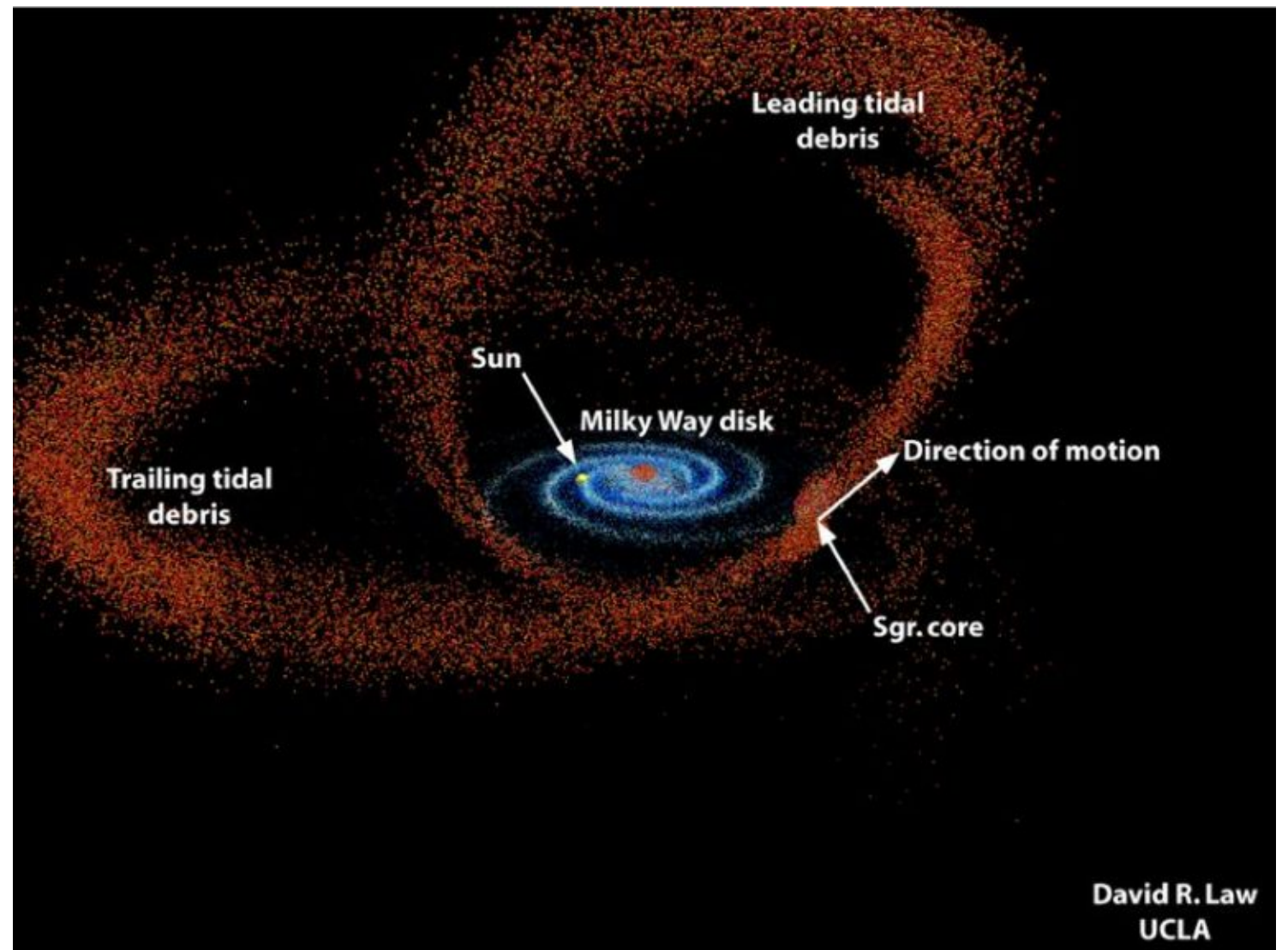
Minor mergers still  
happening



# Hierarchical Merger Model

Minor mergers still happening

Stars and DM in the proto-galactic fragments only interact via gravity



<http://www.stsci.edu/~dlaw/Sgr/TimeEvol.html>

To find dark matter distribution, find stars from early mergers

# Dark Matter Tracers

To find dark matter distribution, find stars from early mergers

Early merger → Old star → Low metallicity

$$[\text{Fe}/\text{H}] = \log_{10} \left( \frac{N_{\text{Fe}}}{N_{\text{H}}} \right) - \log_{10} \left( \frac{N_{\text{Fe}}}{N_{\text{H}}} \right)_{\odot}$$



# Dark Matter Tracers

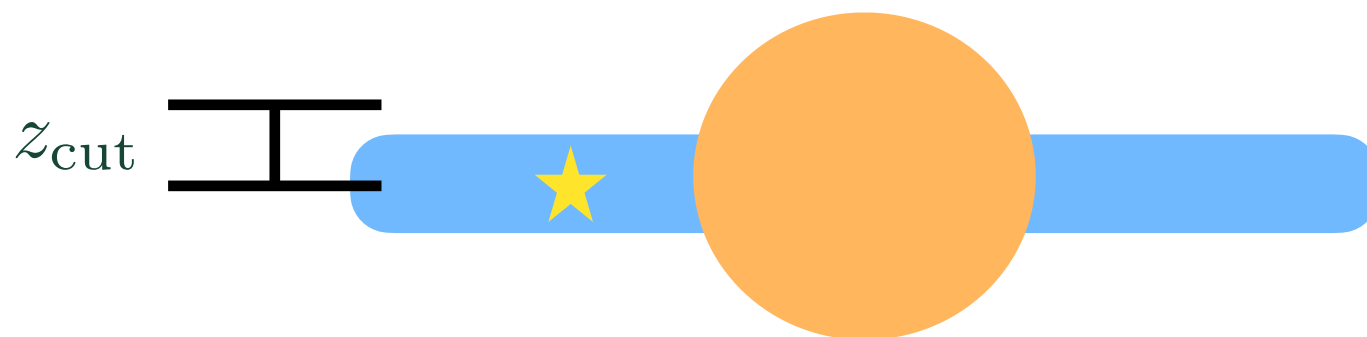
To find dark matter distribution, find stars from early mergers

Early merger → Old star → Low metallicity

$$[\text{Fe}/\text{H}] = \log_{10} \left( \frac{N_{\text{Fe}}}{N_{\text{H}}} \right) - \log_{10} \left( \frac{N_{\text{Fe}}}{N_{\text{H}}} \right)_{\odot}$$

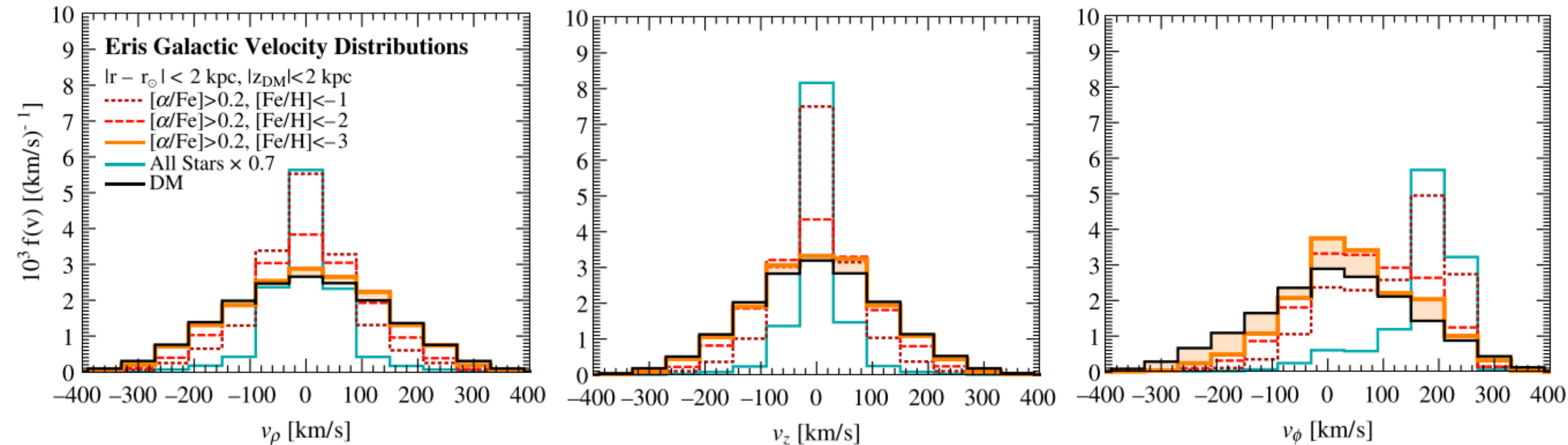
Also helps to not look directly in the disk

$$|z| > z_{\text{cut}}$$



# Dark Matter Tracers

To find dark matter distribution, find stars from early mergers



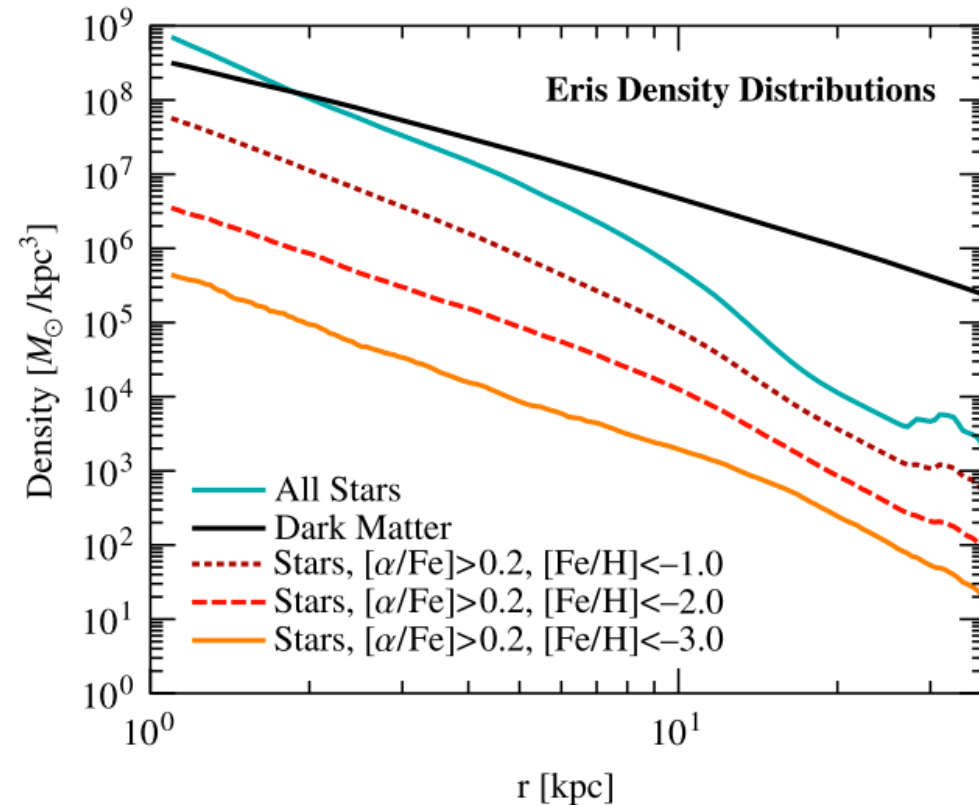
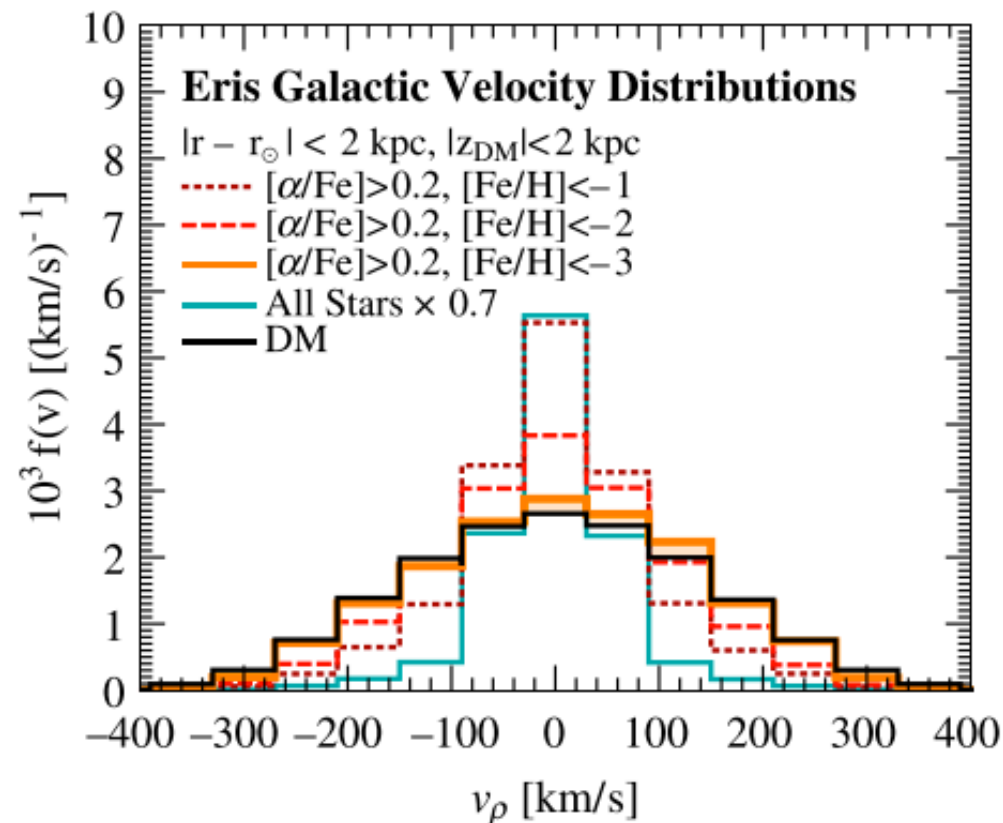
[arXiv:1704.04499]

Old (low  $[\text{Fe}/\text{H}]$ ) stars and dark matter share the same **velocity** distributions!



# Dark Matter Tracers

To find dark matter distribution, find stars from early mergers

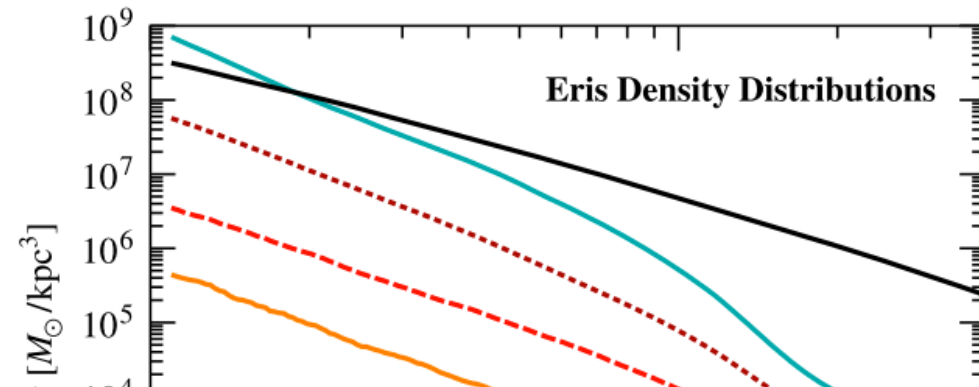
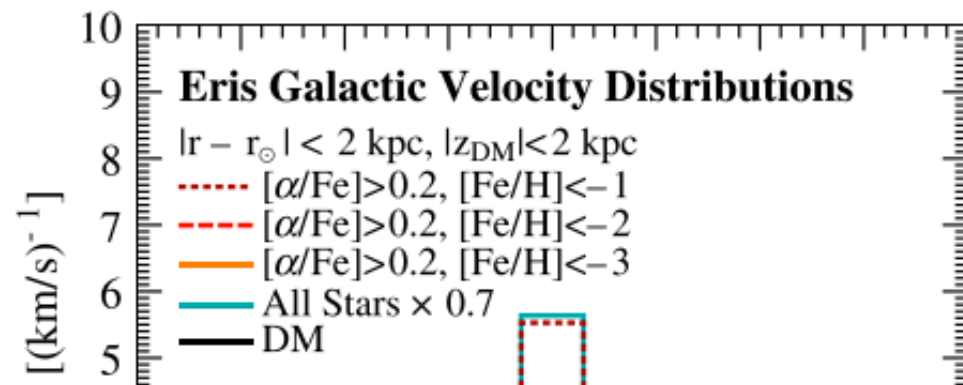


[arXiv:1704.04499]

Old (low  $[\text{Fe}/\text{H}]$ ) stars and dark matter share  
same **density** profile!

# Dark Matter Tracers

To find dark matter distribution, find stars from early mergers



Simulation shows old stars act as tracers

Now need to measure phase space of the old stars

[arXiv:1704.04499]

Old (low  $[\text{Fe}/\text{H}]$ ) stars and dark matter share  
same **density** profile!



# Catalogs of real data

## Phase Space (5-d)

- Gaia DR1 (2-d) location for 1 billion stars
  - ★ Cross matched with Tycho-2 catalog of Hipparcos → 2 million stars
- Gaia DR2 (5-d) information for 1 billion stars

## Spectroscopy

- Radial VELOCITY Experiment
- Sloan Digital Sky Survey

# Catalogs of real data

## Phase Space (5-d)

- Gaia DR1 (2-d) location for 1 billion stars
  - ★ Cross matched with Tycho-2 catalog of Hipparcos → 2 million stars
- Gaia DR2 (5-d) information for 1 billion stars

## Spectroscopy

- Radial VElocity Experiment
- Sloan Digital Sky Survey

RAVE-TGAS (255,922 stars)

# Catalogs of real data

## Phase Space (5-d)

- Gaia DR1 (2-d) location for 1 billion stars
  - ★ Cross matched with Tycho-2 catalog of Hipparcos → 2 million stars
- Gaia DR2 (5-d) information for 1 billion stars

## Spectroscopy

- Radial VElocity Experiment

- Sloan Digital Sky Survey

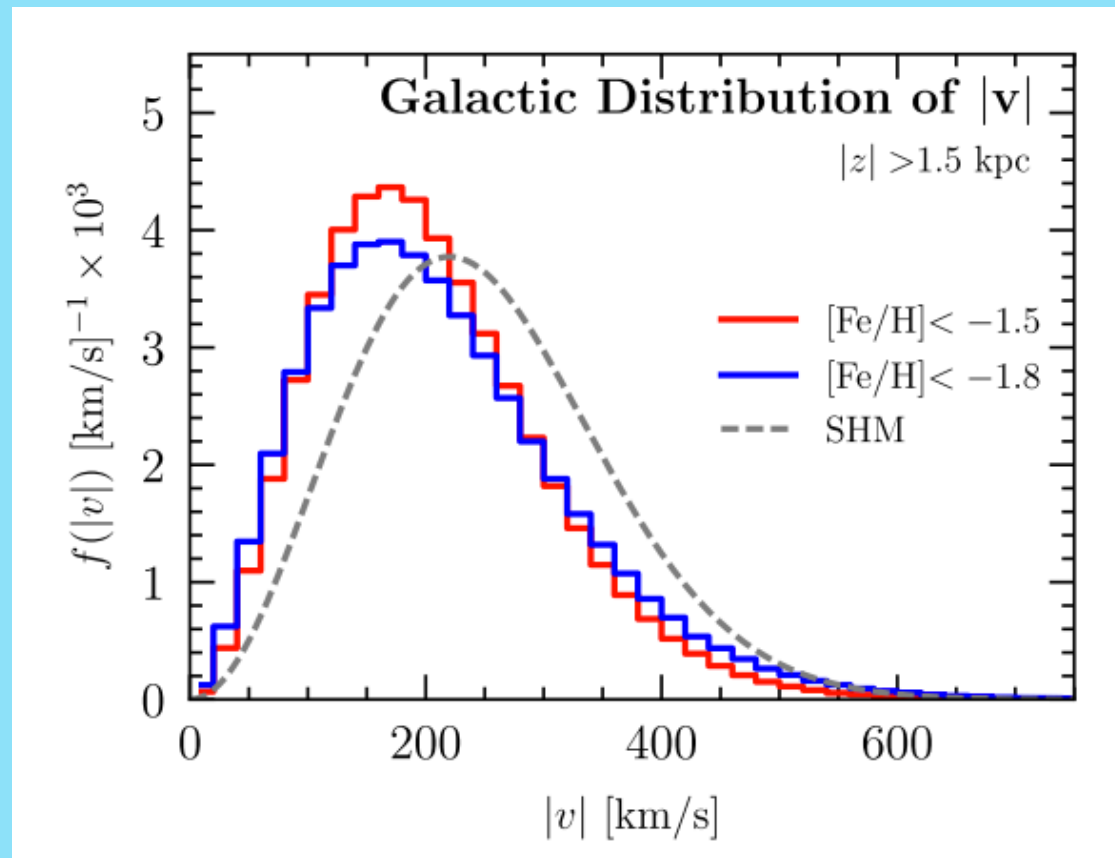
RAVE-TGAS (255,922 stars)

Gaia-SDSS (193,162 stars)



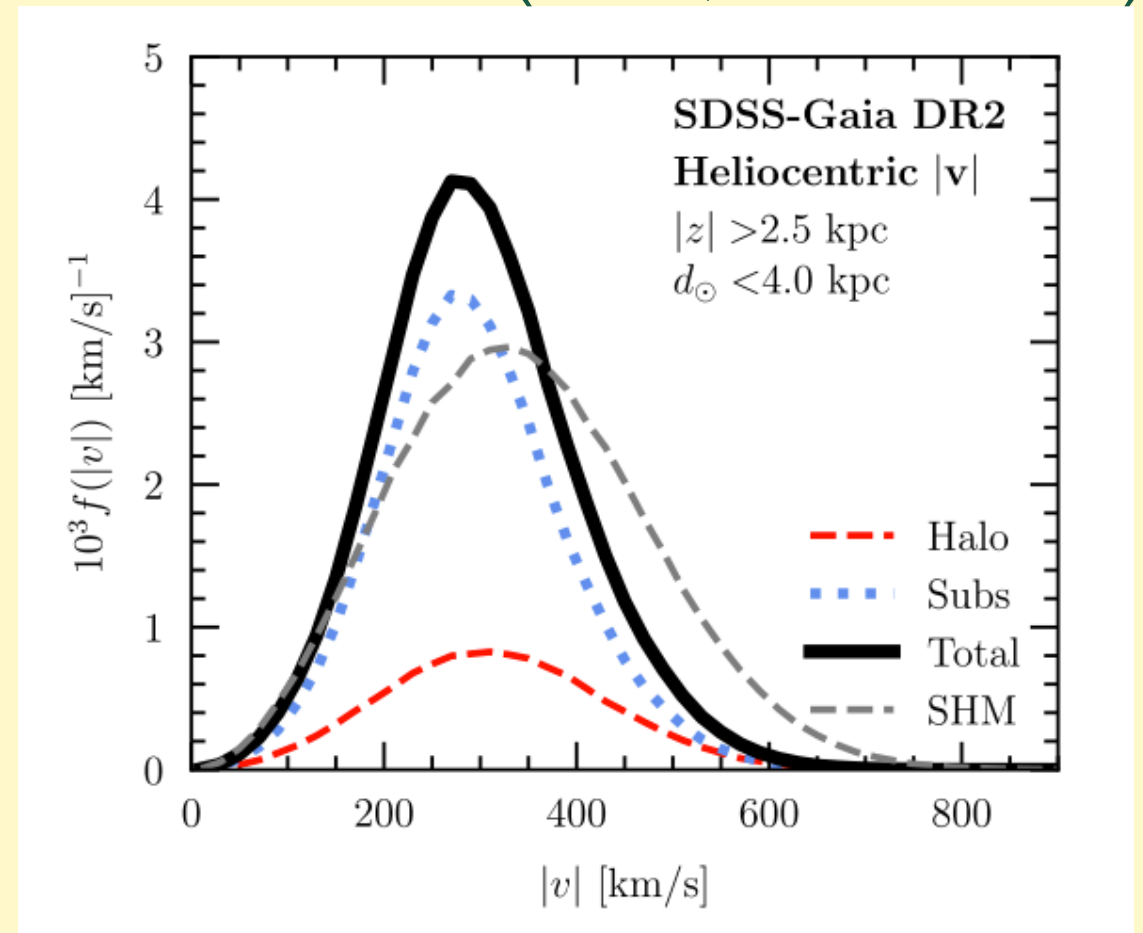
# Catalogs of real data

## RAVE-TGAS (255,922 stars)



J. Herzog-Arbeitman, M. Lisanti and L. Necib, JCAP **1804**, no. 04, 052 (2018) doi:10.1088/1475-7516/2018/04/052 [arXiv:1708.03635 [astro-ph.GA]].

## Gaia-SDSS (193,162 stars)



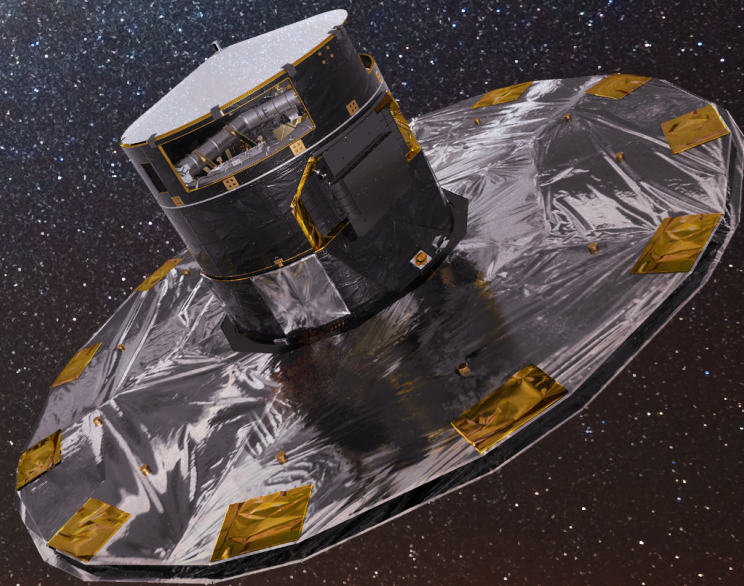
L. Necib, M. Lisanti and V. Belokurov, arXiv:1807.02519 [astro-ph.GA].

Empirical determination of halo velocity distribution smaller than standard model halo → direct detection interpretation



Gaia measures 5-d information of 1 billion stars

Requiring spectroscopic  
data reduces size of  
dataset available



Gaia Artist's impression - credits: ESA/ATG medialab; background image: ESO/S. Brunier \*\*\*\*\* June 2013

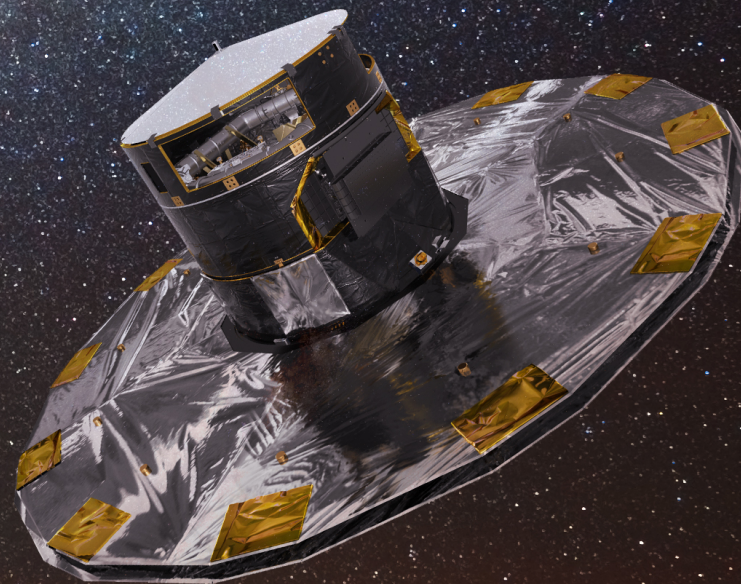
Is it possible to classify halo stars using only  
5-d information?



Gaia measures 5-d information of 1 billion stars

Requiring spectroscopic  
data reduces size of  
dataset available

Use deep neural  
network as generic  
distribution fitter



Gaia Artist's impression - credits: ESA/ATG medialab; background image: ESO/S. Brunier \*\*\*\*\* June 2013

Is it possible to classify halo stars using only  
5-d information?



# Brief aside on Machine Learning



<https://www.techemergence.com/what-is-machine-learning/>

# Review: Linear Regression

## How to fit data

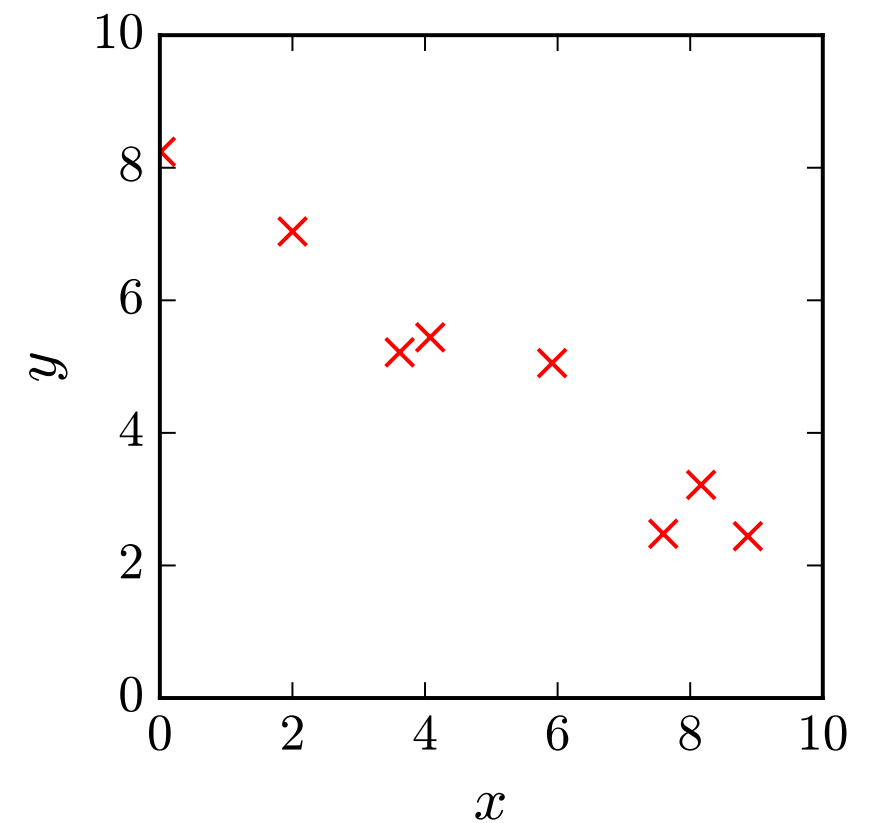
1. Plot the data
2. Define the function
  - $f(x, \vec{a}) = a_0 + a_1 x$
3. Choose how to know what fits best

- a.k.a. *Loss Function*

- MSE: 
$$L(x, y, \vec{a}) = \frac{1}{N} \sum_{i=1}^N (f(x_i, \vec{a}) - y_i)^2$$

5. Find the minimum error (loss) (cost)

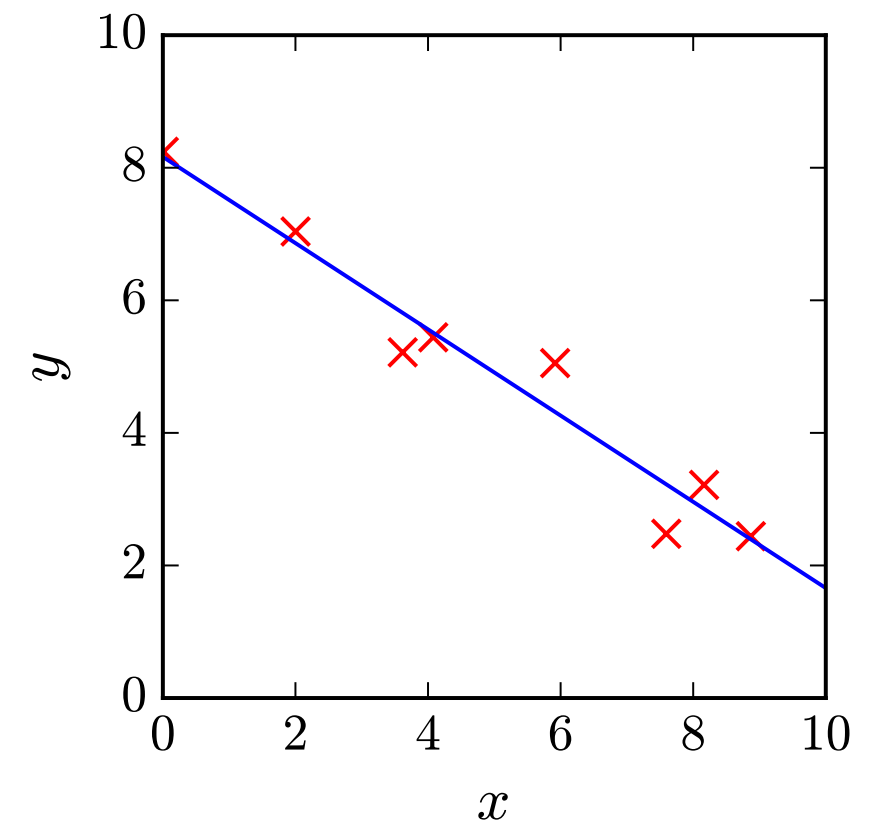
- $a_{\text{best}} = a$  when  $\left( \frac{\partial L(x, y, \vec{a})}{\partial \vec{a}} \right) \Big|_{x, y} = 0$



# Review: Linear Regression

## How to fit data

1. Plot the data
2. Define the function
  - $f(x, \vec{a}) = a_0 + a_1x$
3. Choose how to know what fits best
  - a.k.a. *Loss Function*



- MSE:  $L(x, y, \vec{a}) = \frac{1}{N} \sum_{i=1}^N (f(x_i, \vec{a}) - y_i)^2$
5. Find the minimum error (loss) (cost)
    - $a_{\text{best}} = a$  when  $\left( \frac{\partial L(x, y, \vec{a})}{\partial \vec{a}} \right) \Big|_{x, y} = 0$



# Review: Linear Regression

## How to fit data

1. Plot the data
2. Define the function
3. Choose how to know what fits best

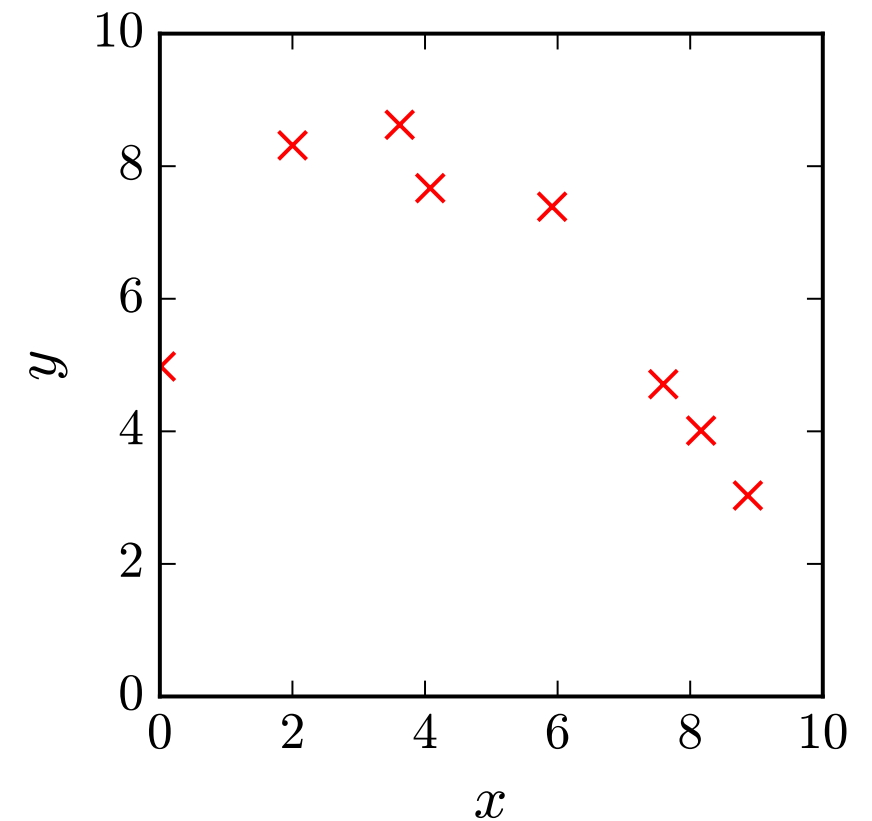
- $f(x, \vec{a}) = a_0 + a_1x + a_2x^2$

- a.k.a. *Loss Function*

- MSE:  $L(x, y, \vec{a}) = \frac{1}{N} \sum_{i=1}^N (f(x_i, \vec{a}) - y_i)^2$

5. Find the minimum error (loss) (cost)

- $a_{\text{best}} = a$  when  $\left( \frac{\partial L(x, y, \vec{a})}{\partial \vec{a}} \right) \Big|_{x, y} = 0$



# Review: ~~Linear~~ Regression

Quadratic?

## How to fit data

1. Plot the data
2. Define the function
3. Choose how to know what fits best

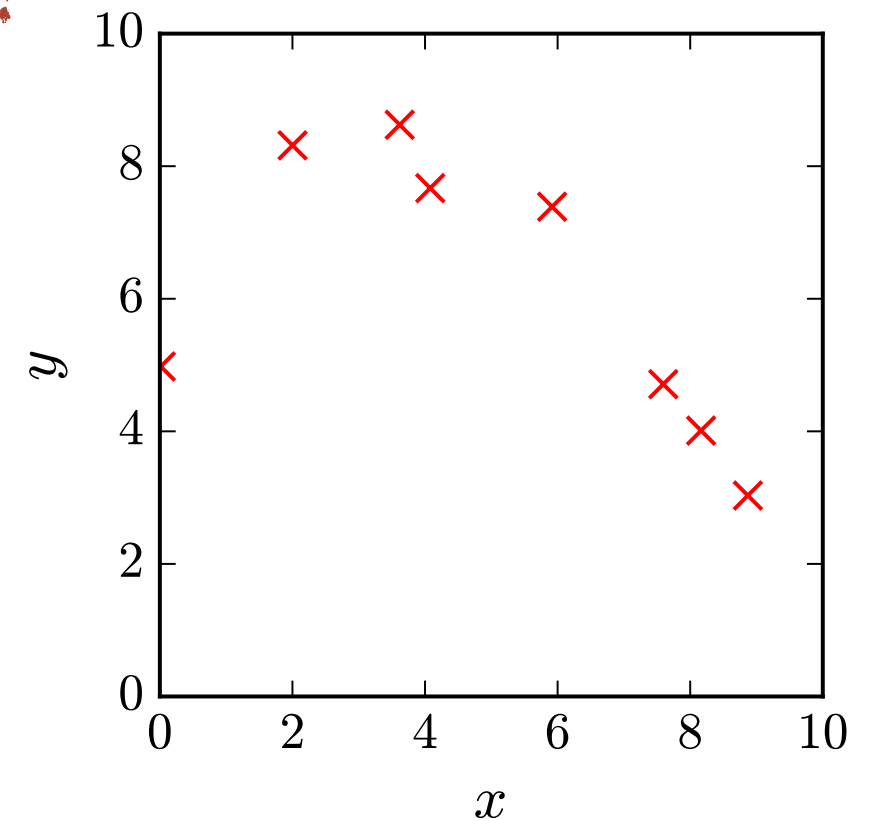
- $f(x, \vec{a}) = a_0 + a_1x + a_2x^2$

- a.k.a. *Loss Function*

- MSE:  $L(x, y, \vec{a}) = \frac{1}{N} \sum_{i=1}^N (f(x_i, \vec{a}) - y_i)^2$

5. Find the minimum error (loss) (cost)

- $a_{\text{best}} = a$  when  $\left( \frac{\partial L(x, y, \vec{a})}{\partial \vec{a}} \right) \Big|_{x, y} = 0$



# Review: ~~Linear~~ Regression

Quadratic?

## How to fit data

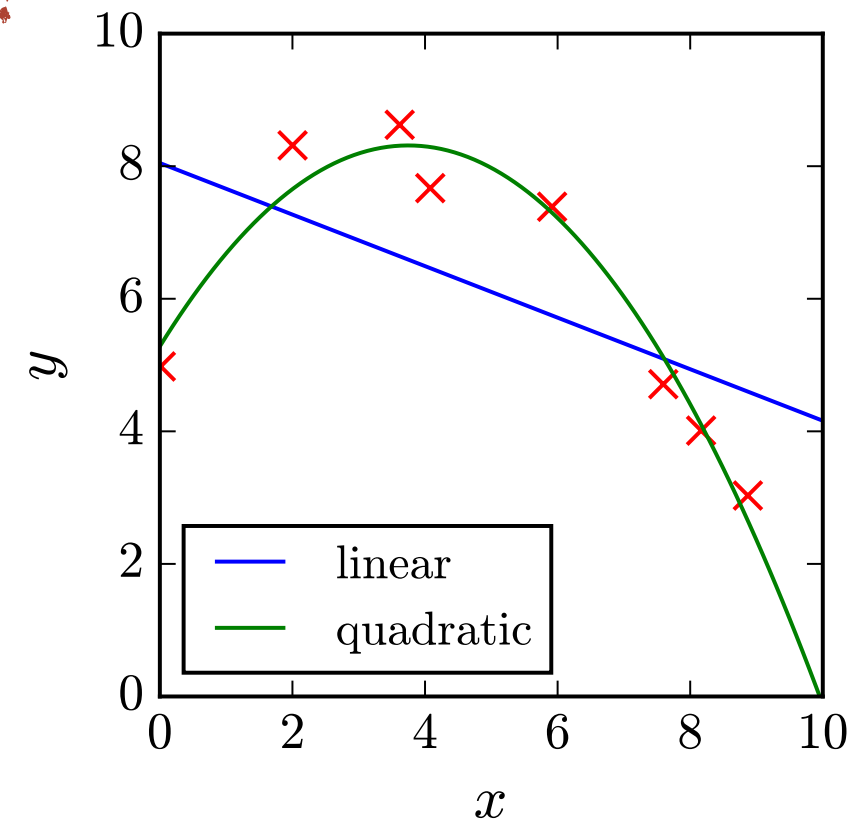
1. Plot the data
2. Define the function
  - $f(x, \vec{a}) = a_0 + a_1x + a_2x^2$
3. Choose how to know what fits best

- a.k.a. *Loss Function*

- MSE:  $L(x, y, \vec{a}) = \frac{1}{N} \sum_{i=1}^N (f(x_i, \vec{a}) - y_i)^2$

5. Find the minimum error (loss) (cost)

- $a_{\text{best}} = a$  when  $\left( \frac{\partial L(x, y, \vec{a})}{\partial \vec{a}} \right) \Big|_{x, y} = 0$





# Review: ~~Linear~~ Regression

Quadratic?

## How to fit data

1. Plot the data
2. Define the function
3. Choose how to know what fits best

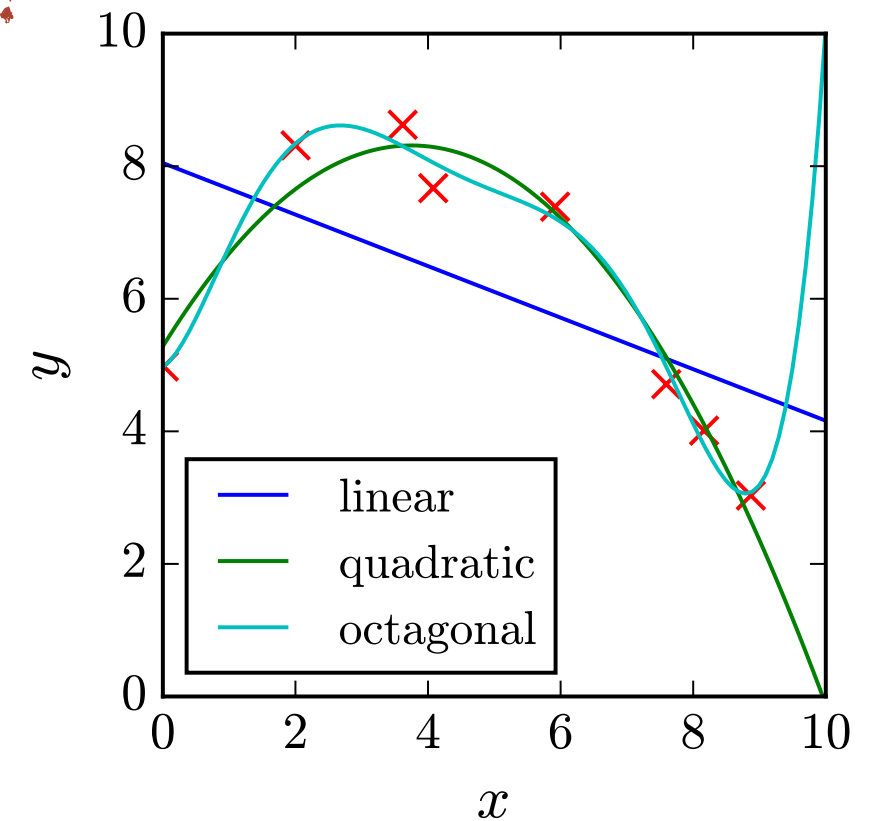
- $f(x, \vec{a}) = a_0 + a_1x + a_2x^2$

- a.k.a. *Loss Function*

- MSE:  $L(x, y, \vec{a}) = \frac{1}{N} \sum_{i=1}^N (f(x_i, \vec{a}) - y_i)^2$

5. Find the minimum error (loss) (cost)

- $a_{\text{best}} = a$  when  $\left( \frac{\partial L(x, y, \vec{a})}{\partial \vec{a}} \right) \Big|_{x,y} = 0$



Is that good enough?  
How many  
parameters can we  
add?

# Logistic Regression

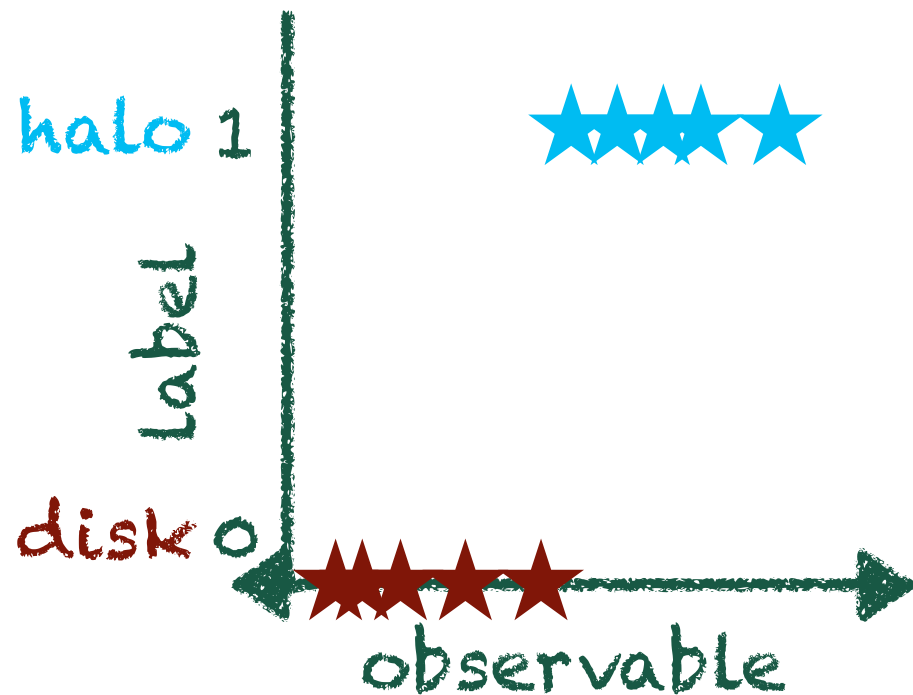
---

What if we are trying to predict a class, not a number?



# Logistic Regression

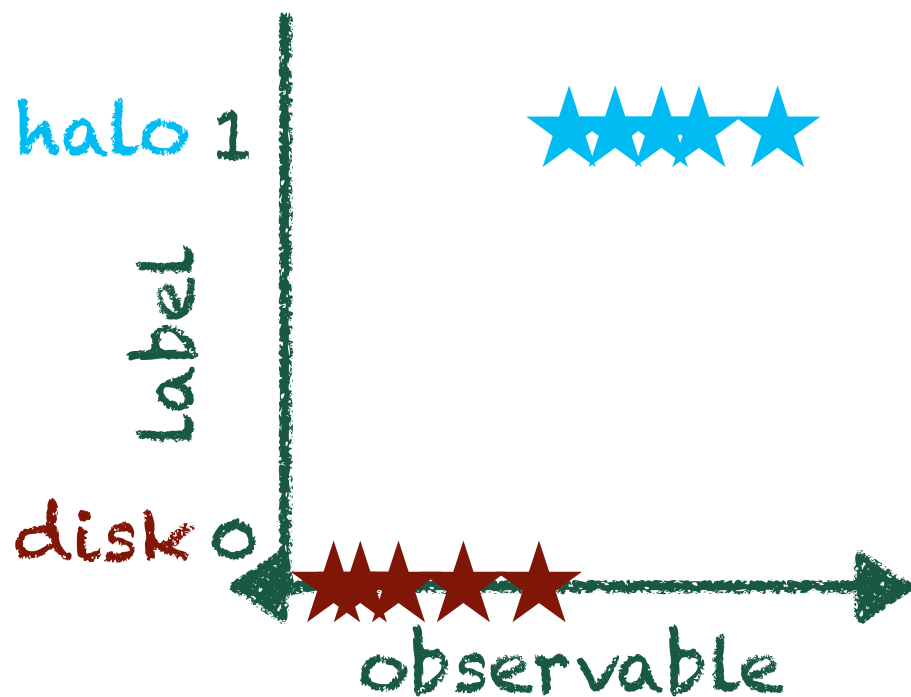
What if we are trying to predict a class, not a number?



# Logistic Regression

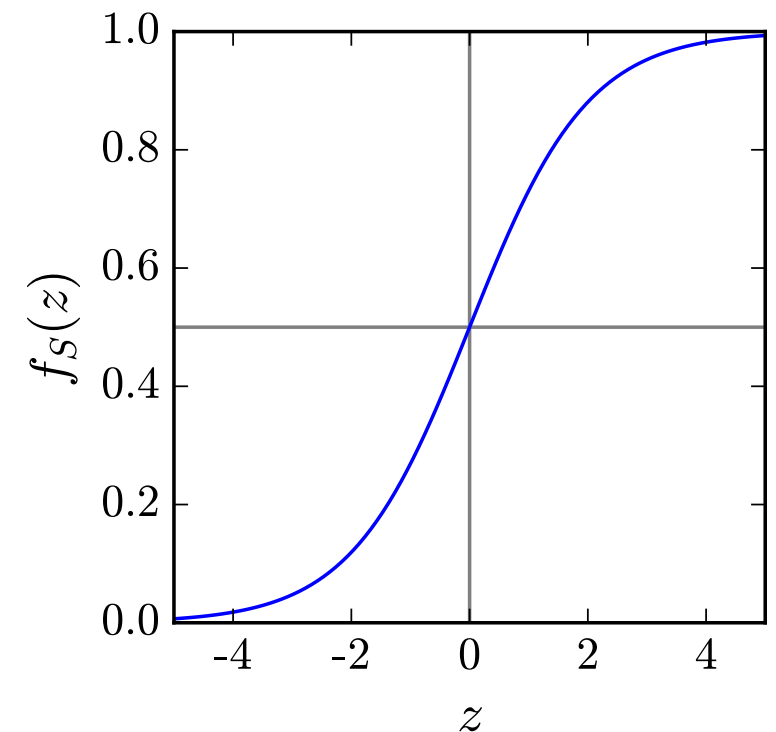
What if we are trying to predict a class, not a number?

- Change the shape of function: Logistic/Sigmoid function



$$f_S(z) = \frac{1}{1 + e^{-z}}$$

Does not add  
parameters

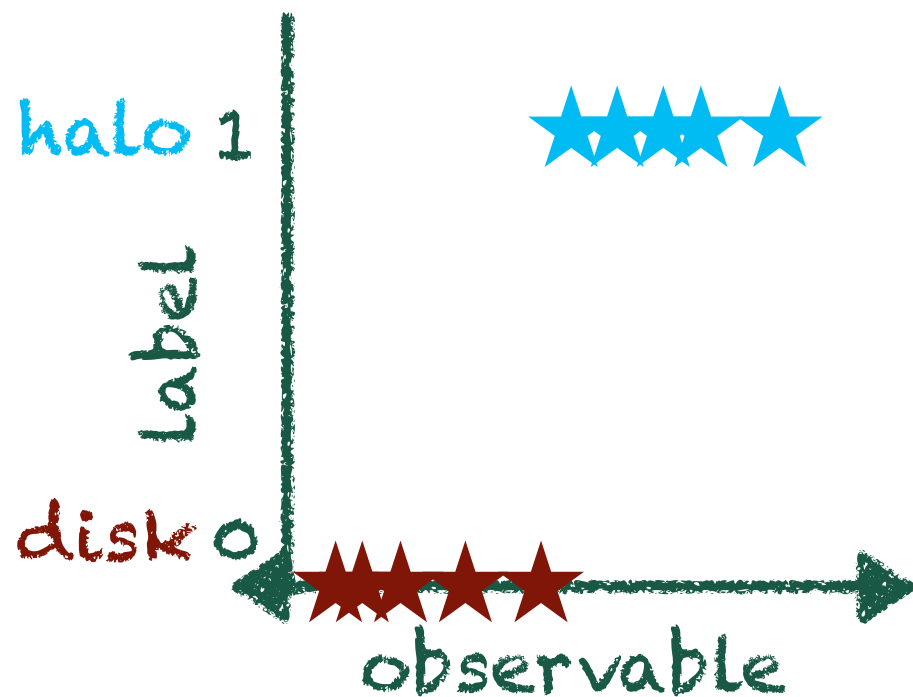




# Logistic Regression

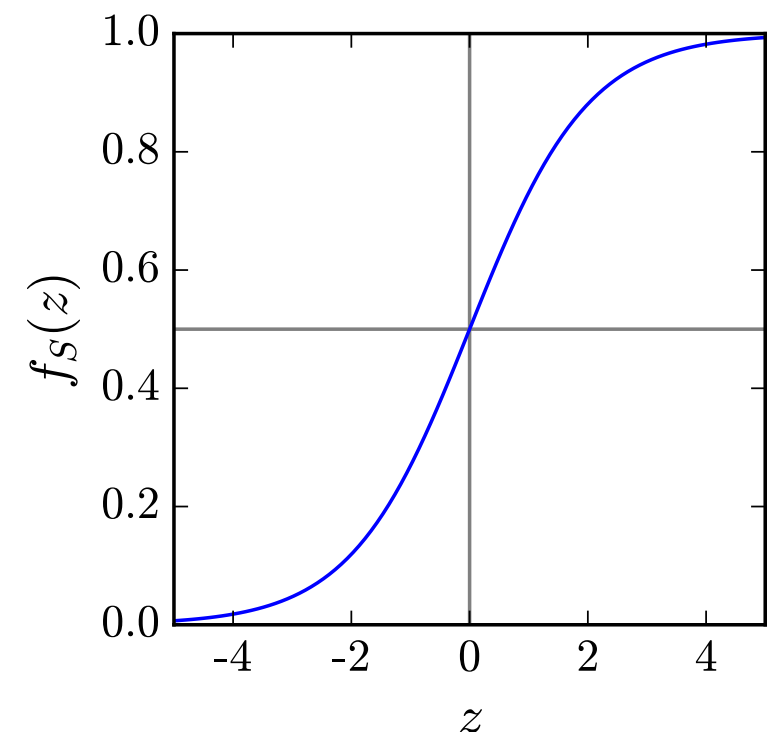
What if we are trying to predict a class, not a number?

- Change the shape of function: Logistic/Sigmoid function



$$f_S(z) = \frac{1}{1 + e^{-z}}$$

Does not add parameters

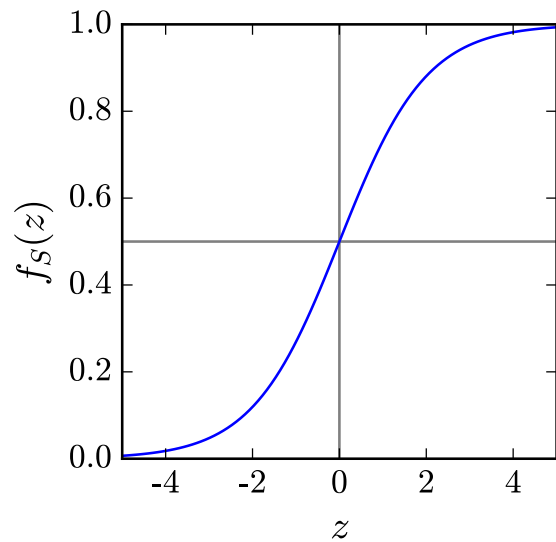


- Change the loss function: BCE

$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log \left( f_S(p(x, a)) \right) + (1 - y_i) \log \left( 1 - f_S(p(x, a)) \right) \right)$$

# Logistic Regression

What if we are trying to predict a class, not a number?

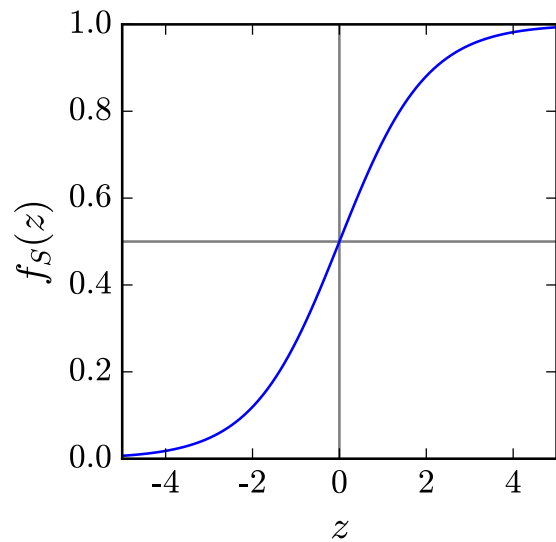


$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log \left( f_S(p(x, a)) \right) + (1 - y_i) \log \left( 1 - f_S(p(x, a)) \right) \right)$$

$$f_S(z) = \frac{1}{1 + e^{-z}} \quad z = p(x, a)$$

# Logistic Regression

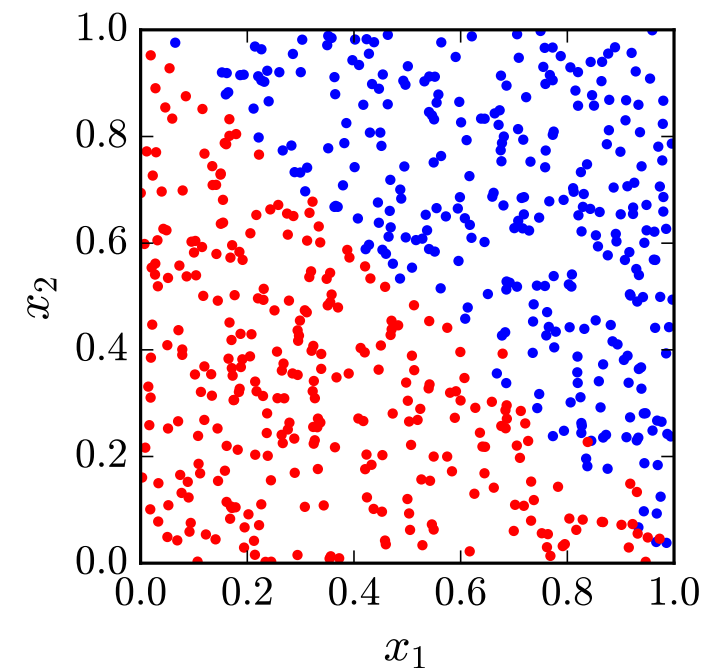
What if we are trying to predict a class, not a number?



$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log \left( f_S(p(x, a)) \right) + (1 - y_i) \log \left( 1 - f_S(p(x, a)) \right) \right)$$

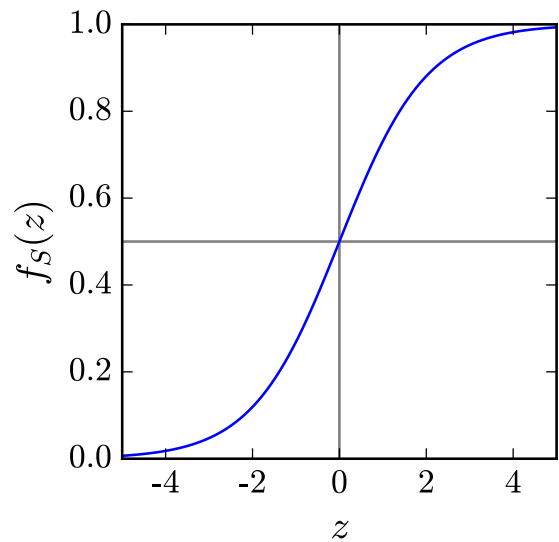
$$f_S(z) = \frac{1}{1 + e^{-z}} \quad z = p(x, a)$$

What is  $p(x, a)$ ?



# Logistic Regression

What if we are trying to predict a class, not a number?

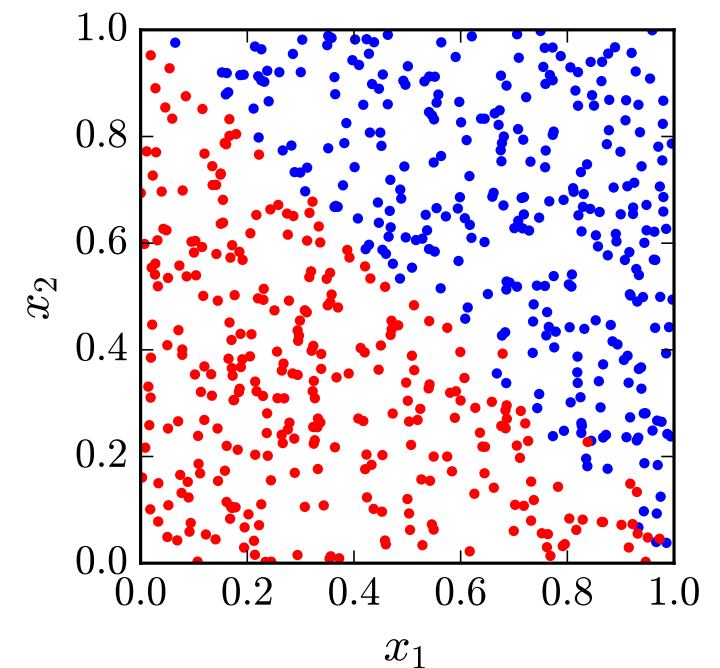
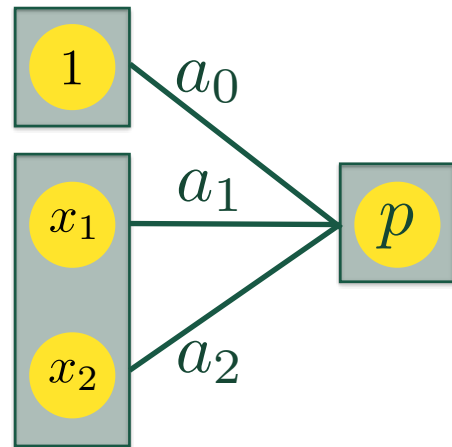


$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log(f_S(p(x, a))) + (1 - y_i) \log(1 - f_S(p(x, a))) \right)$$

$$f_S(z) = \frac{1}{1 + e^{-z}} \quad z = p(x, a)$$

What is  $p(x, a)$ ?

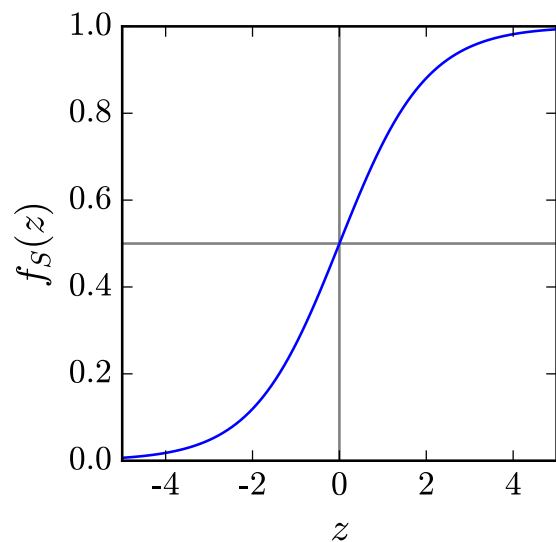
$$p(x, a) = a_0 + x_1 a_1 + x_2 a_2$$





# Logistic Regression

What if we are trying to predict a class, not a number?

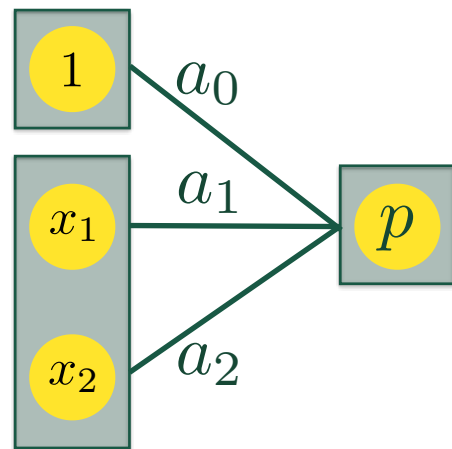


$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log(f_S(p(x, a))) + (1 - y_i) \log(1 - f_S(p(x, a))) \right)$$

$$f_S(z) = \frac{1}{1 + e^{-z}} \quad z = p(x, a)$$

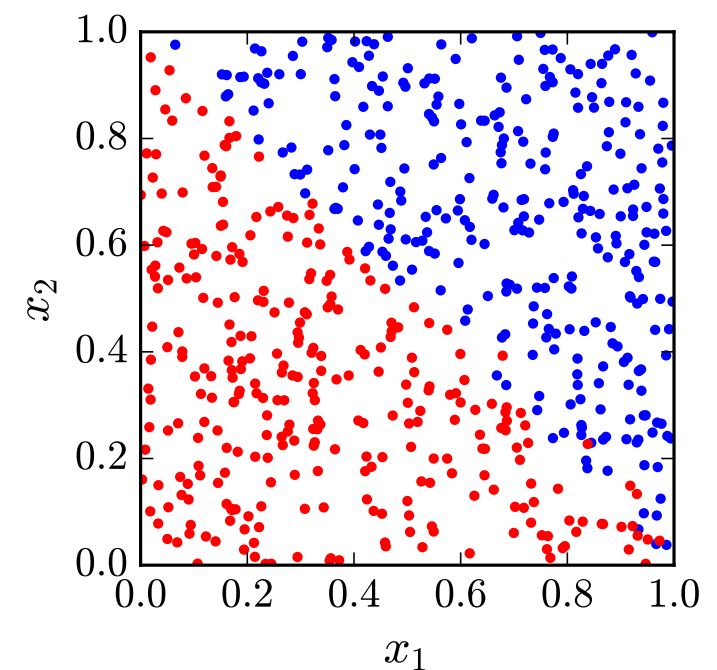
What is  $p(x, a)$ ?

$$p(x, a) = a_0 + x_1 a_1 + x_2 a_2$$



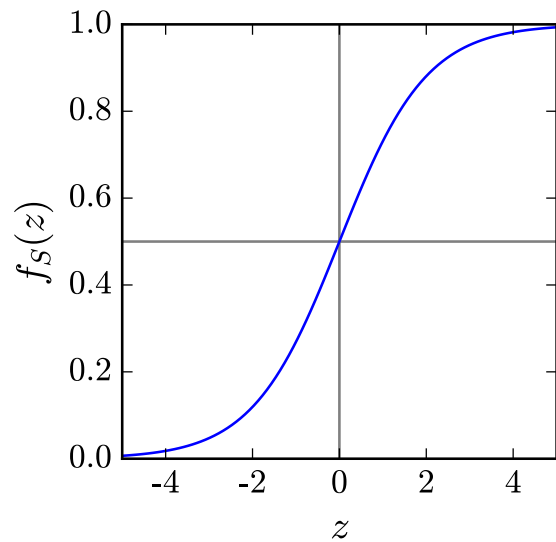
Minimize the loss with respect to  $\vec{a}$

Boundary at  $p(x, a) = 0$



# Logistic Regression

What if we are trying to predict a class, not a number?



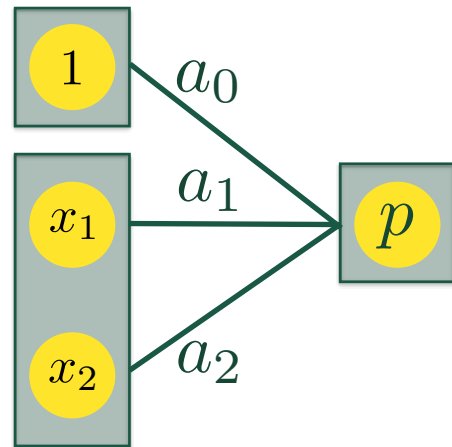
$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log(f_S(p(x, a))) + (1 - y_i) \log(1 - f_S(p(x, a))) \right)$$

$$f_S(z) = \frac{1}{1 + e^{-z}} \quad z = p(x, a)$$

What is  $p(x, a)$ ?

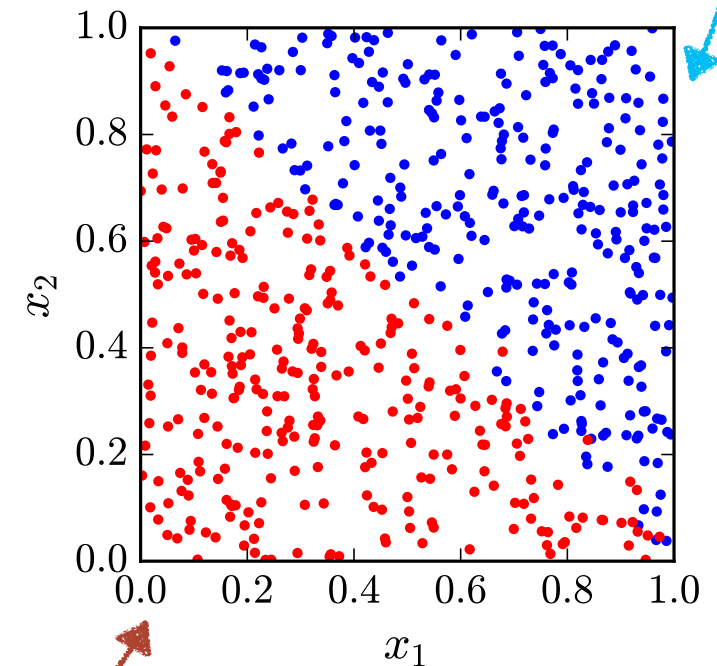
Large + values of  $p$

$$p(x, a) = a_0 + x_1 a_1 + x_2 a_2$$



Minimize the loss with respect to  $\vec{a}$

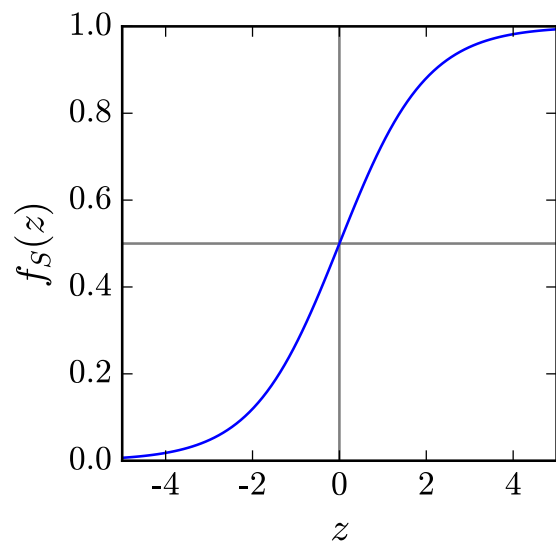
Boundary at  $p(x, a) = 0$



Large - values of  $p$

# Logistic Regression

What if we are trying to predict a class, not a number?

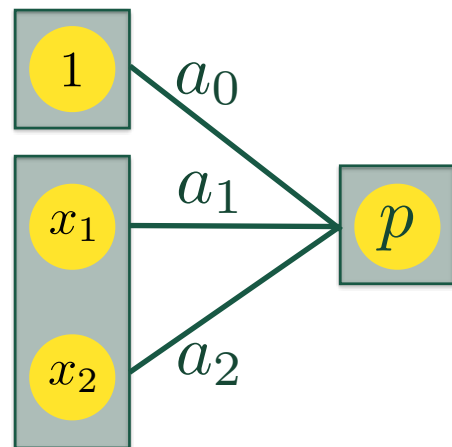


$$L(\vec{x}, \vec{y}, \vec{a}) = -\frac{1}{N} \sum_{i=1}^N \left( y_i \log(f_S(p(x, a))) + (1 - y_i) \log(1 - f_S(p(x, a))) \right)$$

$$f_S(z) = \frac{1}{1 + e^{-z}} \quad z = p(x, a)$$

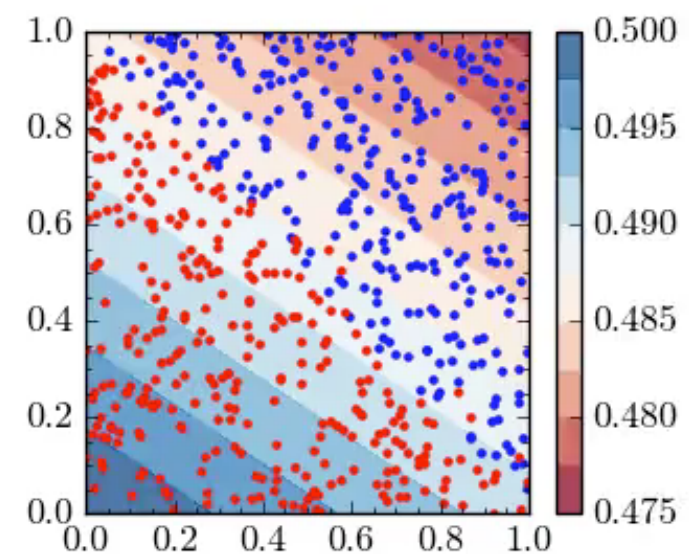
What is  $p(x, a)$ ?

$$p(x, a) = a_0 + x_1 a_1 + x_2 a_2$$



Minimize the loss with respect to  $\vec{a}$

Boundary at  $p(x, a) = 0$

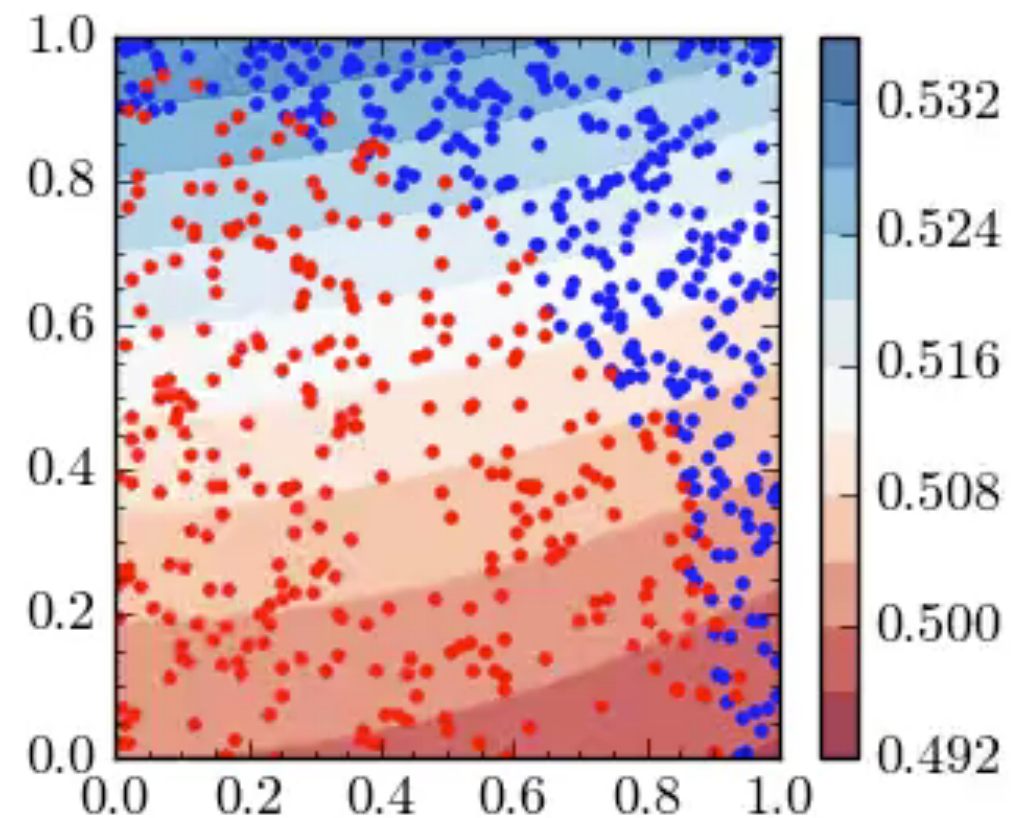
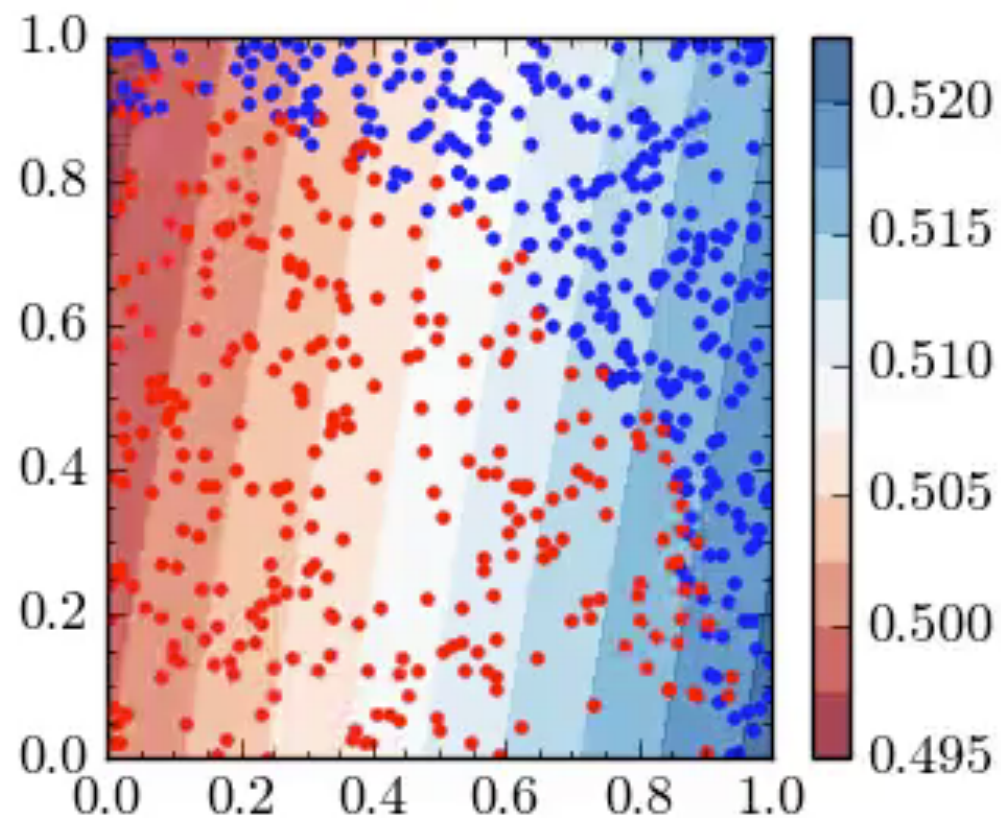


# Logistic Regression

What if there is a shape in the data?

$$p(x, a) = a_0 + x_1 a_1 + x_2 a_2$$

$$p(x, a) = a_0 + a_1 x_1 + a_2 x_2 + a_3 x_1^2 + a_4 x_2^2 + a_5 x_1 x_2$$



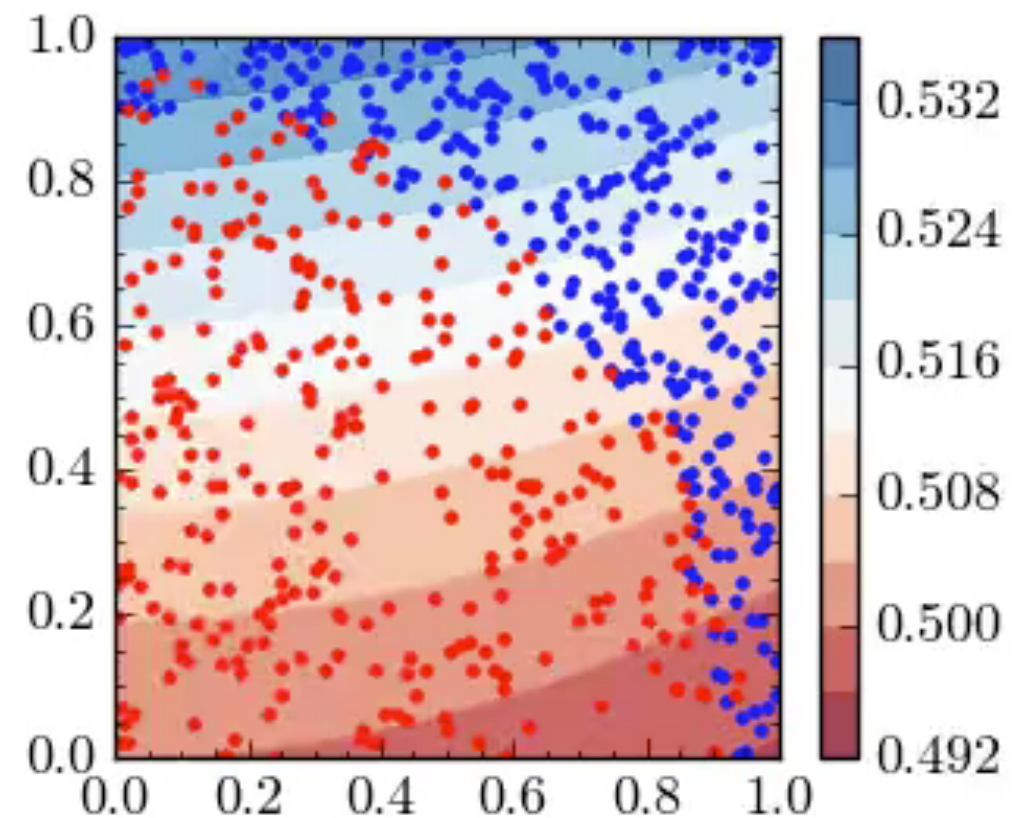
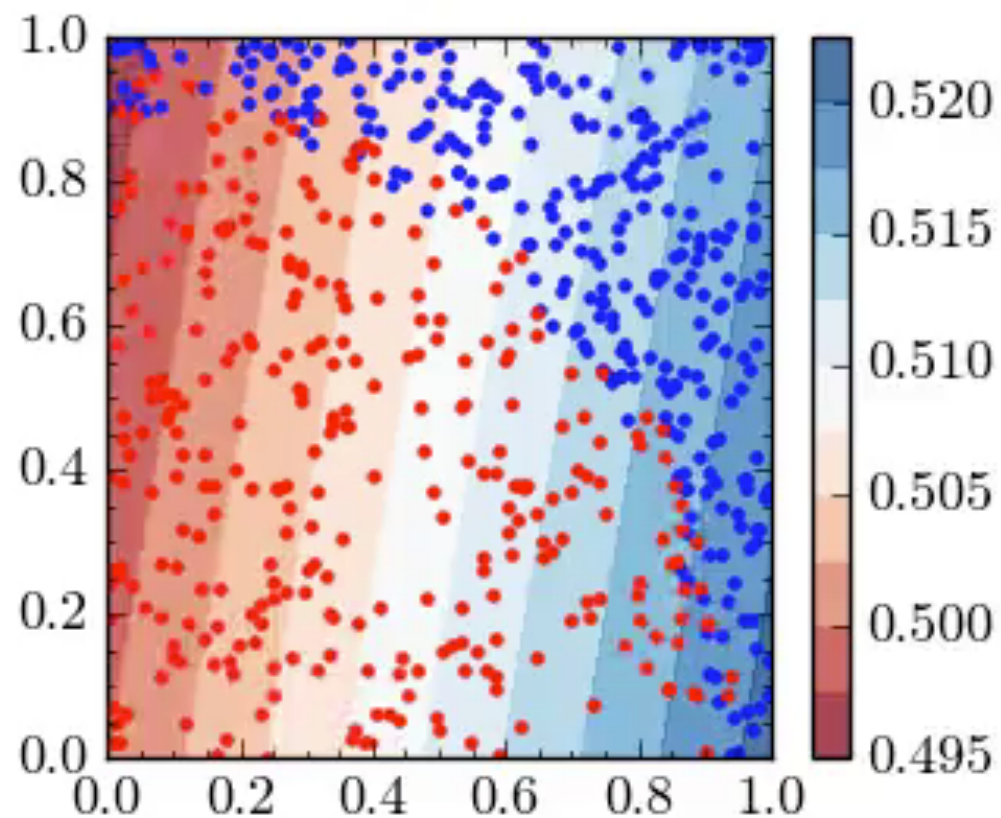


# Logistic Regression

What if there is a shape in the data?

$$p(x, a) = a_0 + x_1 a_1 + x_2 a_2$$

$$p(x, a) = a_0 + a_1 x_1 + a_2 x_2 + a_3 x_1^2 + a_4 x_2^2 + a_5 x_1 x_2$$

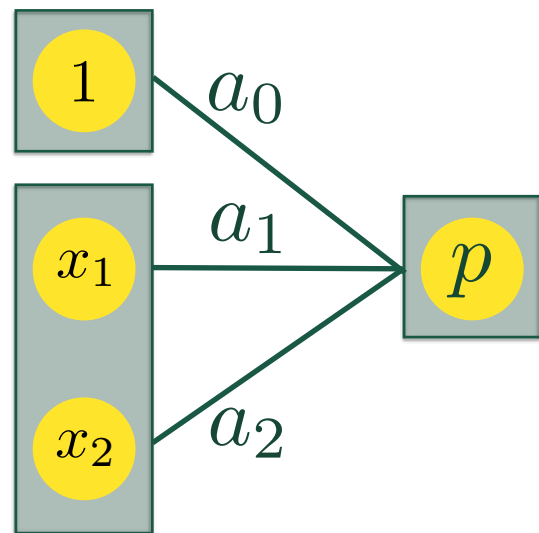


# Regression Review

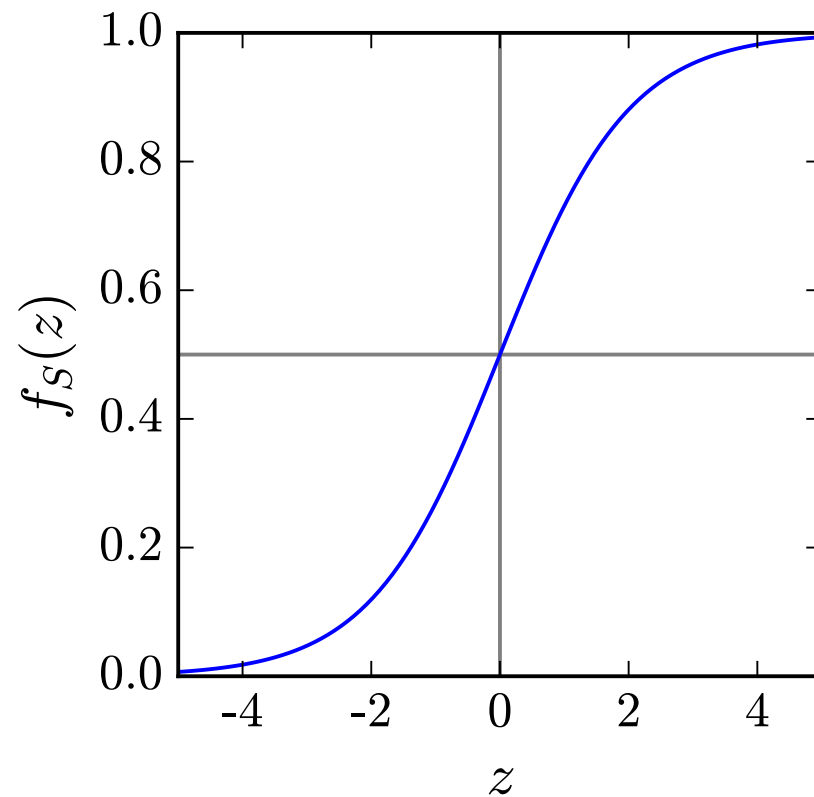
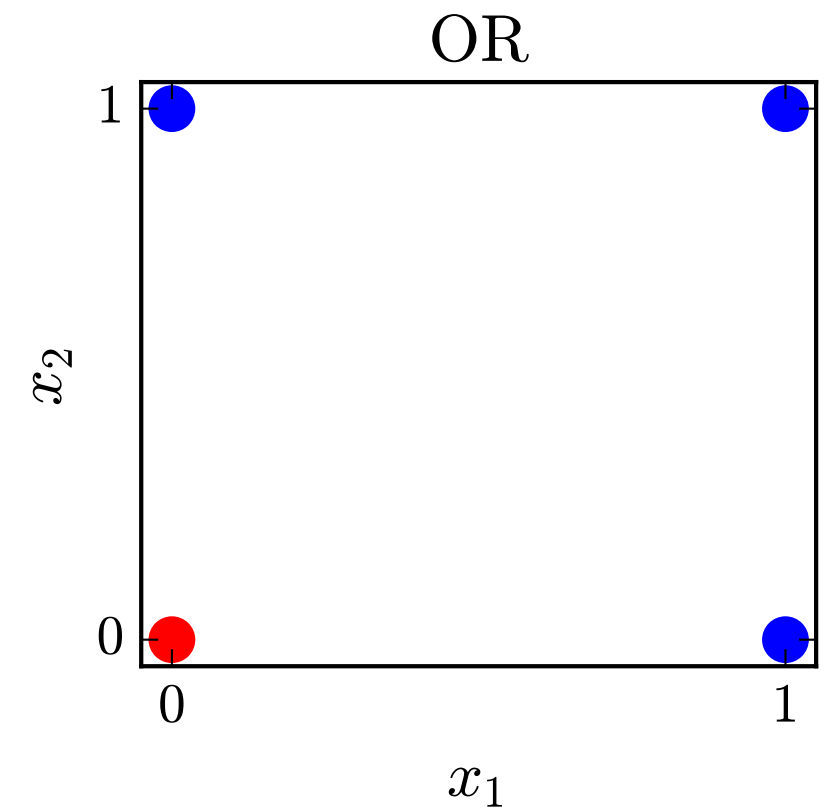
---

1. Can use nearly the same process for fitting a curve (predicting a number) or classification
2. Minimize a defined cost function
3. Easy to add parameters if shape is unknown — worry about over-fitting
4. If many inputs and complicated shapes, number of parameters necessary grows very quickly

# Neural Networks

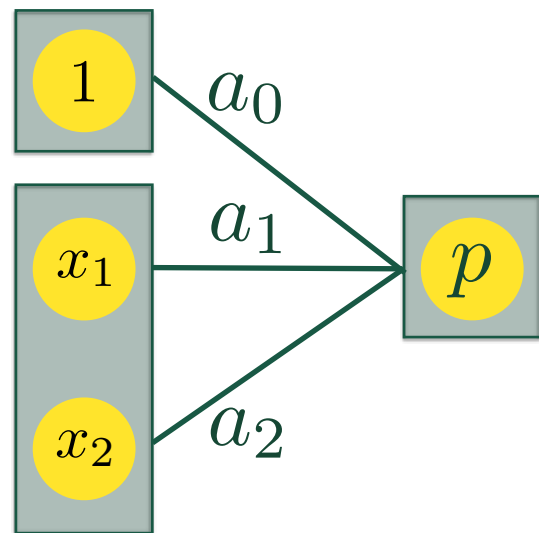


OR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	1

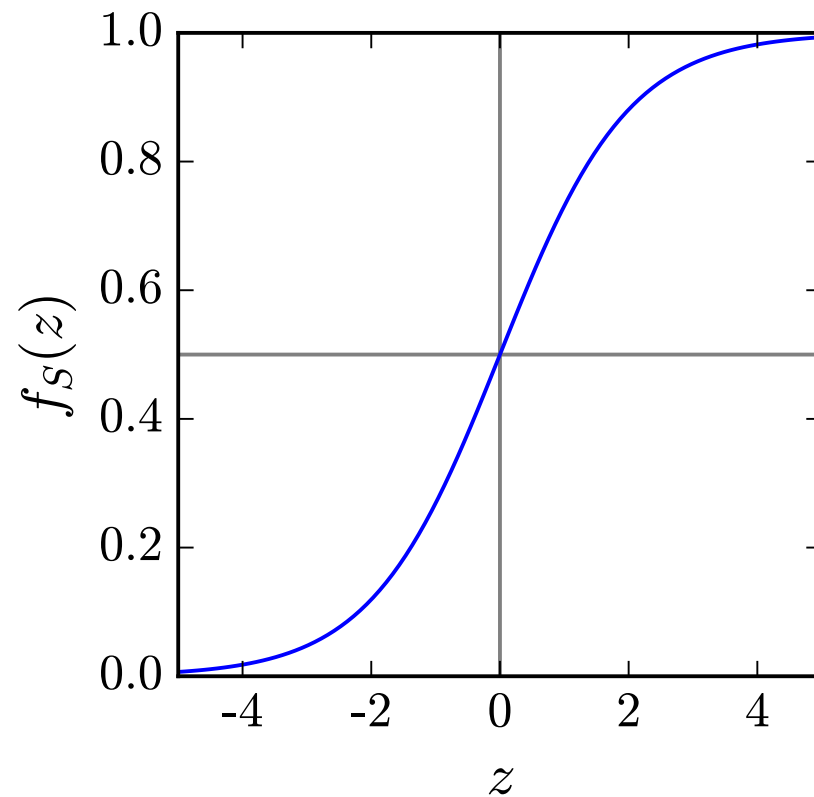
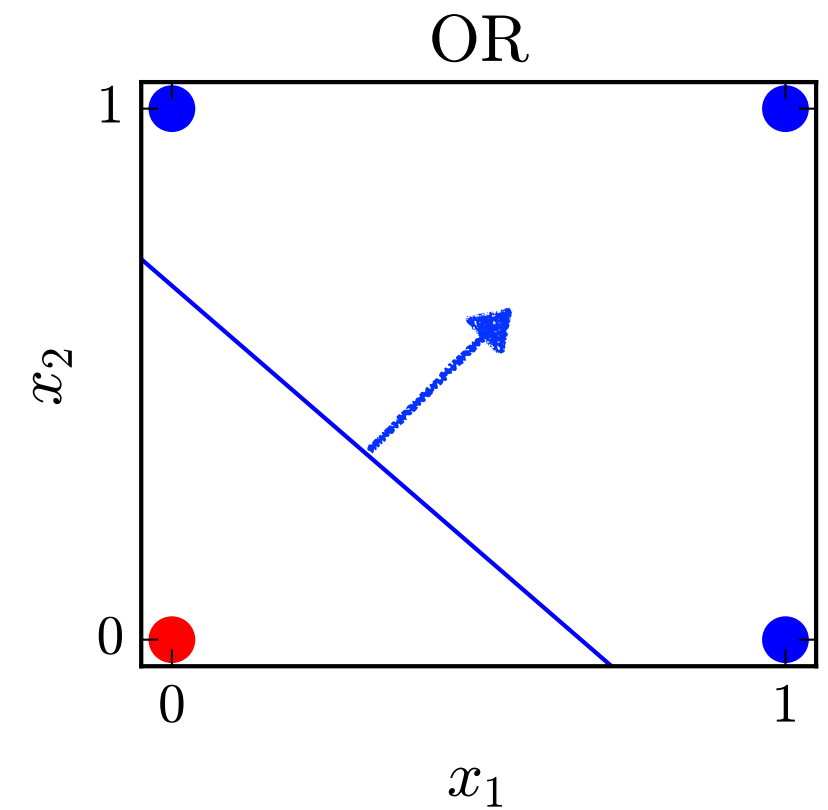




# Neural Networks

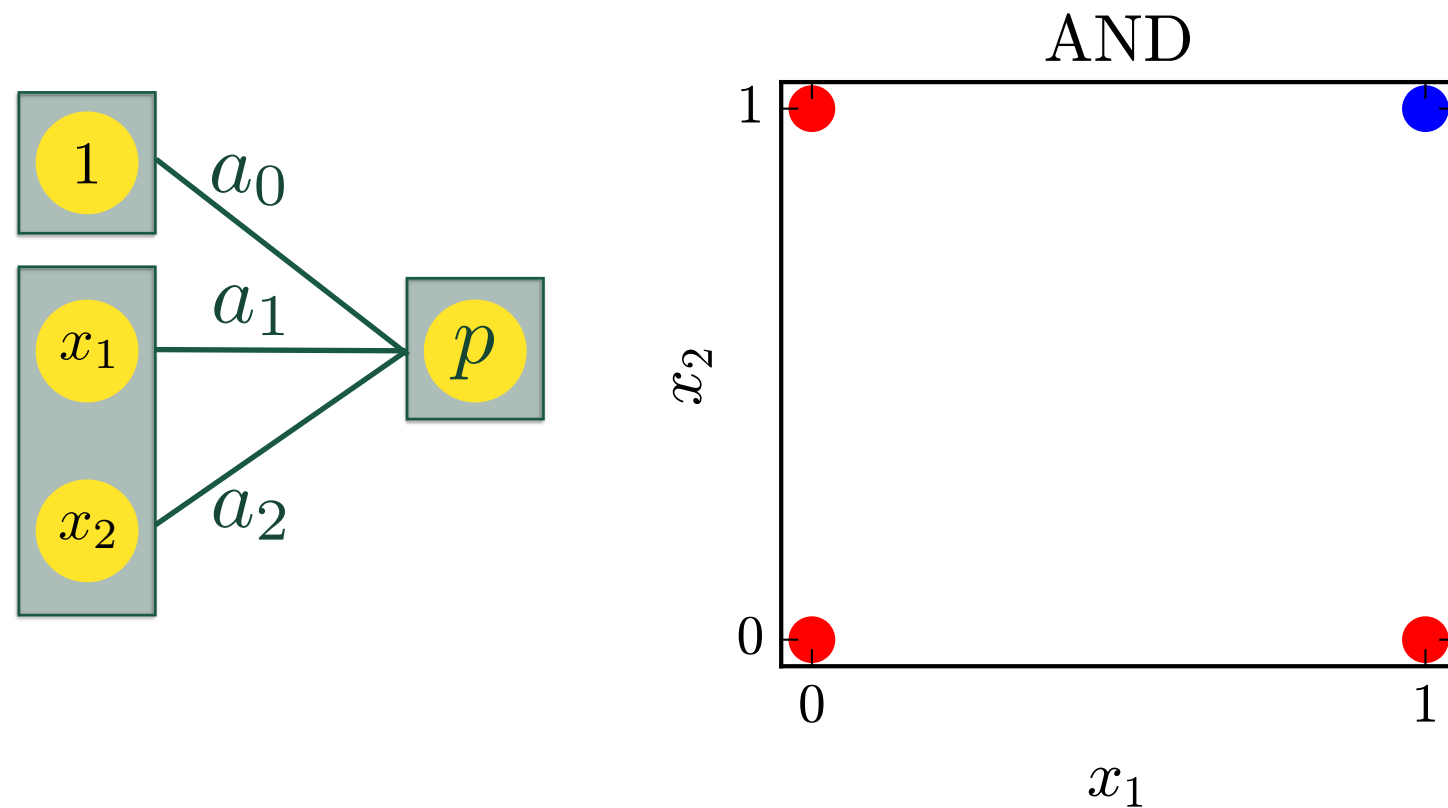


OR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	1

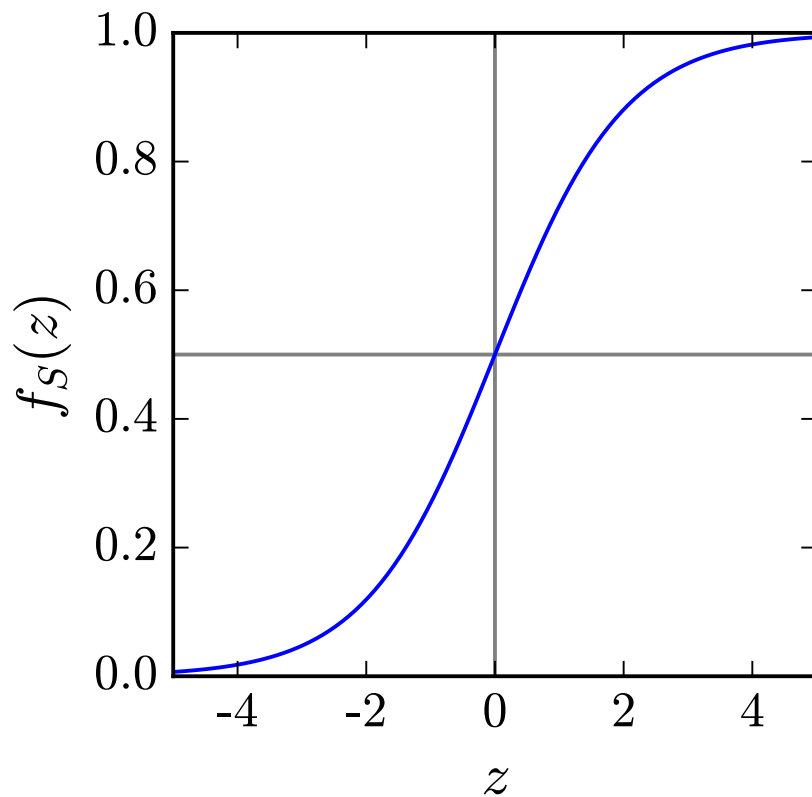


$$a_0 = -10, \quad a_1 = 15, \quad a_2 = 15$$

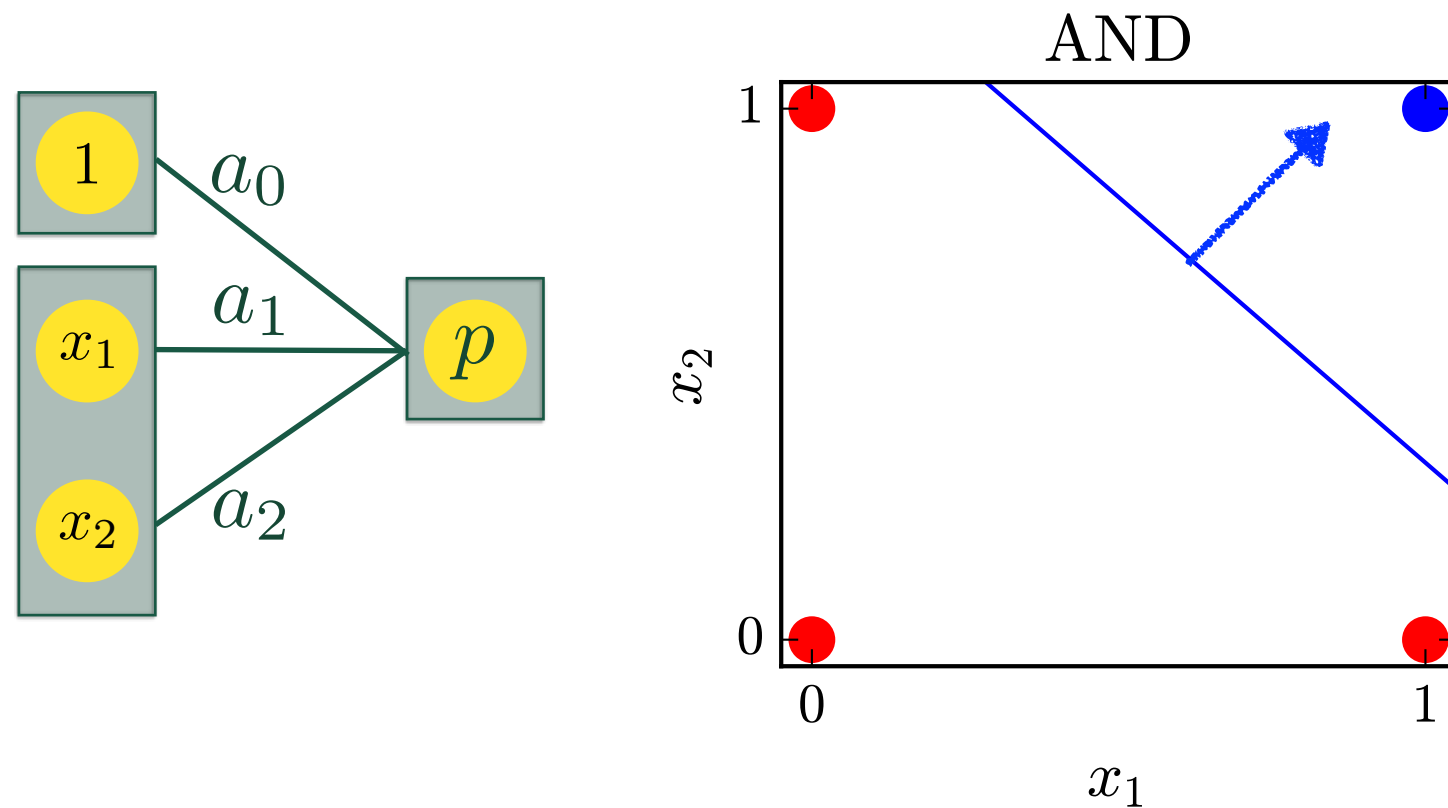
# Neural Networks



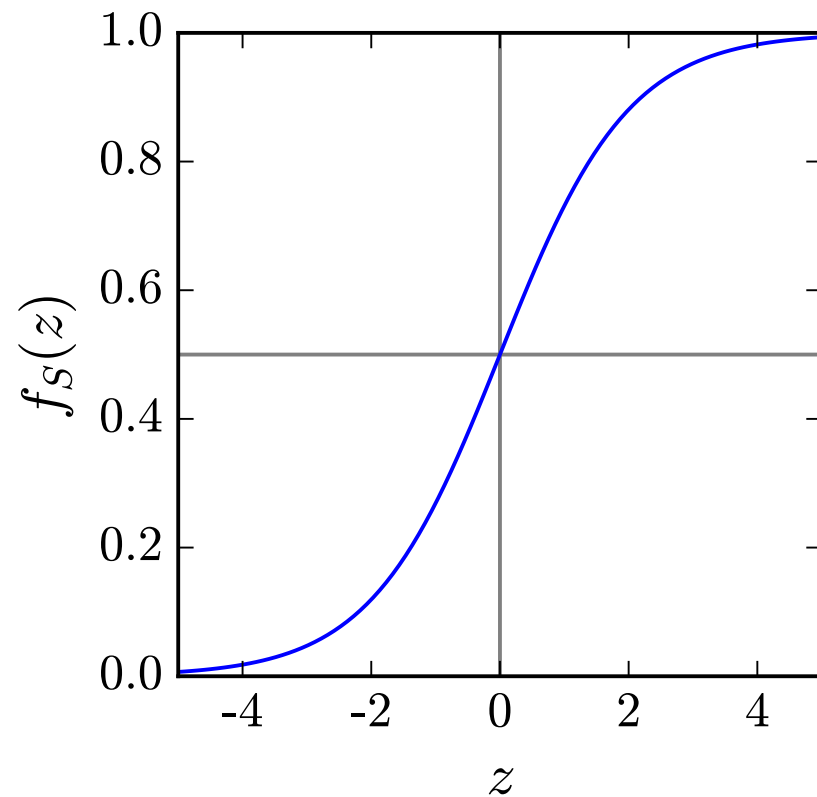
AND		
$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	0
1	1	1



# Neural Networks



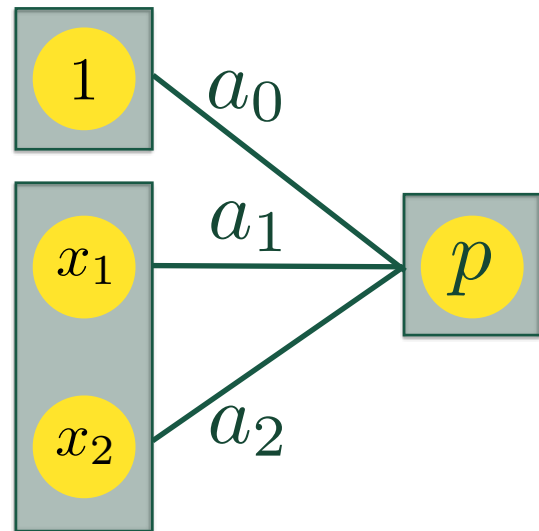
AND		
$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	0
1	1	1



$$a_0 = -20, \quad a_1 = 15, \quad a_2 = 15$$



# Neural Networks



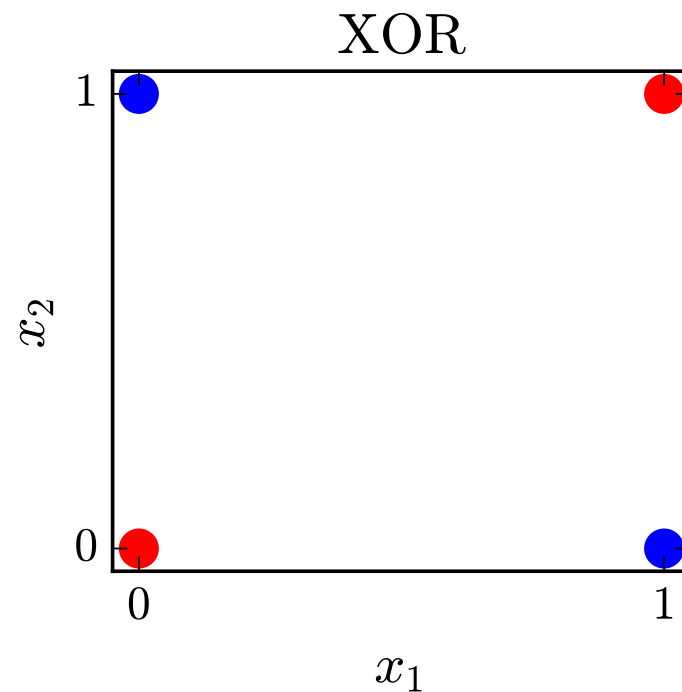
OR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	1

AND		
$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	0
1	1	1

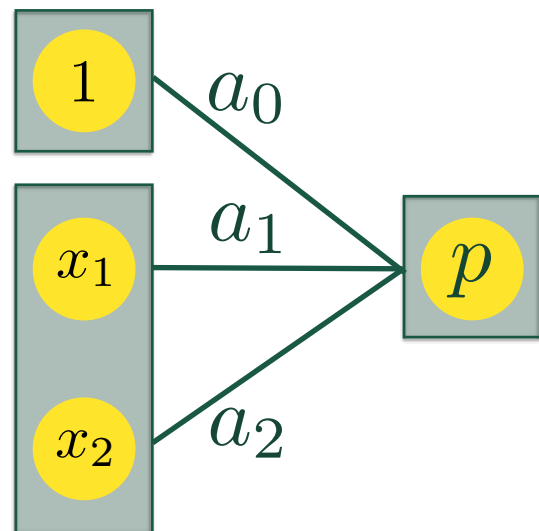
$$a_0 = -10, \quad a_1 = 15, \quad a_2 = 15$$

$$a_0 = -20, \quad a_1 = 15, \quad a_2 = 15$$

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



# Neural Networks



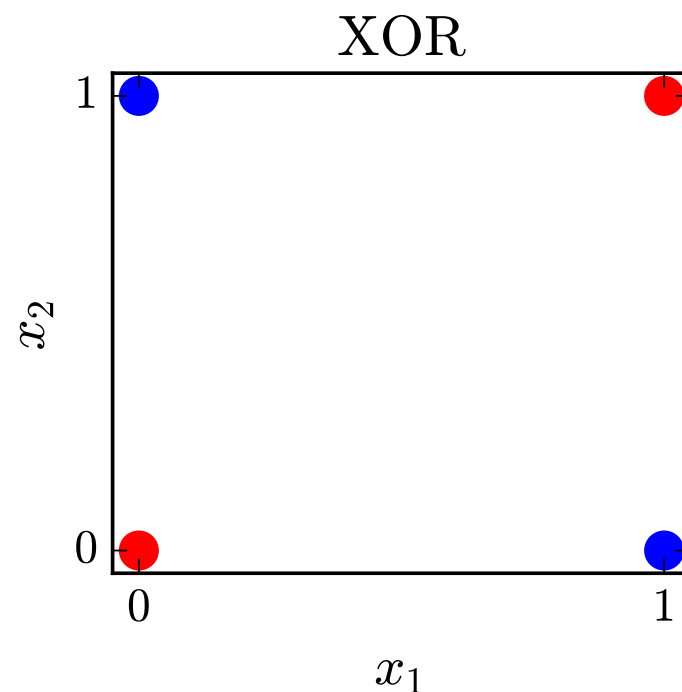
OR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	1

AND		
$x_1$	$x_2$	$y$
0	0	0
0	1	0
1	0	0
1	1	1

$$a_0 = -10, \quad a_1 = 15, \quad a_2 = 15$$

$$a_0 = -20, \quad a_1 = 15, \quad a_2 = 15$$

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0

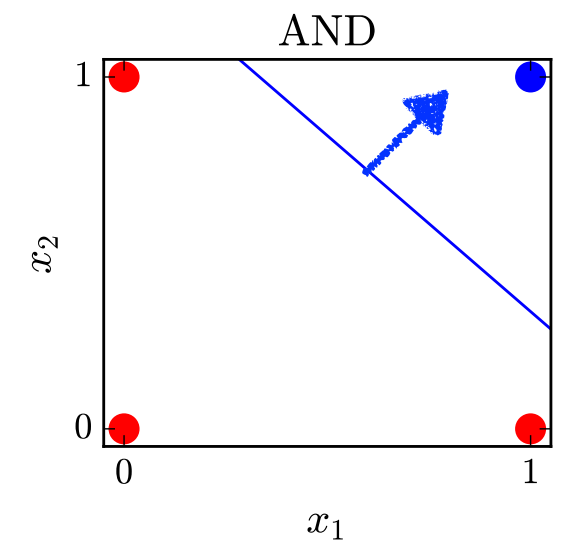
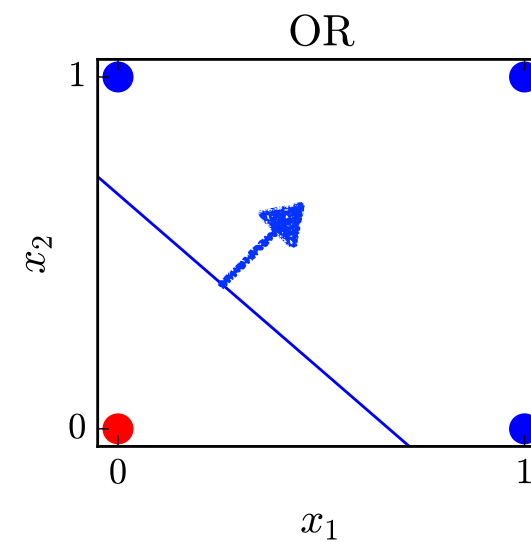
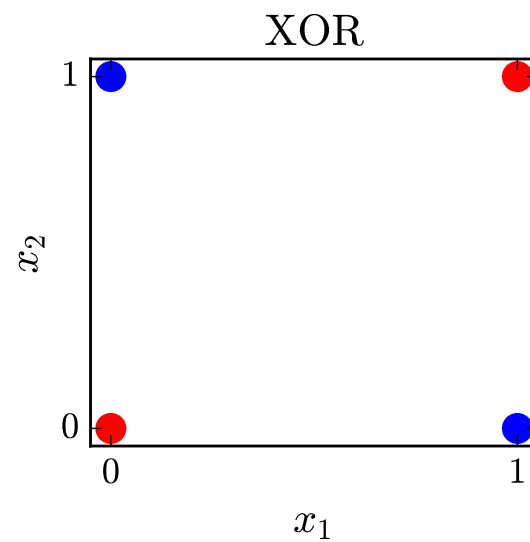


This system cannot  
produce XOR

(cannot make a two sided cut)

# Neural Networks

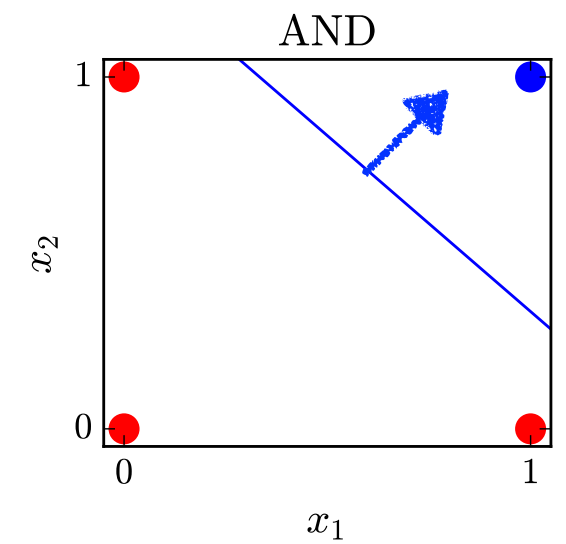
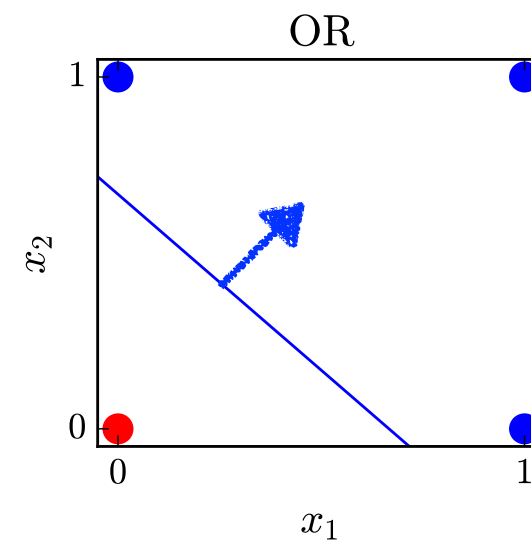
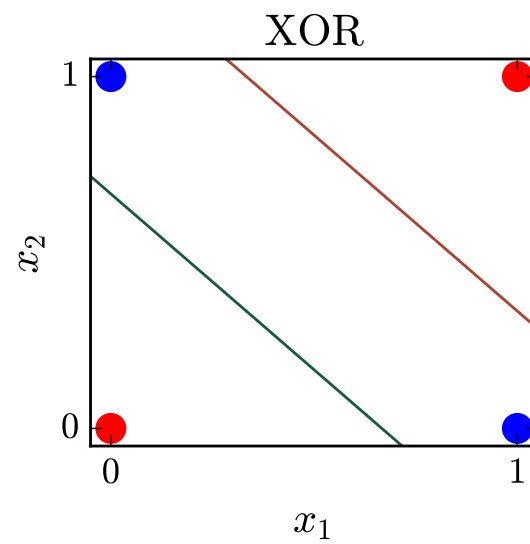
XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0





# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



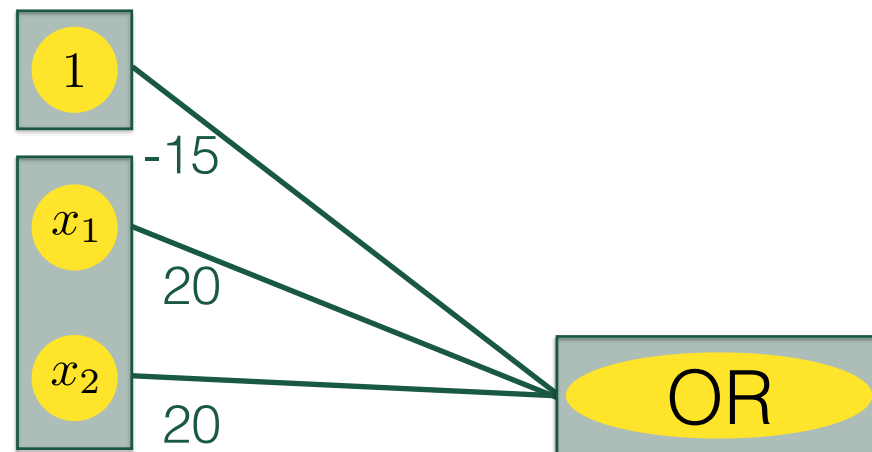
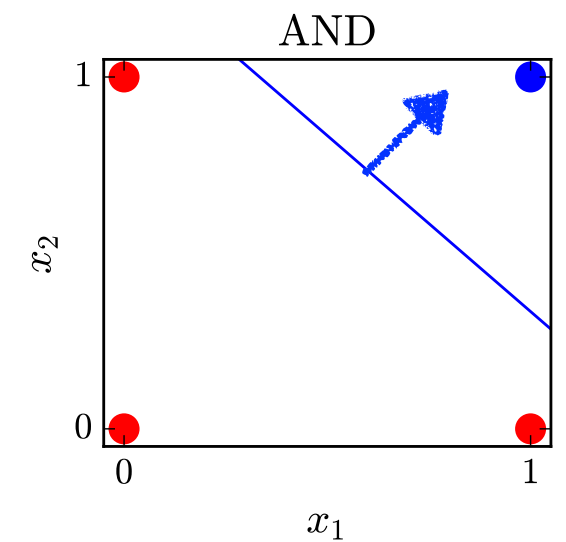
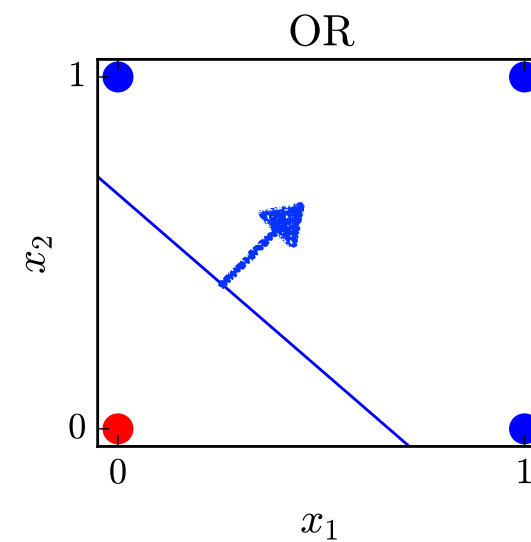
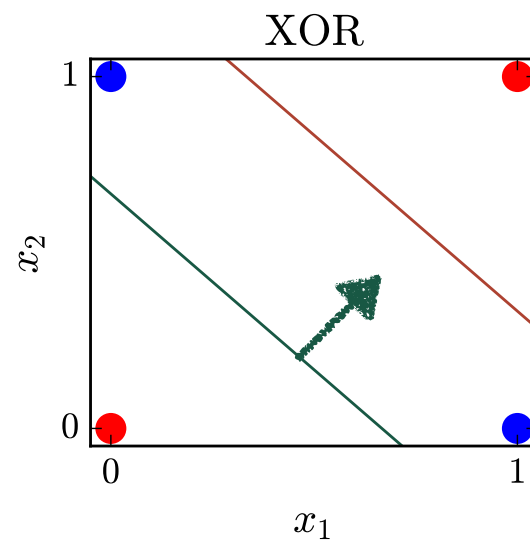
1

$x_1$

$x_2$

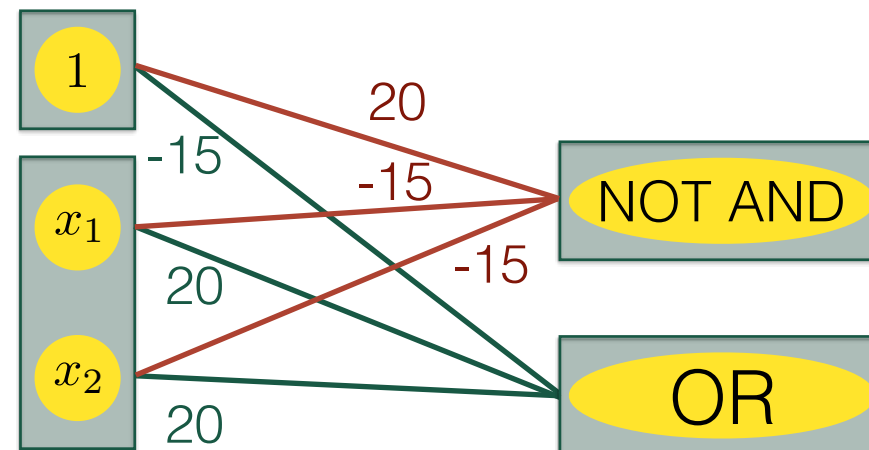
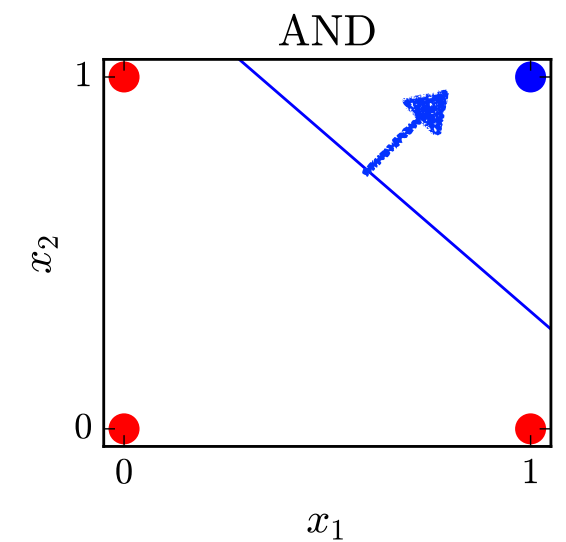
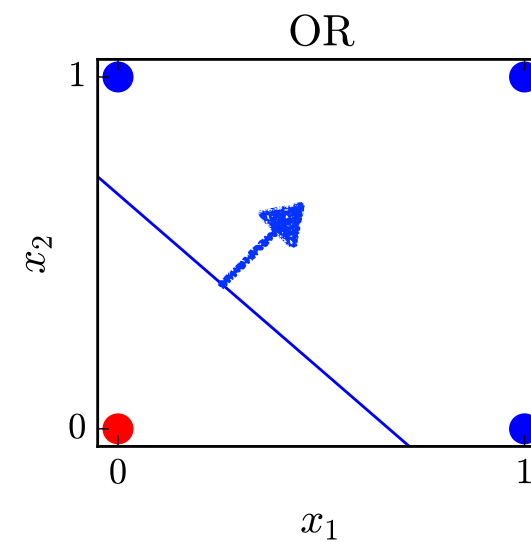
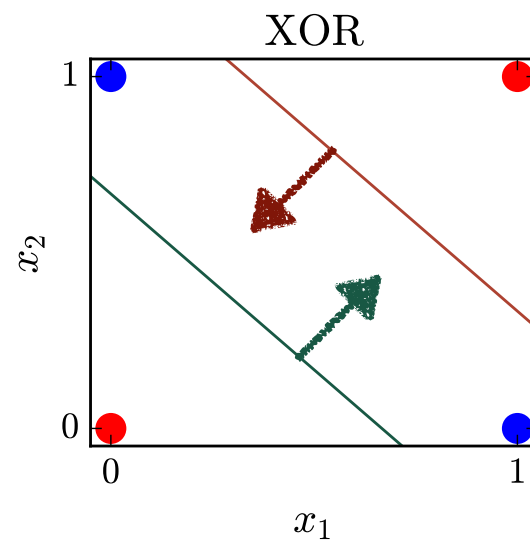
# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



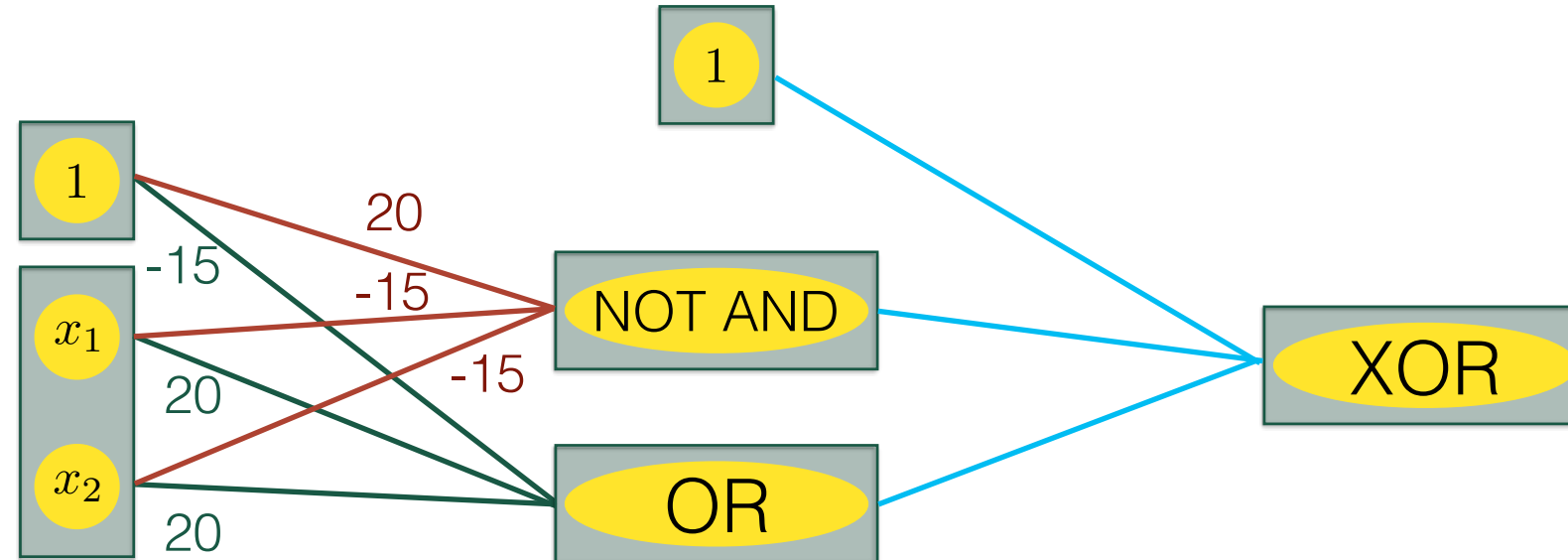
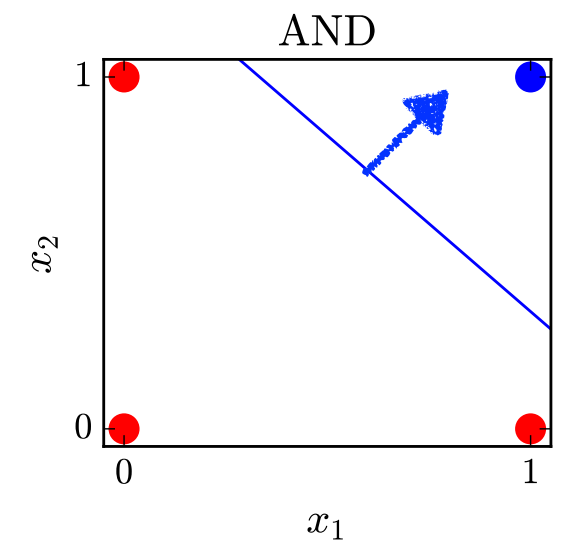
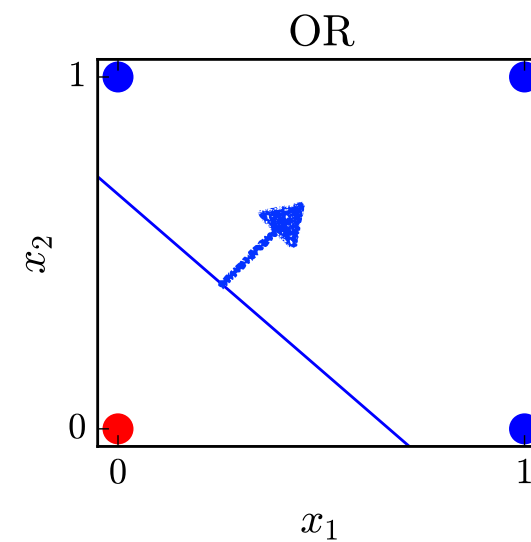
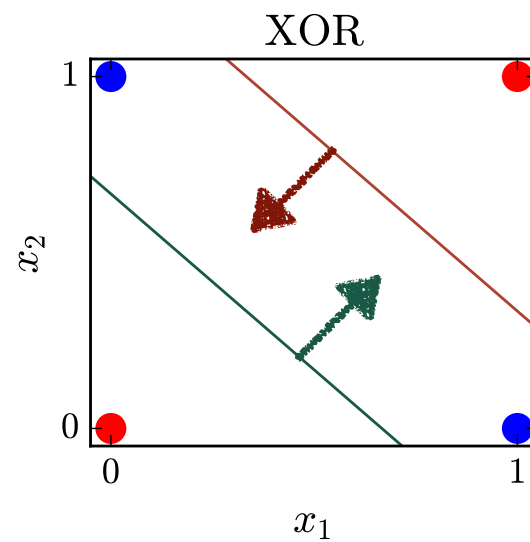
# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



# Neural Networks

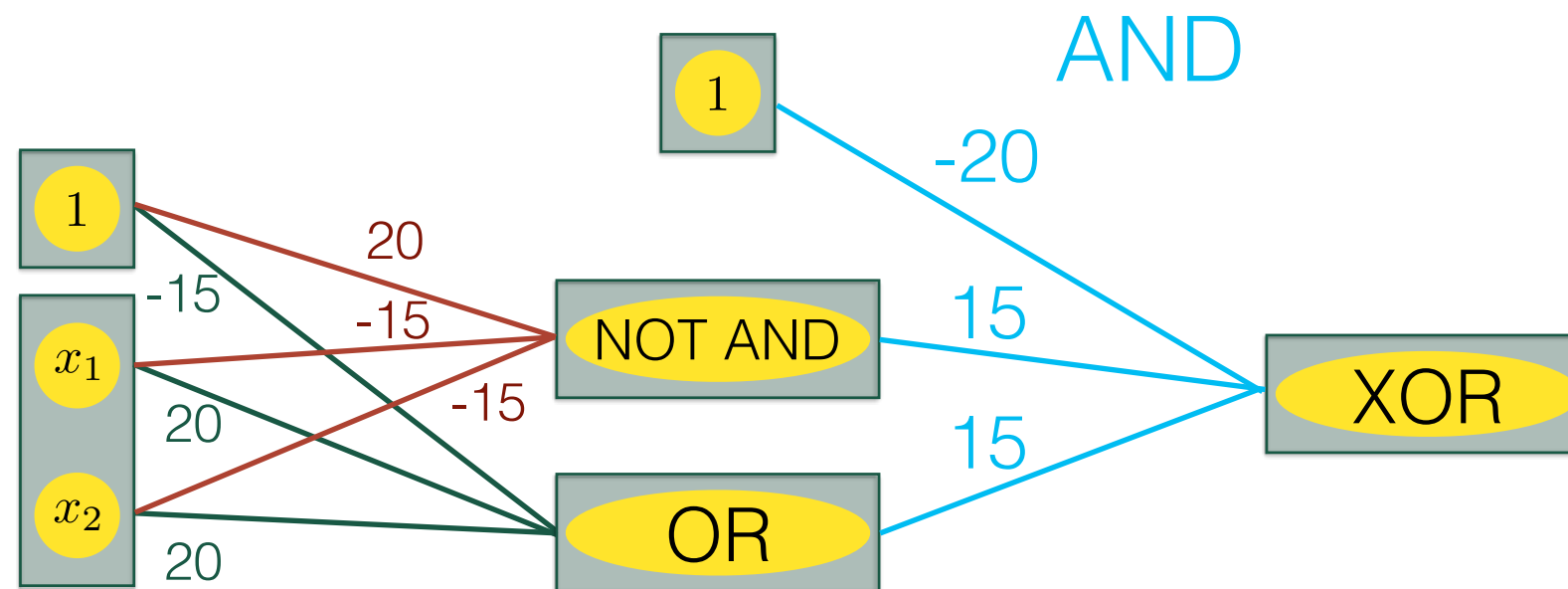
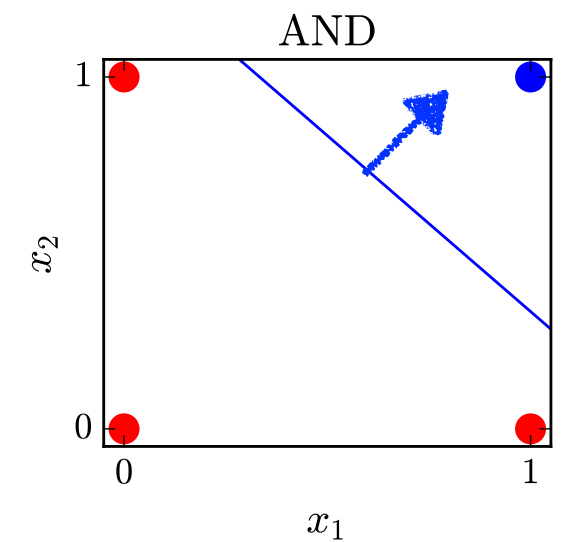
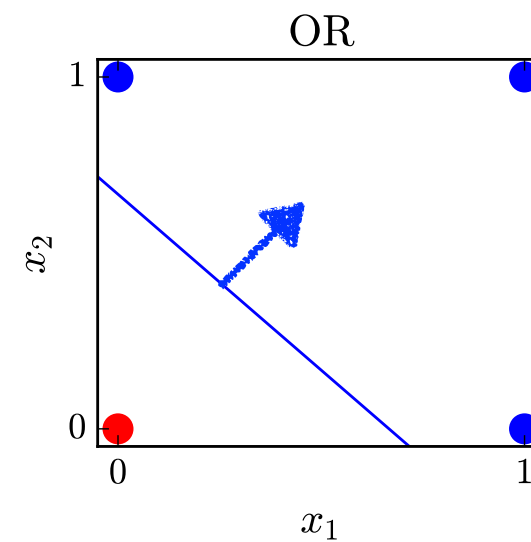
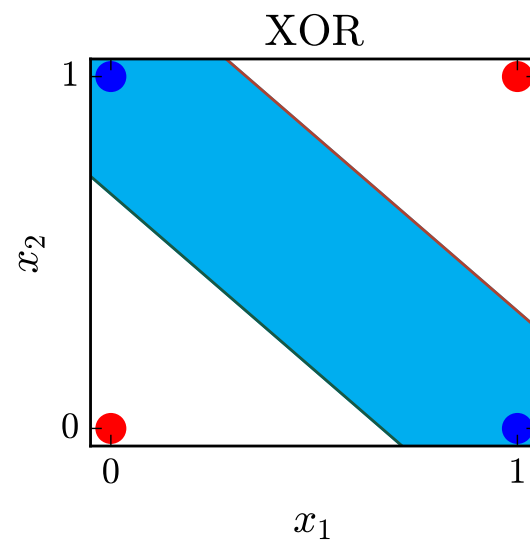
XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0





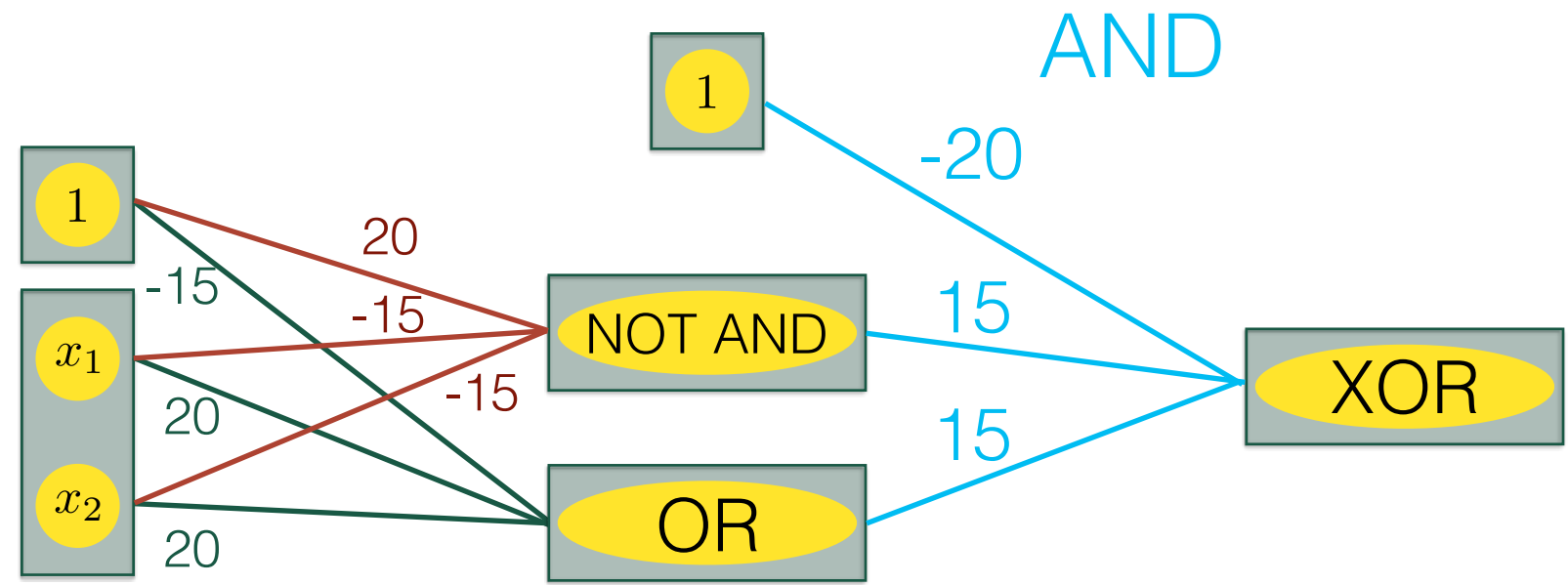
# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0



# Neural Networks

XOR		
$x_1$	$x_2$	$y$
0	0	0
0	1	1
1	0	1
1	1	0

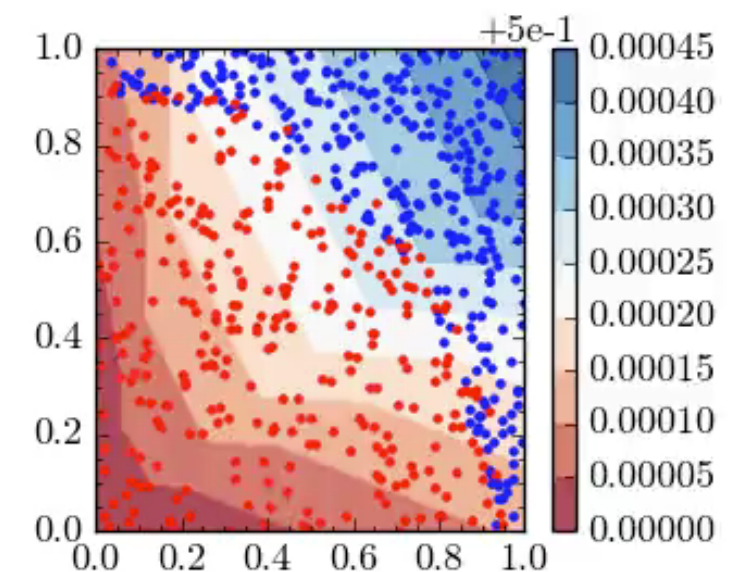
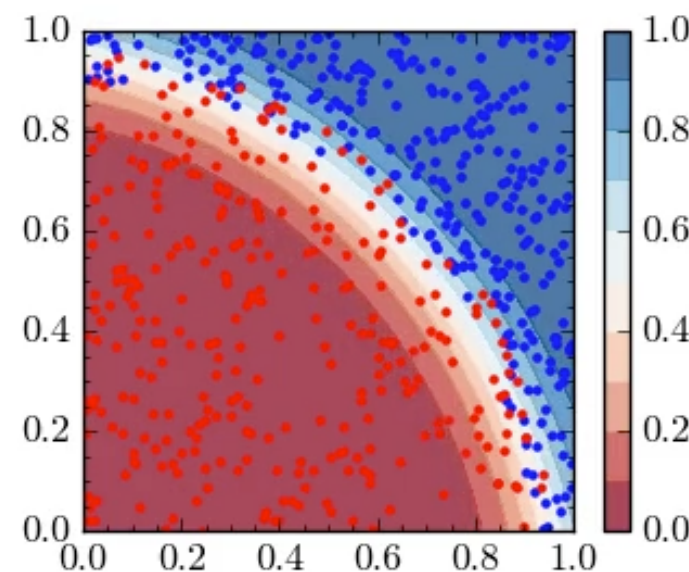
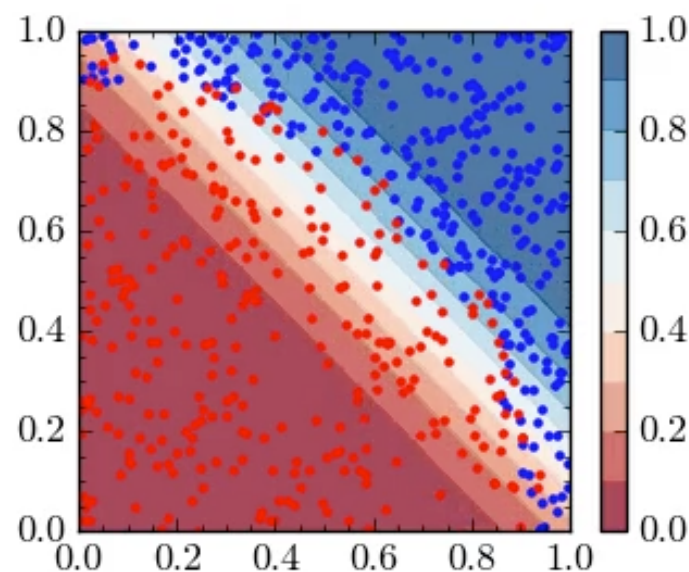
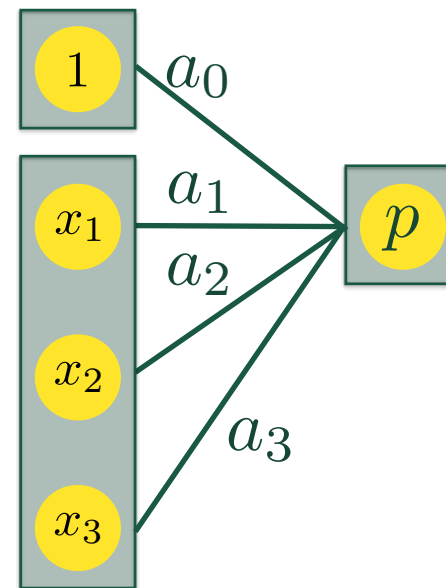


Simple example showing that neural network can access 'high-level' functions

To learn weights, need large training set and CPU time

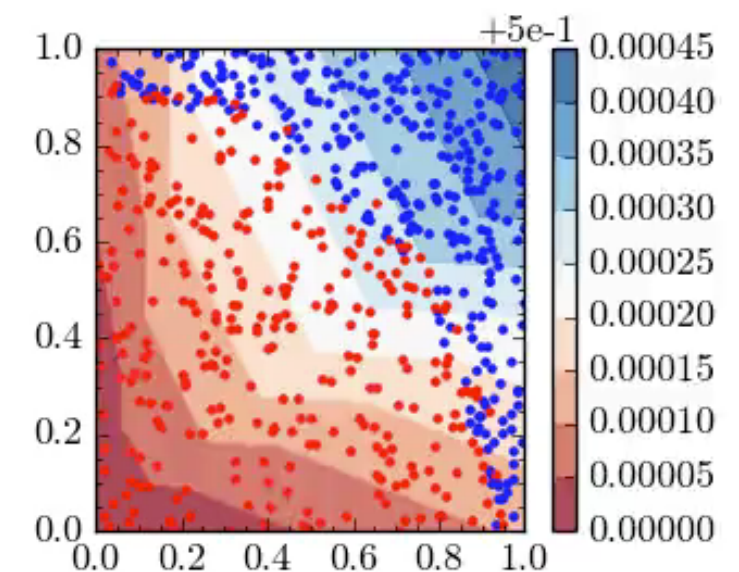
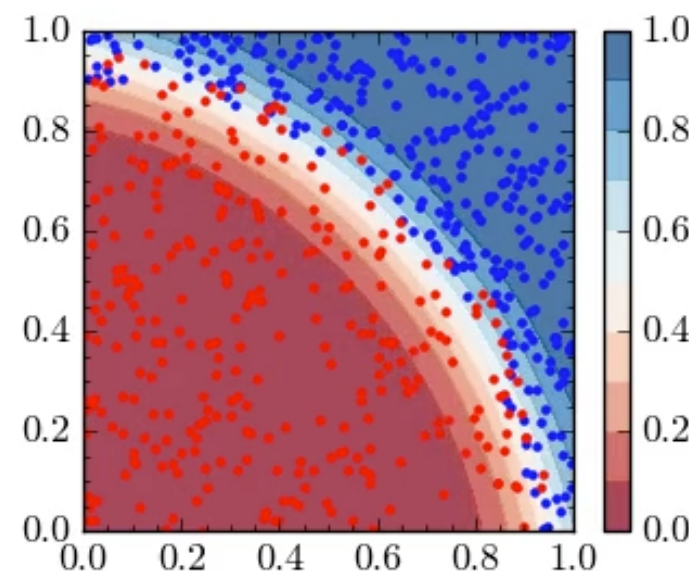
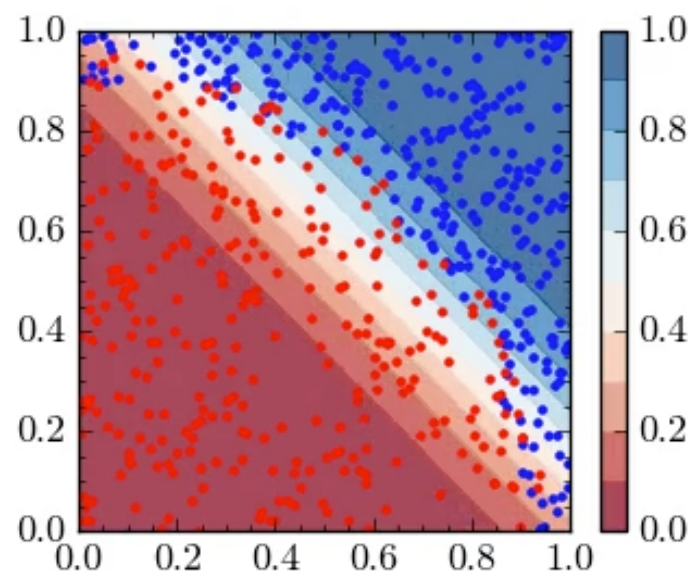
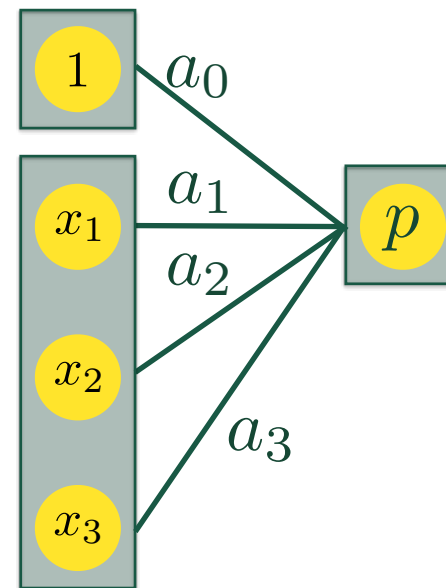
# Neural Networks

- Don't add more inputs, let machine find own shape
- Ability to learn 'any' function
- More nodes/hidden layers allows for more complex features



# Neural Networks

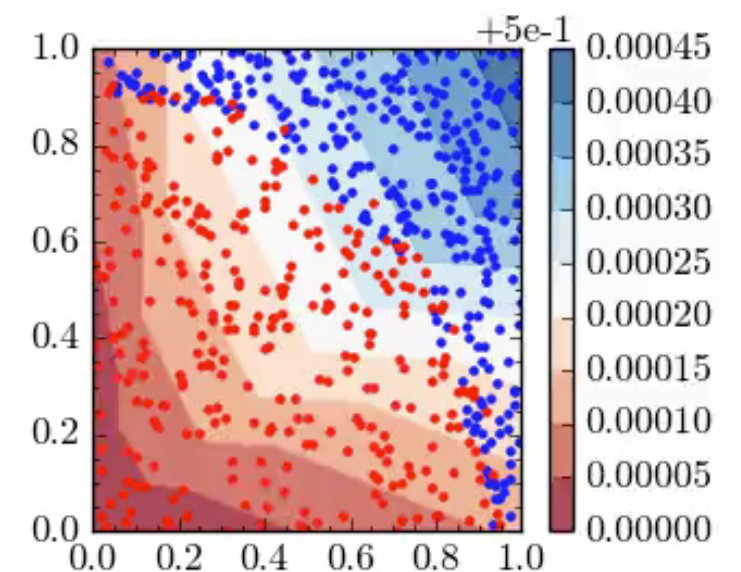
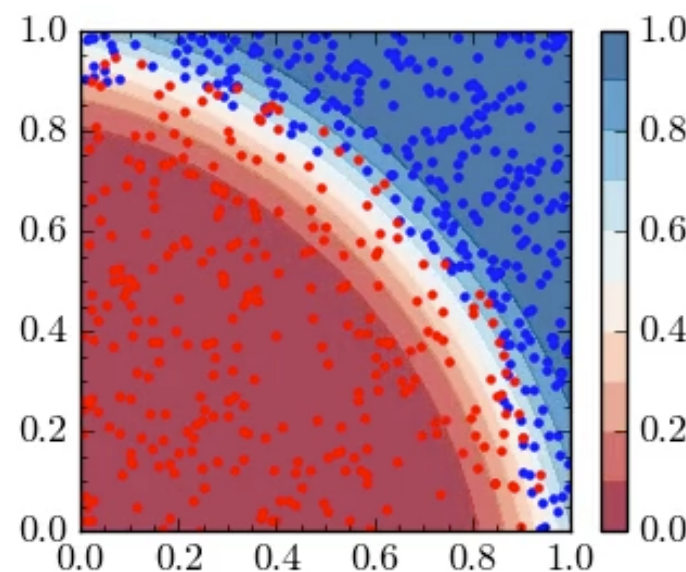
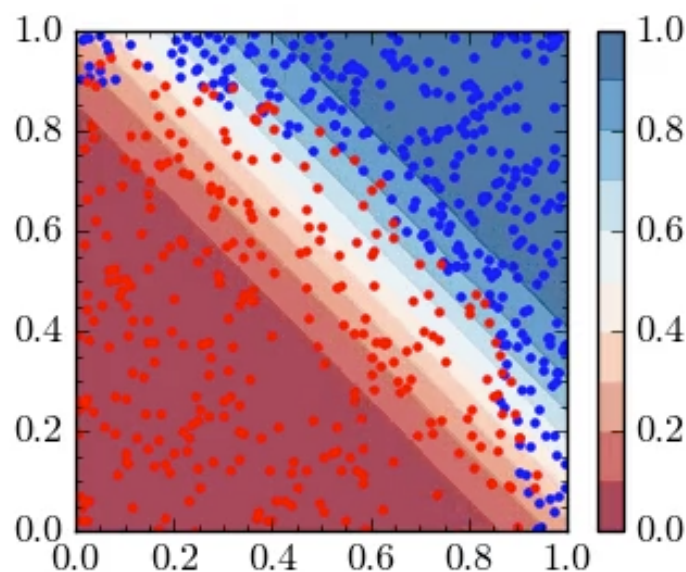
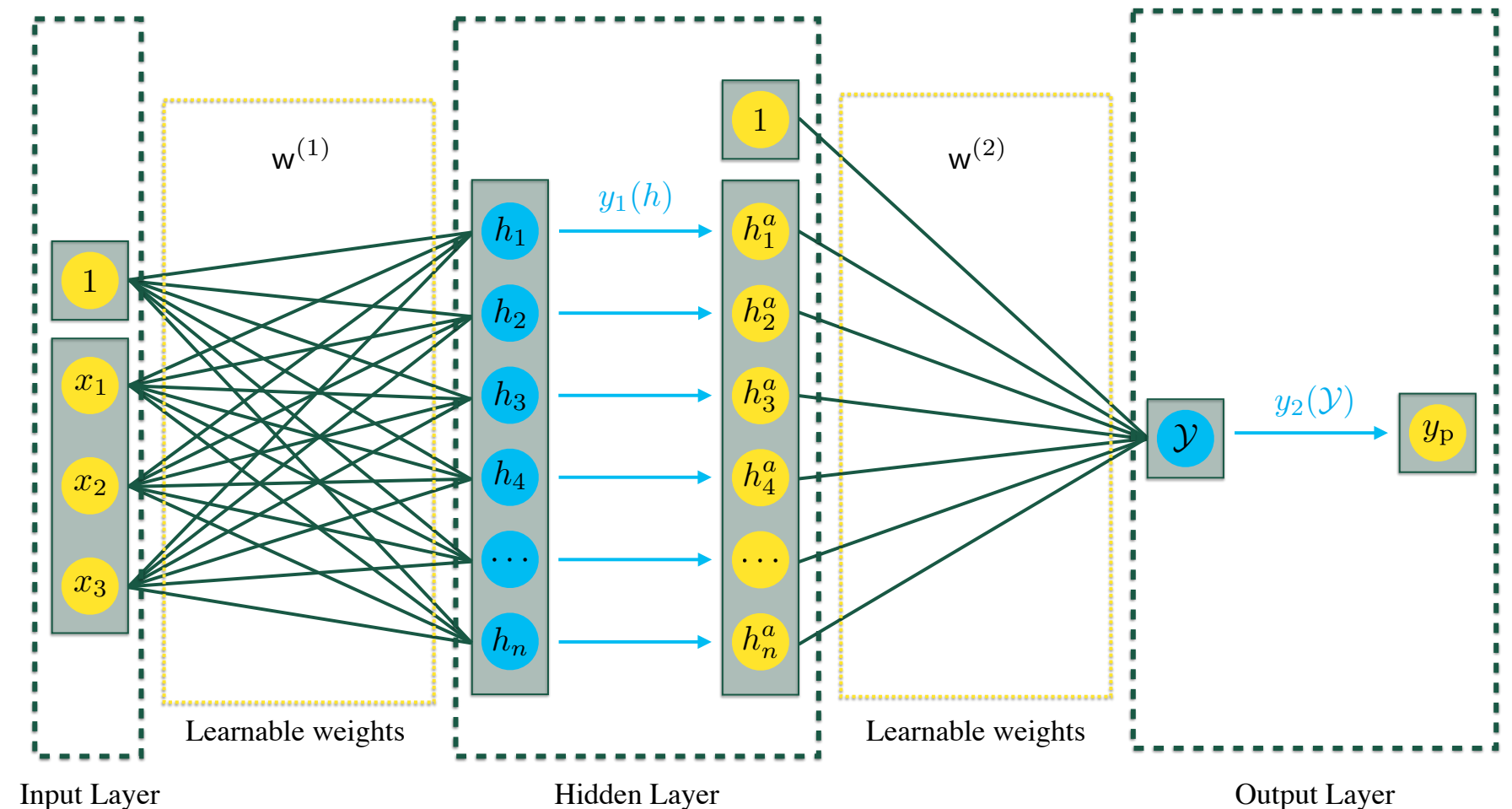
- Don't add more inputs, let machine find own shape
- Ability to learn 'any' function
- More nodes/hidden layers allows for more complex features





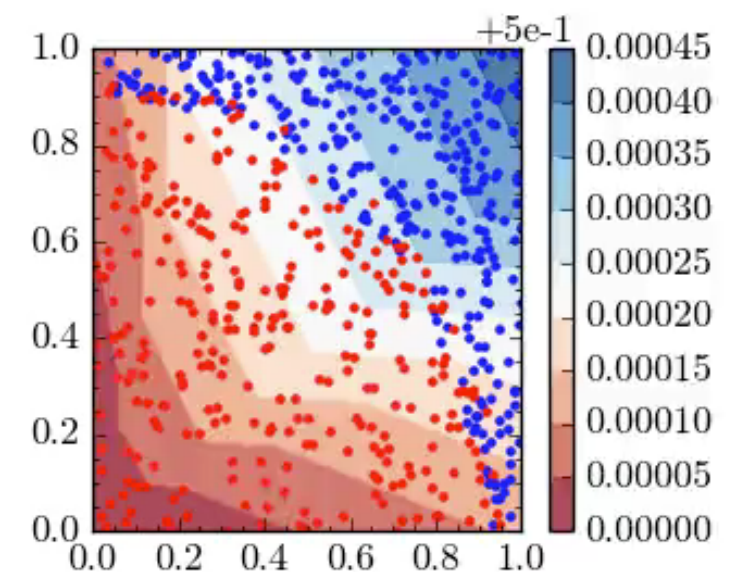
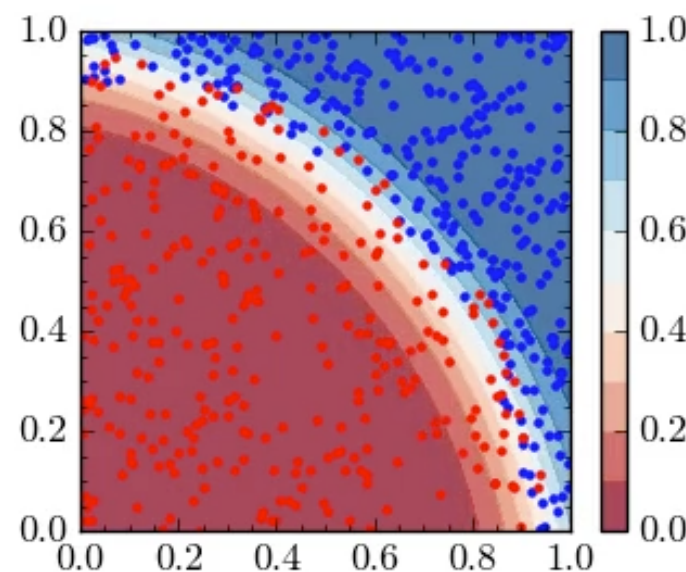
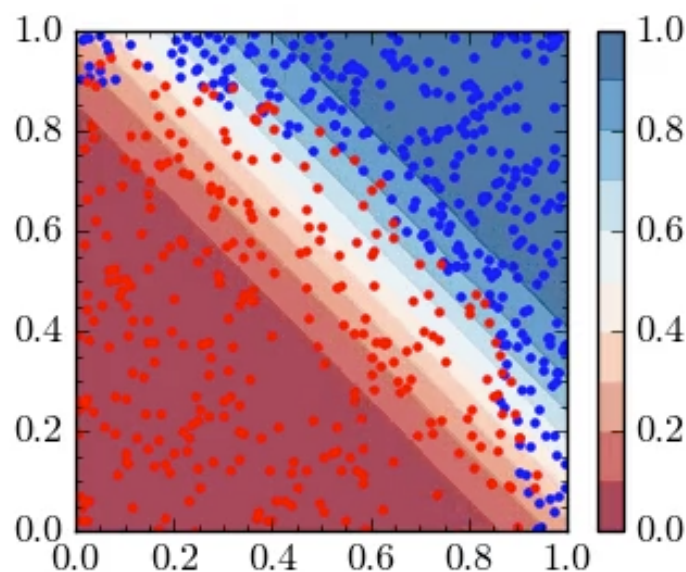
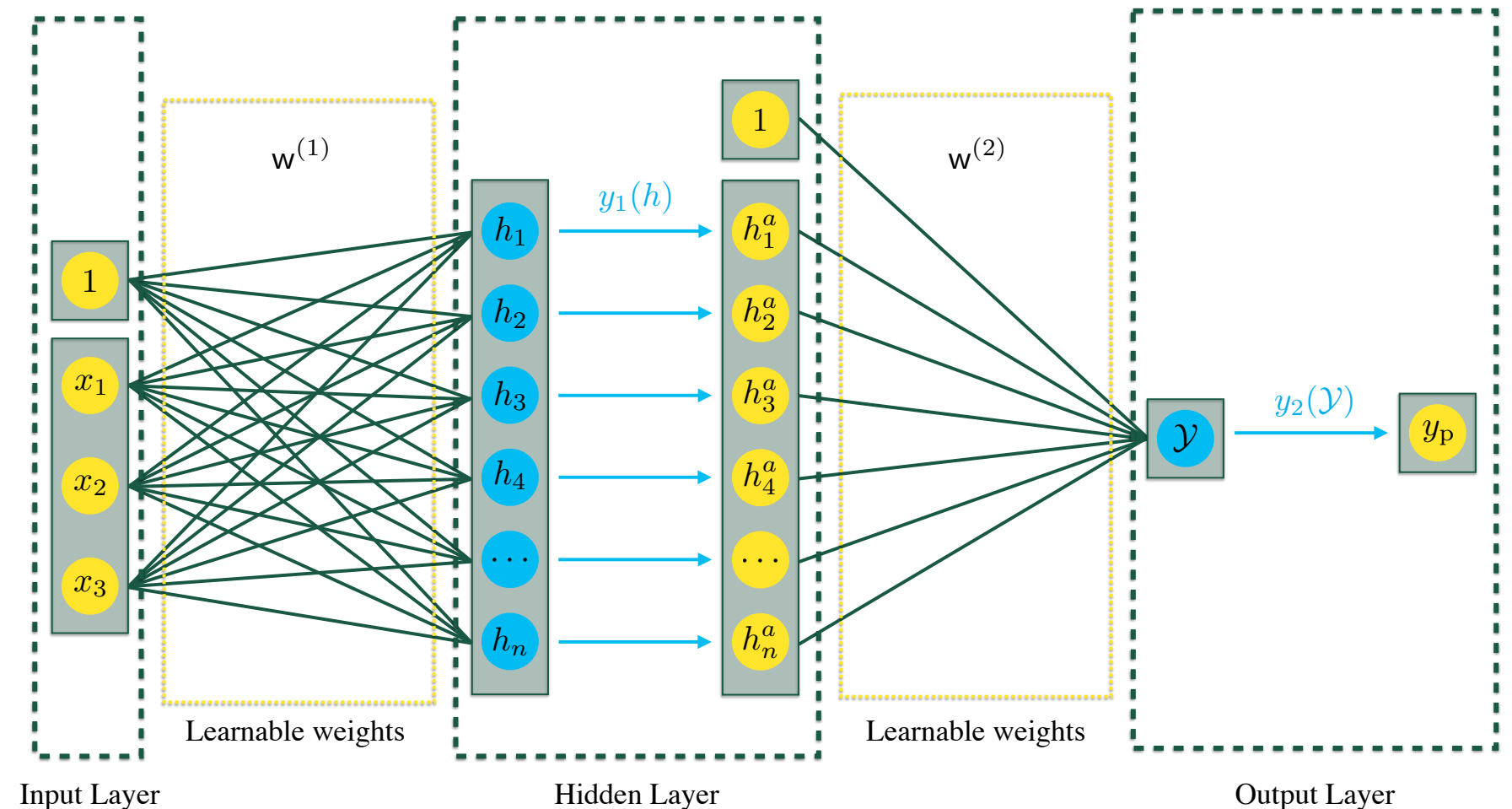
# Neural Networks

- Don't add more inputs, let machine find own shape
- Ability to learn 'any' function
- More nodes/hidden layers allows for more complex features



# Neural Networks

- Don't add more inputs, let machine find own shape
- Ability to learn 'any' function
- More nodes/hidden layers allows for more complex features





# Neural Network Review

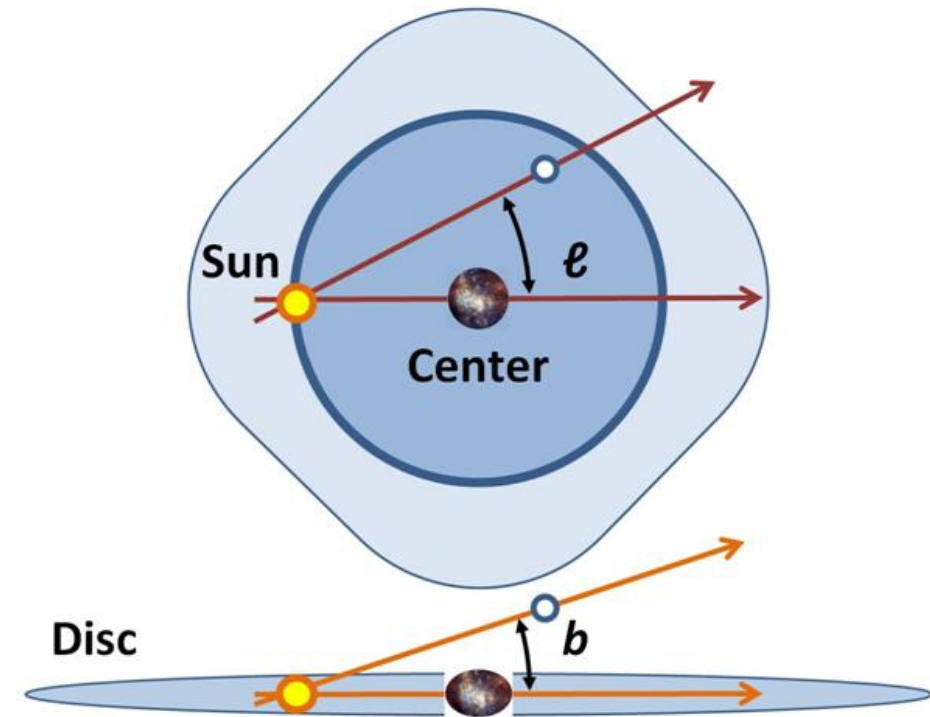
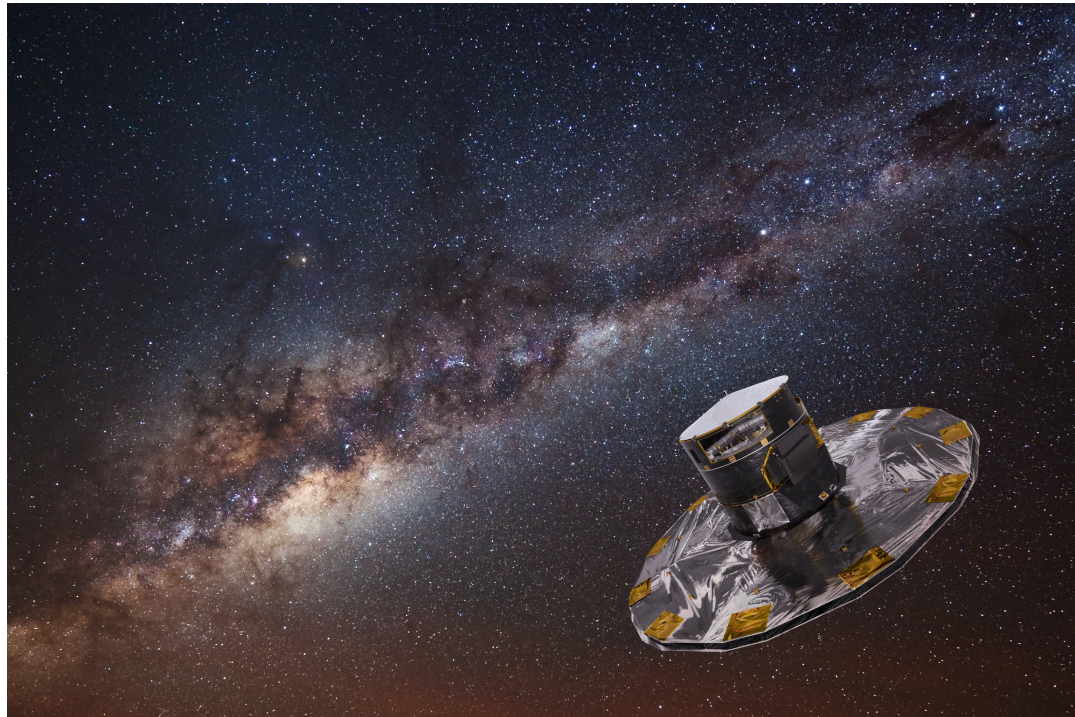
- Neural networks act as universal function fitter
- Deep networks (many hidden layers) allow the network to pick its own features



Is it possible to classify halo stars without spectroscopy?



# Is it possible to classify halo stars using only 5-d information?



Stellar information from Gaia:

- Galactic longitude ( $l$ )
- Galactic latitude ( $b$ )
- Proper motion (ascension)
- Proper motion (declination)
- Parallax (distance =  $1 / \text{parallax}$ )

rate of change of these,  
transferred to different  
coordinate system



Is it possible to classify halo stars using only 5-d information?

How to train the network if we don't know labels for the stars?

### **Sampling**

- Draw stars from model distributions
- Defined labels
- Fast data generation

### **Simulation**

- Distributions from interaction
- Labels from merger history
- Can't generate ourselves

# Learning the halo

## Sampling

THE ASTROPHYSICAL JOURNAL, 730:3 (20pp), 2011 March 20  
© 2011. The American Astronomical Society. All rights reserved. Printed in the U.S.A.

doi:[10.1088/0004-637X/730/1/3](https://doi.org/10.1088/0004-637X/730/1/3)

### GALAXIA: A CODE TO GENERATE A SYNTHETIC SURVEY OF THE MILKY WAY

SANJIB SHARMA<sup>1</sup>, JOSS BLAND-HAWTHORN<sup>1,4</sup>, KATHRYN V. JOHNSTON<sup>2</sup>, AND JAMES BINNEY<sup>3</sup>

<sup>1</sup> Sydney Institute for Astronomy, School of Physics, University of Sydney, NSW 2006, Australia

<sup>2</sup> Department of Astronomy, Columbia University, New York, NY 10027, USA

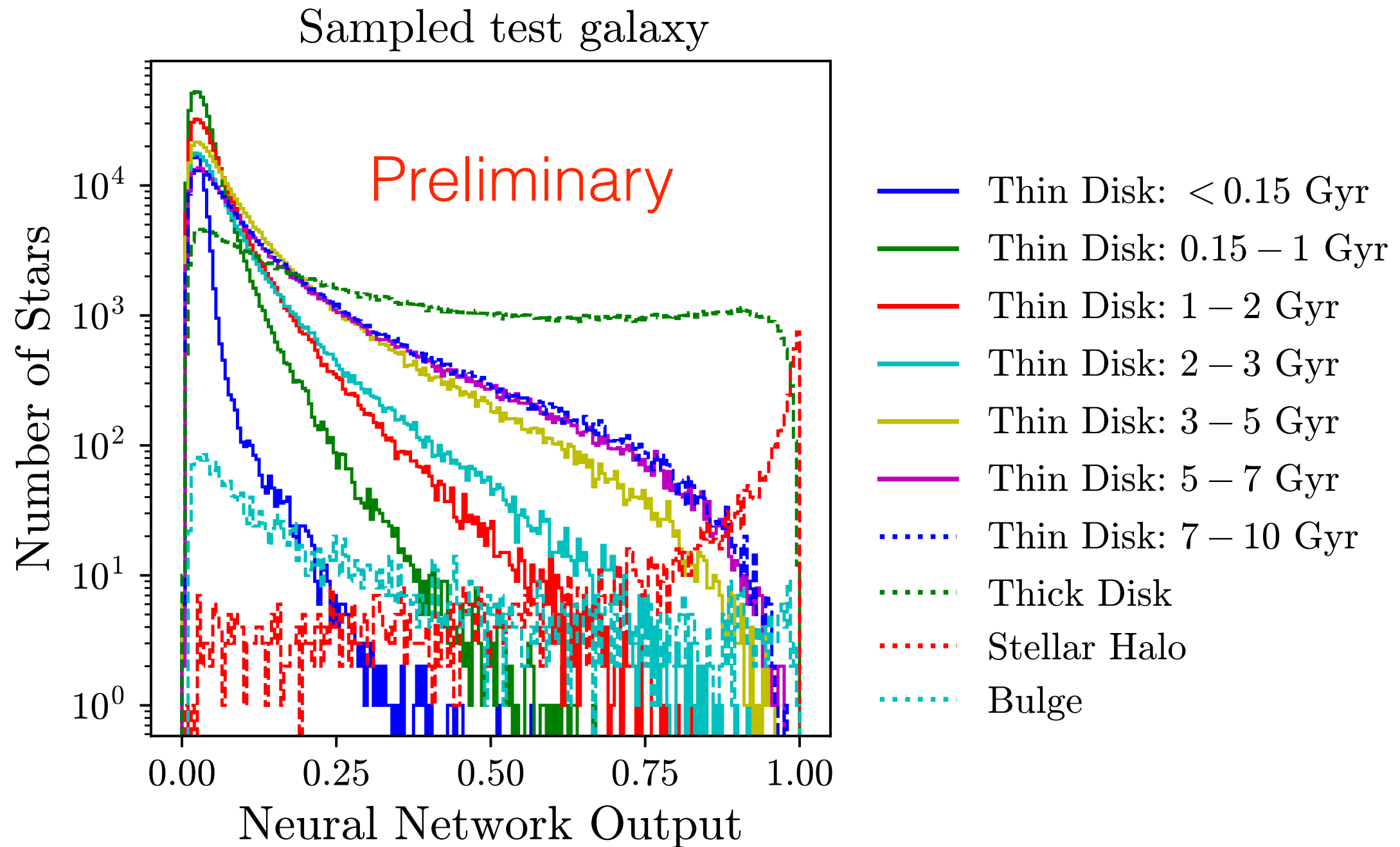
<sup>3</sup> Rudolf Peierls Centre for Theoretical Physics, 1 Keble Rd, Oxford OX1 3NP, UK

*Received 2010 September 16; accepted 2011 January 12; published 2011 February 23*

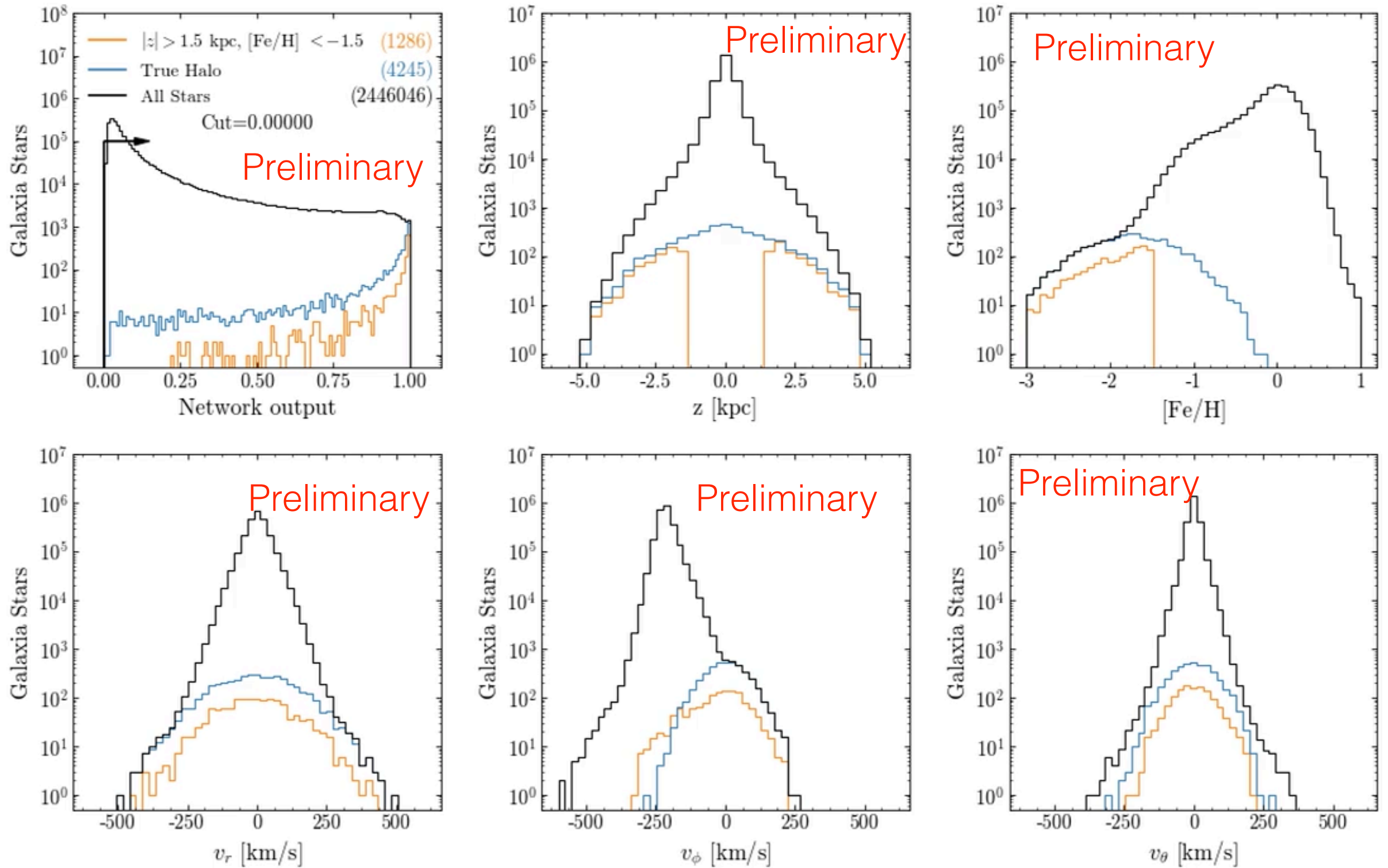
#### ABSTRACT

We present here a fast code for creating a synthetic survey of the Milky Way. Given one or more color–magnitude bounds, a survey size, and geometry, the code returns a catalog of stars in accordance with a given model of the Milky Way. The model can be specified by a set of density distributions or as an  $N$ -body realization. We provide fast and efficient algorithms for sampling both types of models. As compared to earlier sampling schemes which generate stars at specified locations along a line of sight, **our scheme can generate a continuous and smooth distribution of stars over any given volume.** The code is quite general and flexible and can accept input in the form of a star formation rate, age–metallicity relation, age–velocity–dispersion relation, and analytic density distribution functions. Theoretical isochrones are then used to generate a catalog of stars, and support is available for a wide range of photometric bands. As a concrete example, we implement the Besançon Milky Way model for the disk. For the stellar halo we employ the simulated stellar halo  $N$ -body models of Bullock & Johnston. In order to sample  $N$ -body models, we present a scheme that disperses the stars spawned by an  $N$ -body particle, in such a way that the phase-space density of the spawned stars is consistent with that of the  $N$ -body particles. **The code is ideally suited to generating synthetic data sets that mimic near future wide area surveys such as GAIA, LSST, and HERMES.** As an application we study the prospect of identifying structures in the stellar halo with a simulated GAIA survey. We plan to make the code publicly available.

# Learning the halo

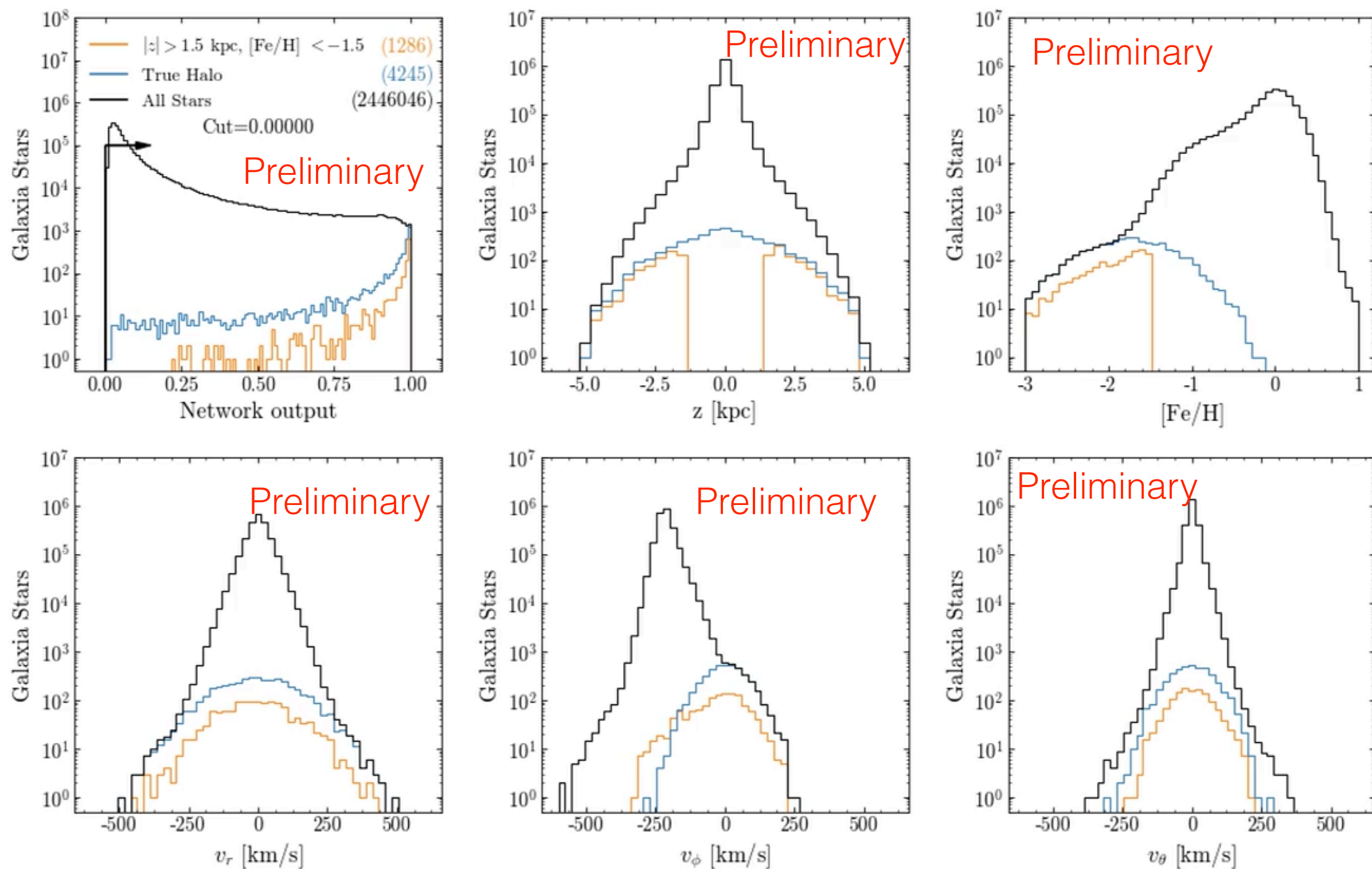


# Learning the halo

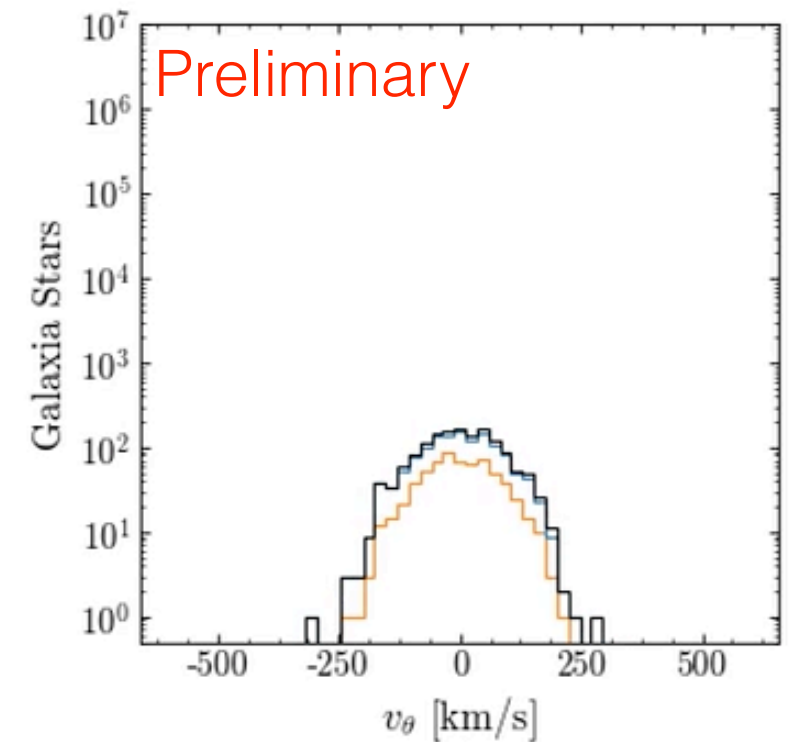
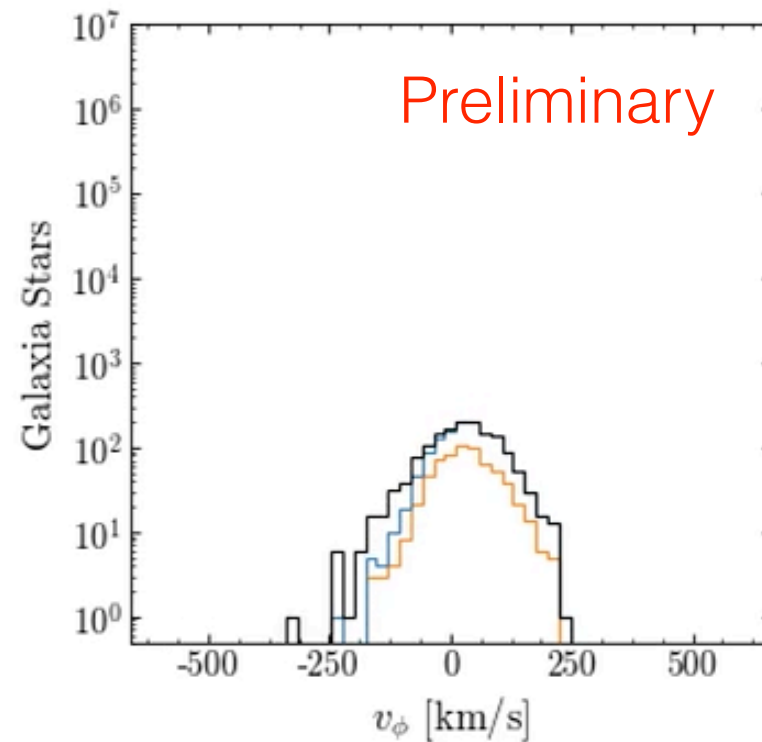
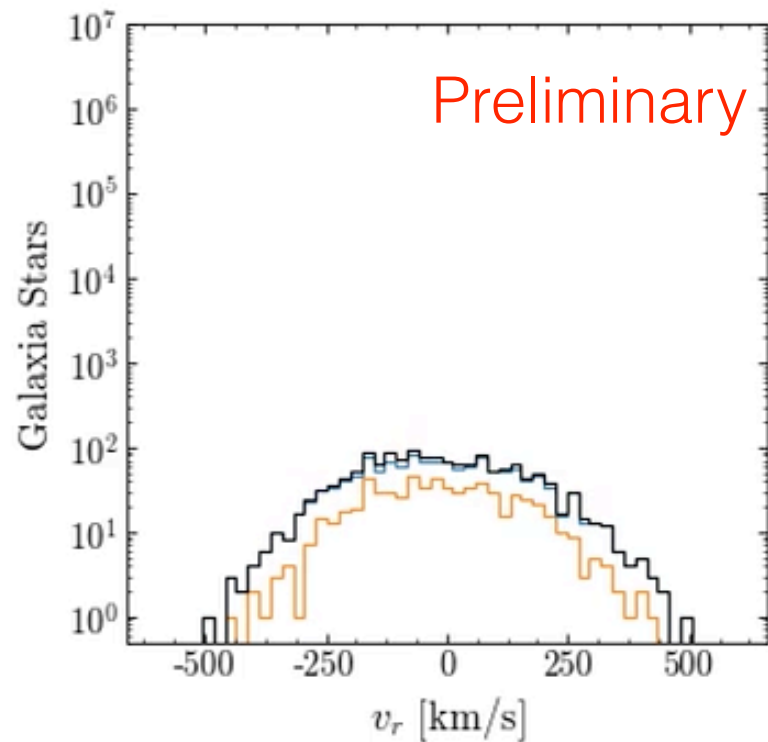
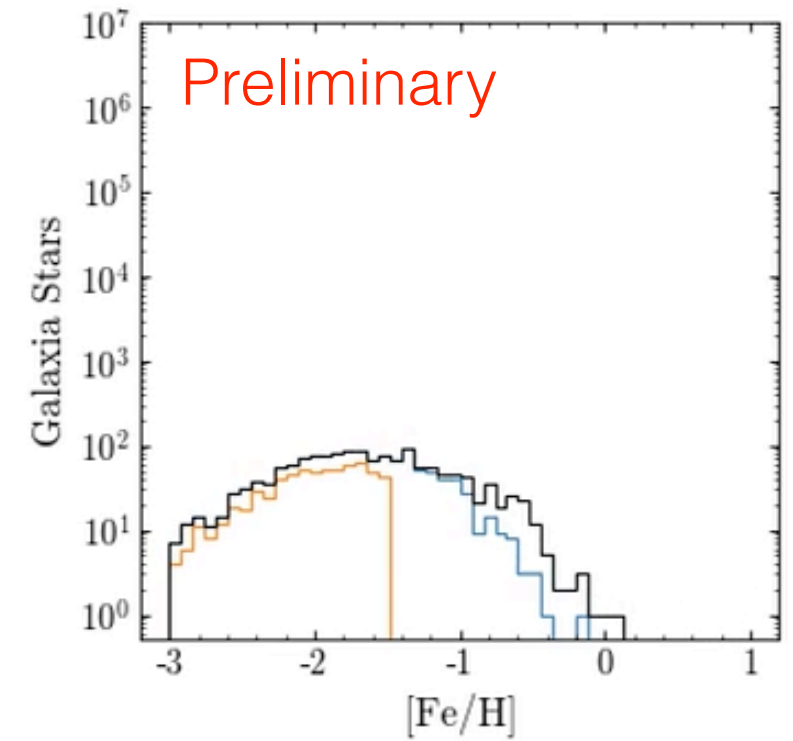
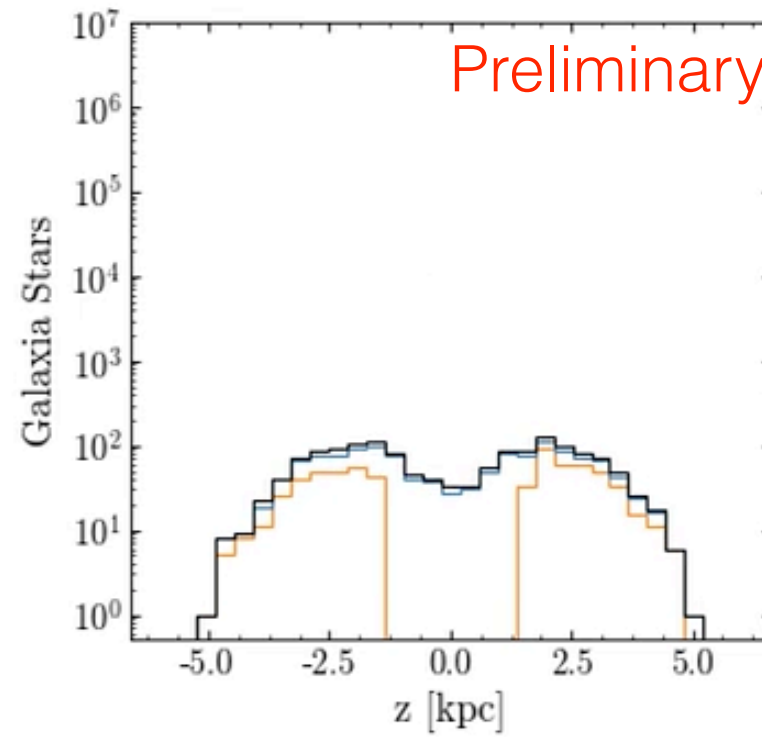
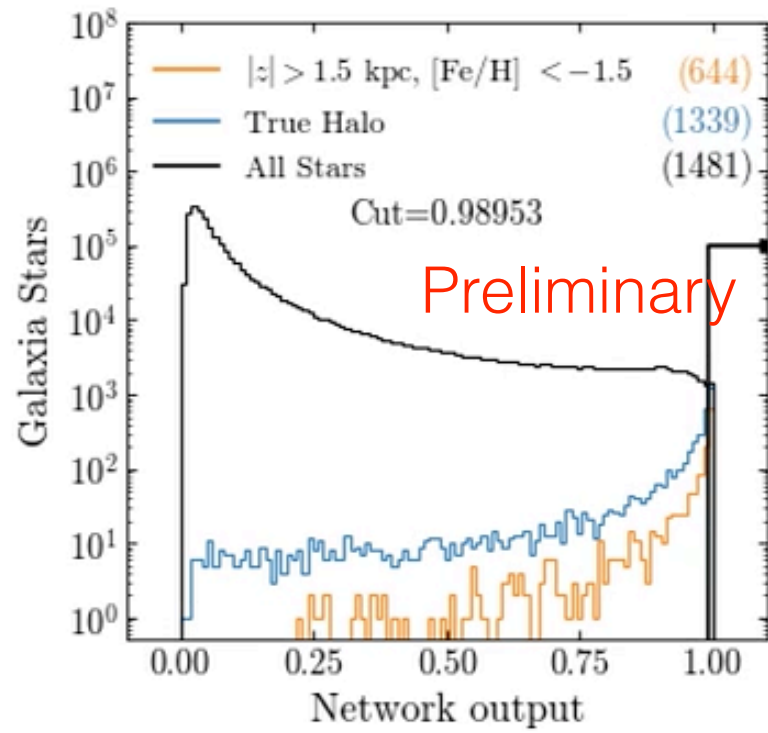




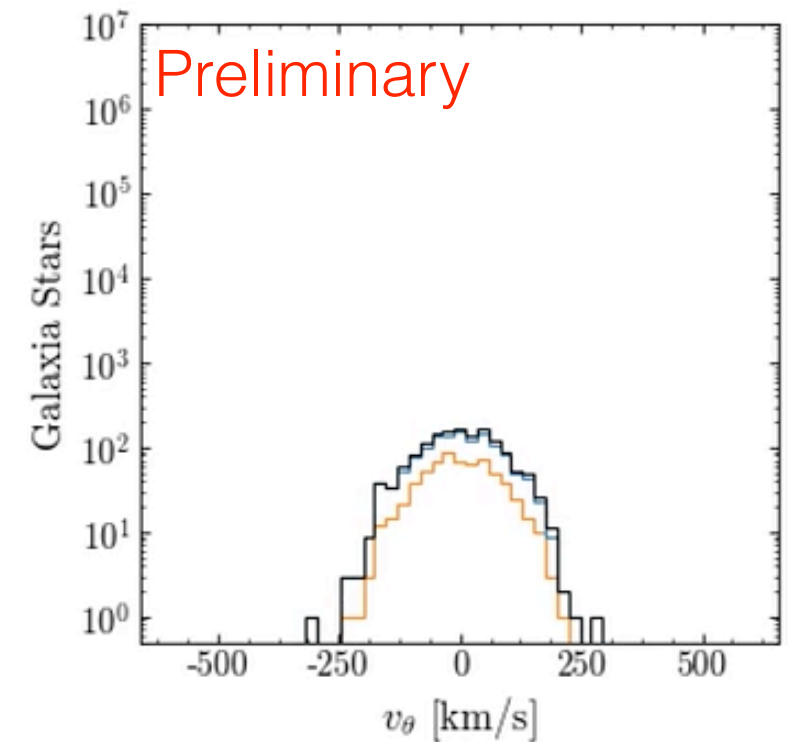
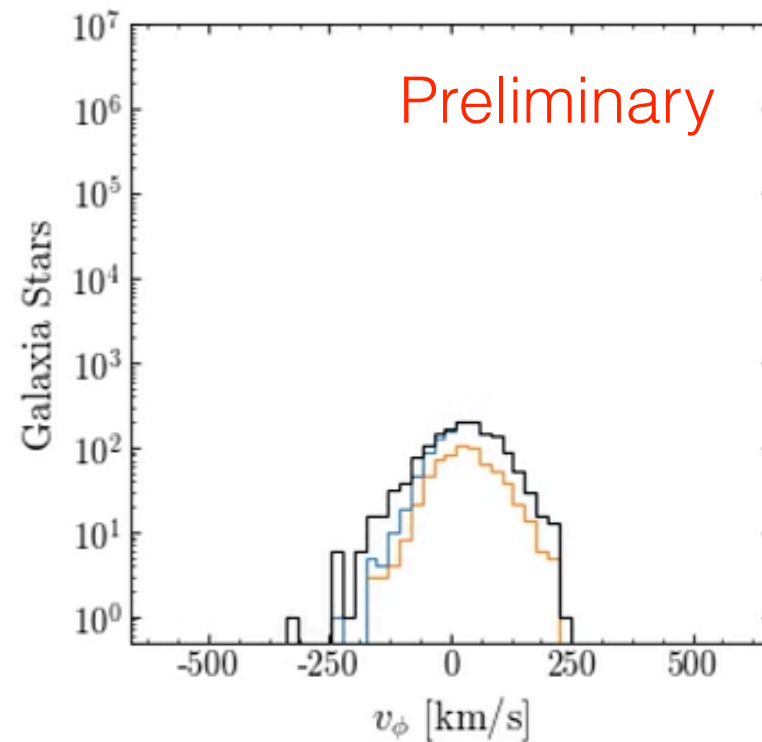
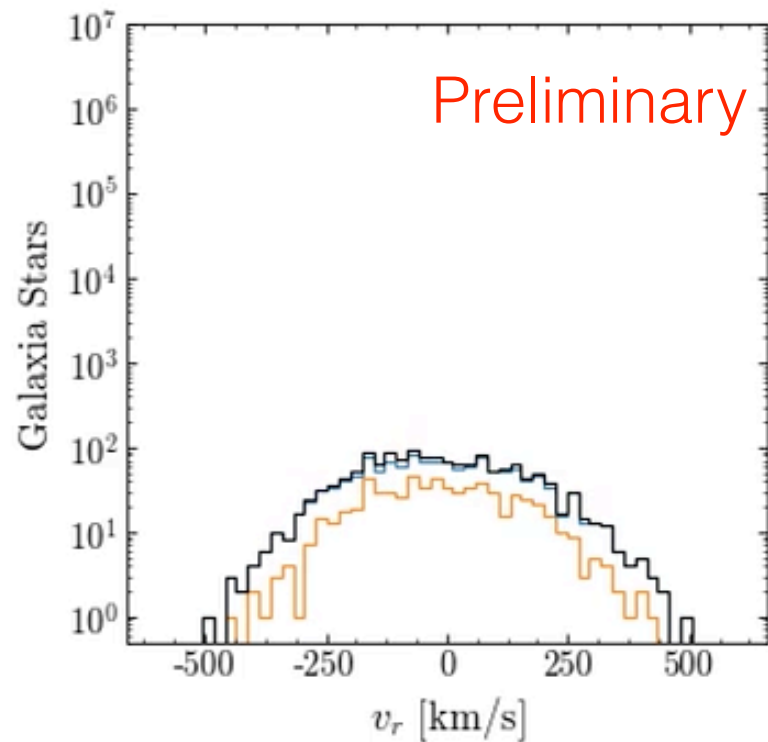
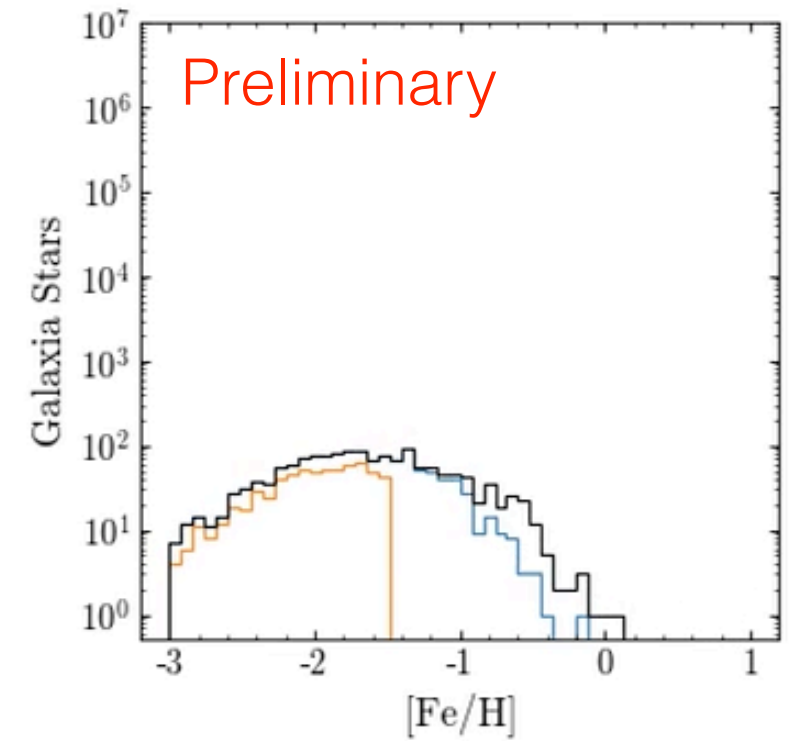
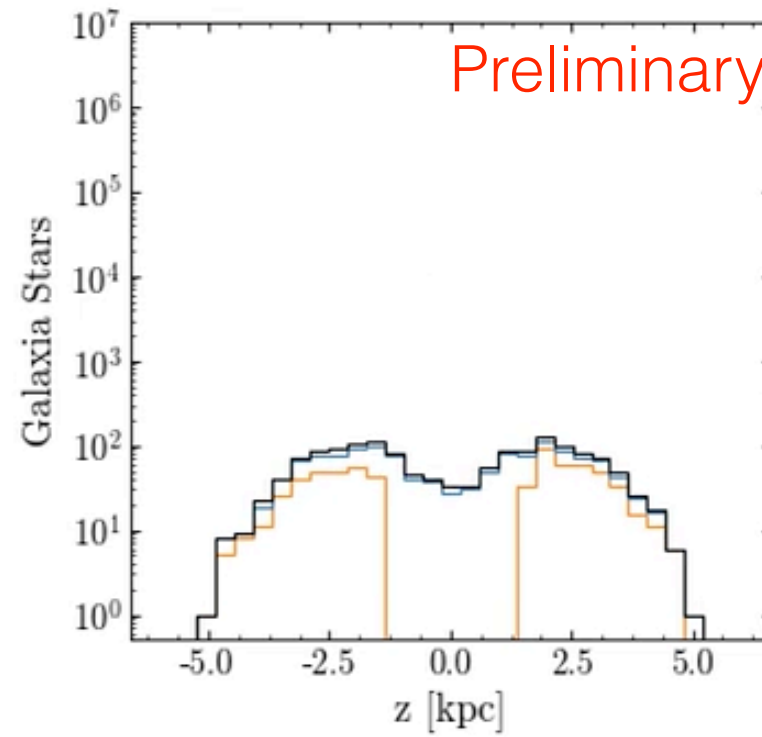
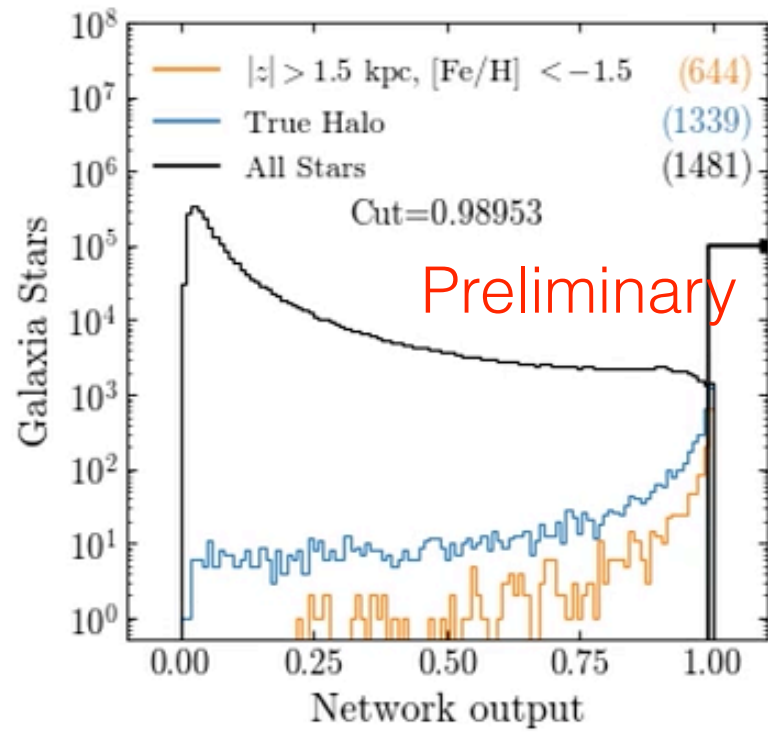
# Learning the halo



# Learning the halo



# Learning the halo



# Compare with other methods

**ZM:**  $|z| > 1.5$  kpc and  $[\text{Fe}/\text{H}] < -1.5$

**Kinematic selection** defines any star which has  $|\mathbf{v} - \mathbf{v}_{LSR}| > v_{LSR}$  as halo, where  $\mathbf{v} = (v_x, v_y, v_z)$  and  $\mathbf{v}_{LSR} = (0, 232, 0)$  km/s.

**Metallicity selection** use gaussian mixture model on 3D velocities. One group should have a peak consistent with the disk (either in  $v_y$  or  $v_\phi$ ). The halo stars are then defined as the stars which have  $[\text{Fe}/\text{H}] < -1$  and are not part of the group with velocities consistent with the disk.

	Halo	Non-halo	FPR	TPR	Purity
Galaxia test set	4245	2441801	-	-	-
$NN > 0.98929$	1359	151	$6.26 \times 10^{-5}$	0.320	90%
ZM	1093	193	$7.90 \times 10^{-5}$	0.257	85%
Kinematic	3139	1763	$7.22 \times 10^{-4}$	0.739	64%
Metallicity	3880	44404	0.0182	0.914	8.0%



# Learning the halo

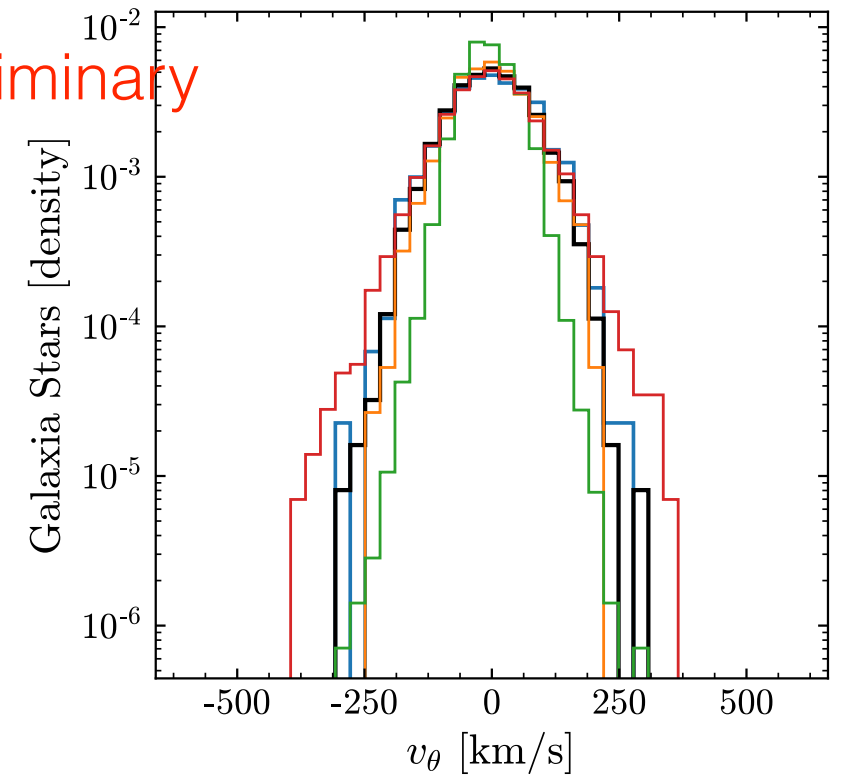
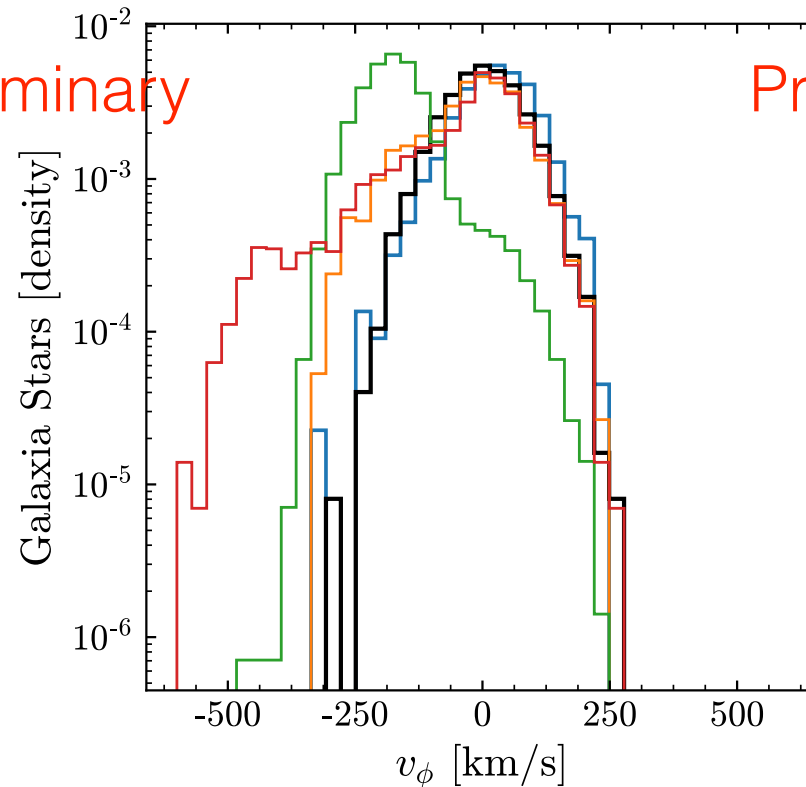
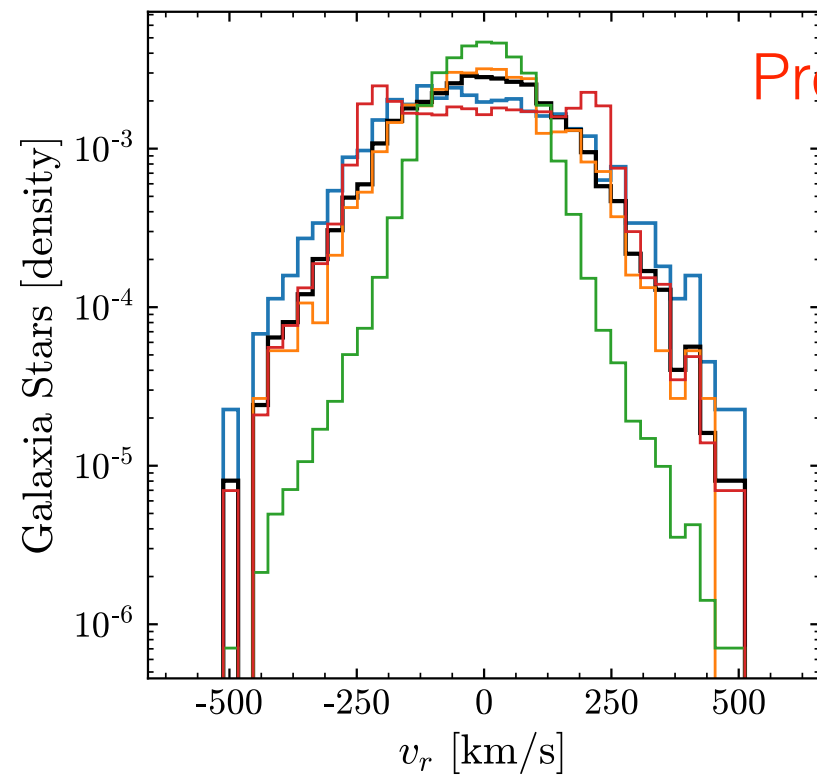
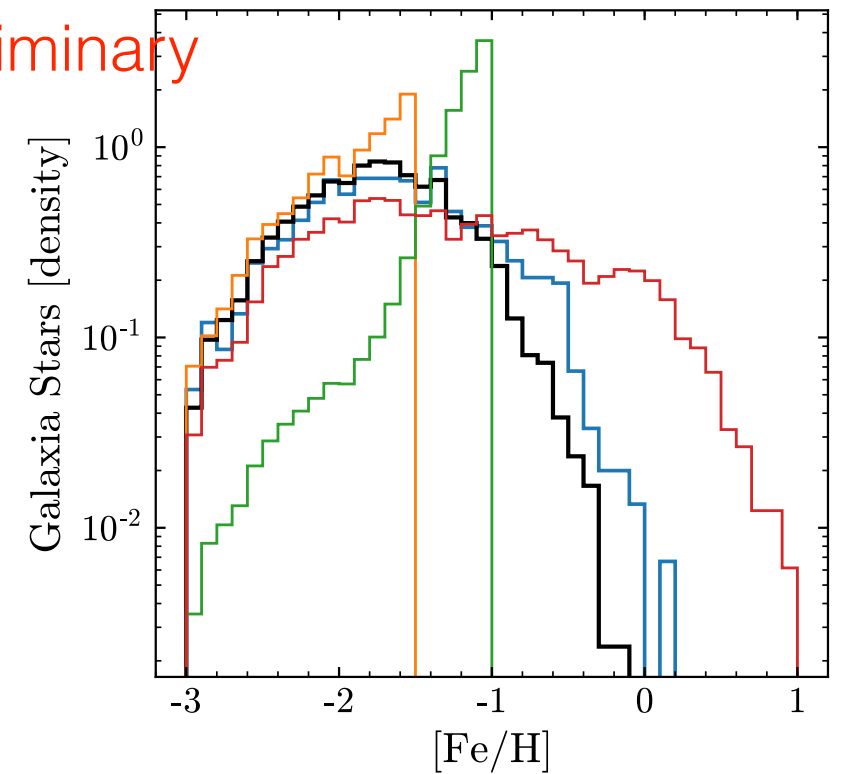
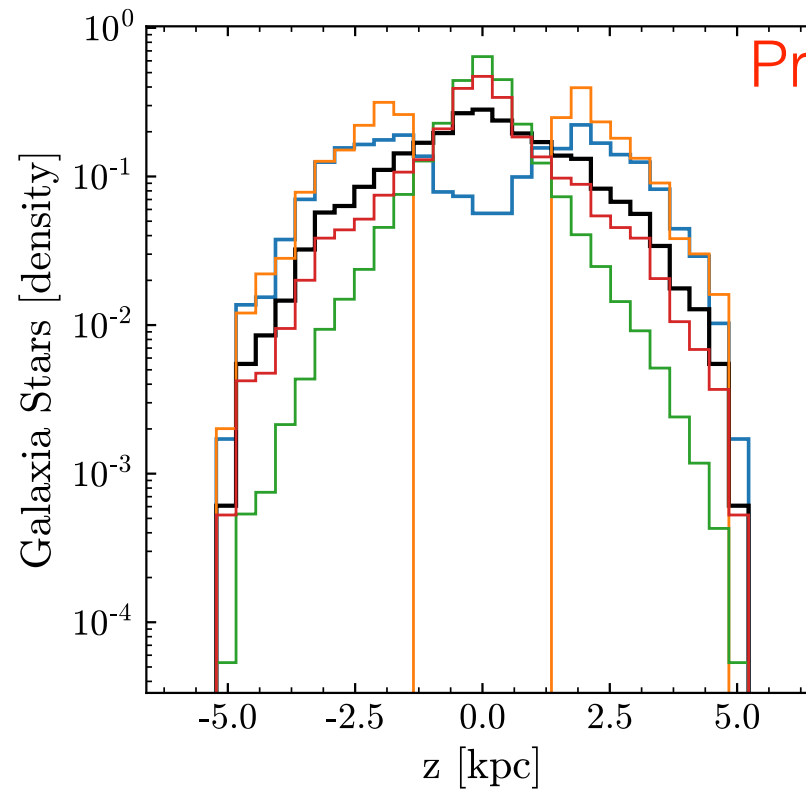
True Halo Stars

Neural Network

$[\text{Fe}/\text{H}] < -1.5, |z| > 1.5 \text{ kpc}$

Kinematic

Metallicity



# Learning the halo

Is it possible to classify halo stars using only 5-d information?

## Sampling

- Draw stars from model distributions
- Defined labels
- Fast data generation

- Classification is possible!
- Can perform better than traditional methods
- High purity still preserves underlying distributions

# Learning the halo

Is it possible to classify halo stars using only 5-d information?

## Sampling

- Draw stars from model distributions
- Defined labels
- Fast data generation

## Simulation

- Distributions from interaction
- Labels from merger history
- Can't generate ourselves

# Learning the halo

## Simulation

arXiv.org > astro-ph > arXiv:1806.10564

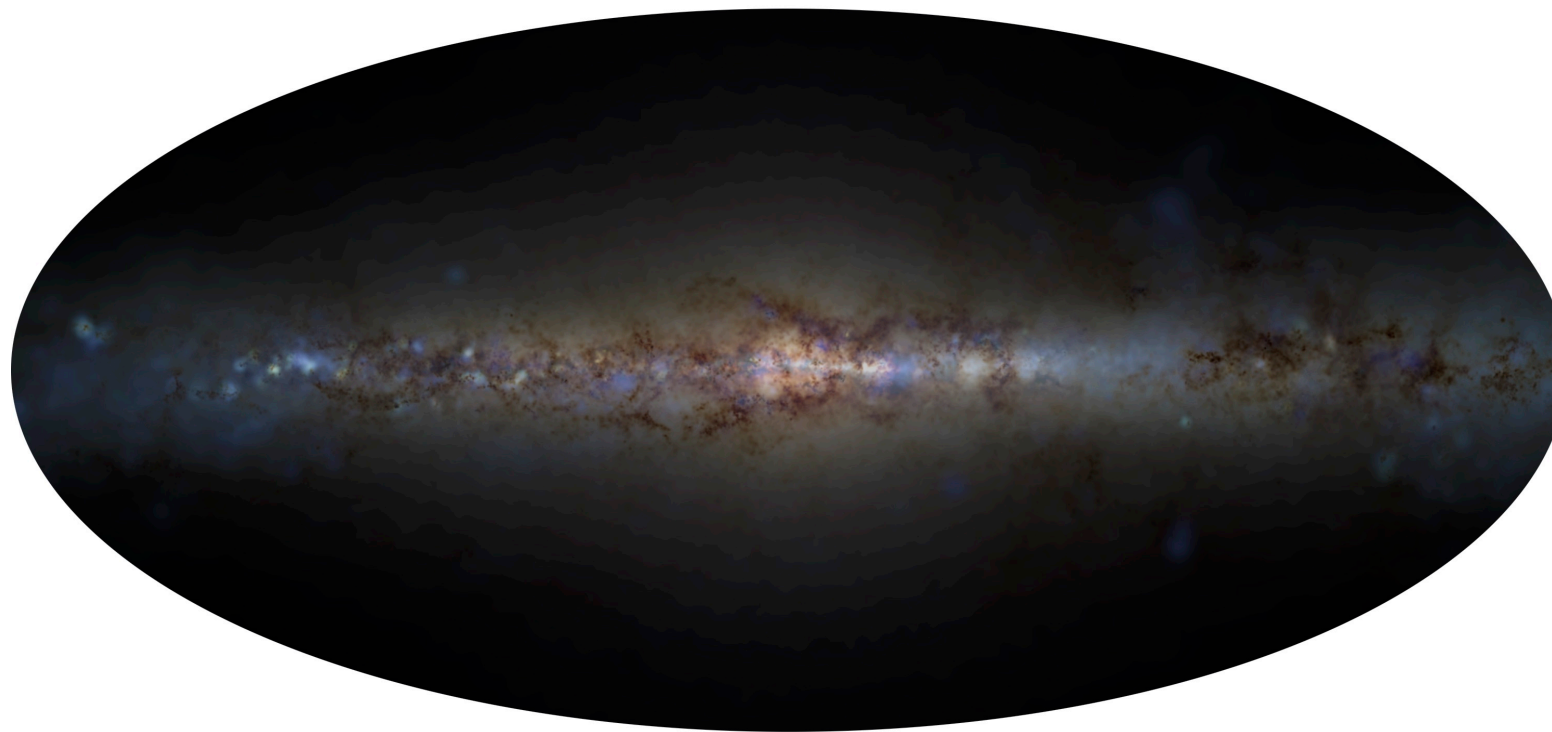
Search or Article

(Help | Advanced search)

Astrophysics > Astrophysics of Galaxies

### Synthetic Gaia surveys from the FIRE cosmological simulations of Milky-Way-mass galaxies

Robyn E. Sanderson (1), Andrew Wetzel (2), Sarah Loebman (2), Sanjib Sharma (3), Philip F. Hopkins (1), Shea Garrison-Kimmel (1), Claude-André Faucher-Giguère (4), Dušan Kereš (5), Eliot Quataert (6) ((1) California Institute of Technology, (2) University of California at Davis, (3) University of Sydney, (4) Northwestern University, (5) University of California at San Diego, (6), University of California Berkeley)



The Latte suite of FIRE-2 cosmological zoom-in baryonic simulations of Milky Way-mass galaxies (Wetzel et al 2016), part of the Feedback In Realistic Environments (FIRE) simulation project, were run using the Gizmo gravity plus hydrodynamics code in meshless finite-mass (MFM) mode (Hopkins 2015) and the FIRE-2 physics model (Hopkins et al 2018).

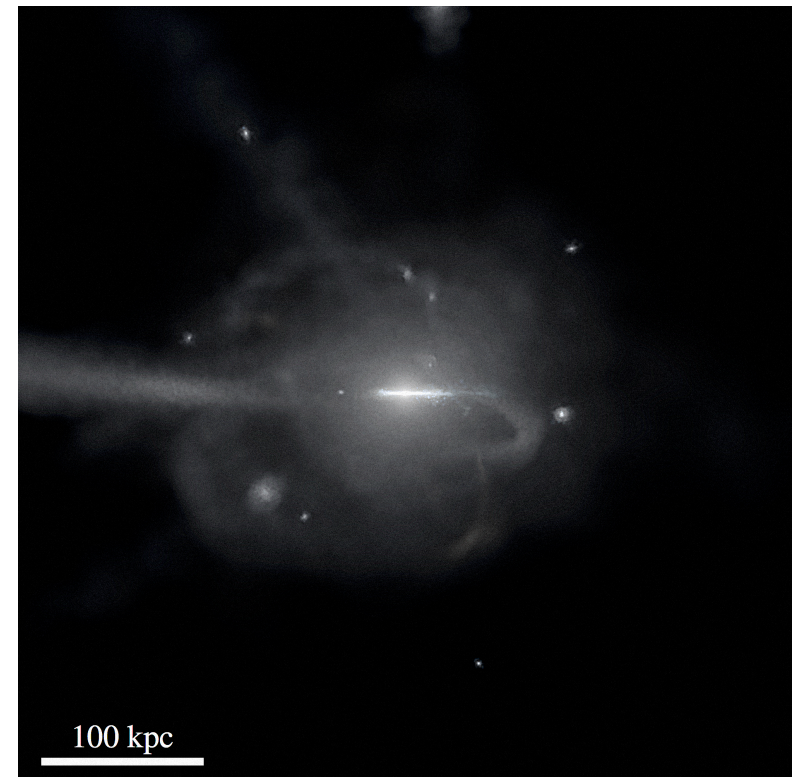
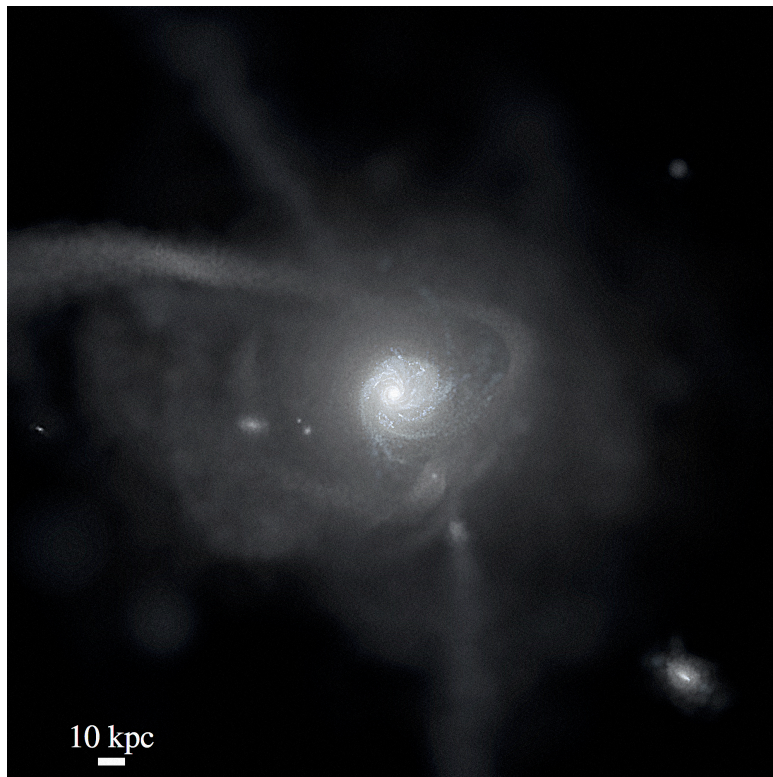
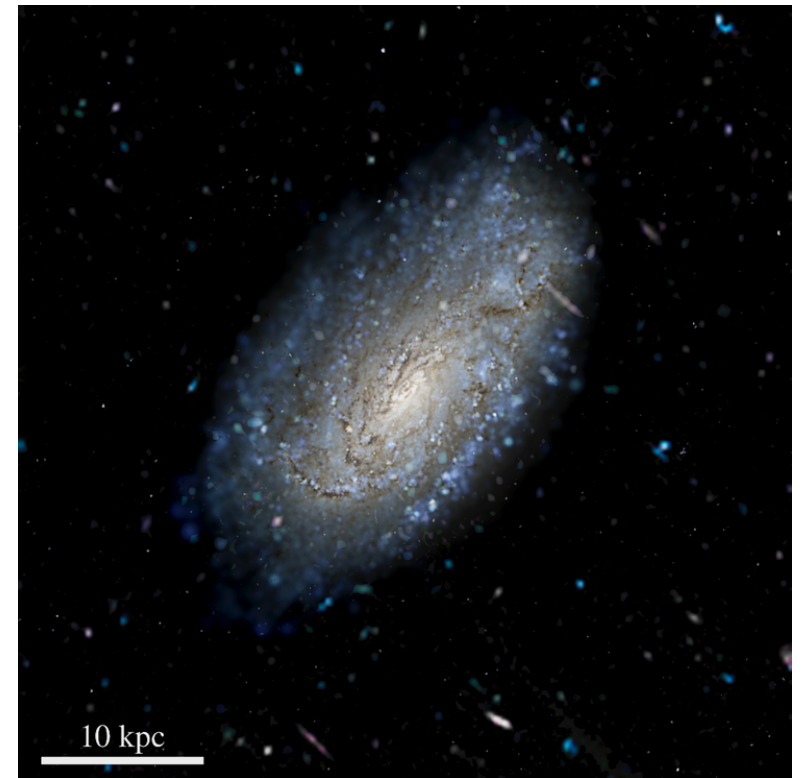
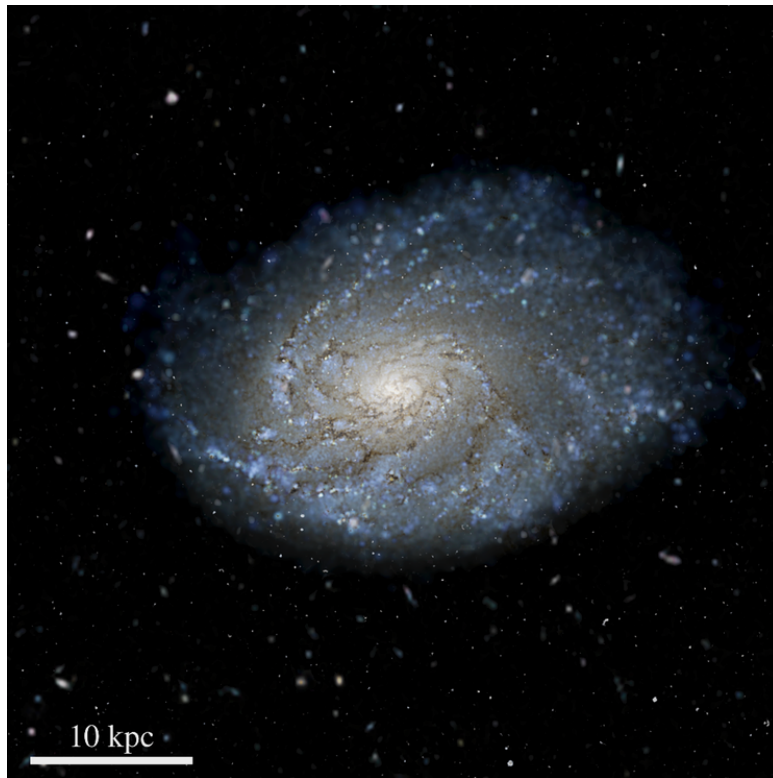
Synthetic Gaia DR2-like surveys of the Latte suite of FIRE-2 simulations were created via the Ananke framework (Sanderson et al 2018).



# Learning the halo

## Simulation

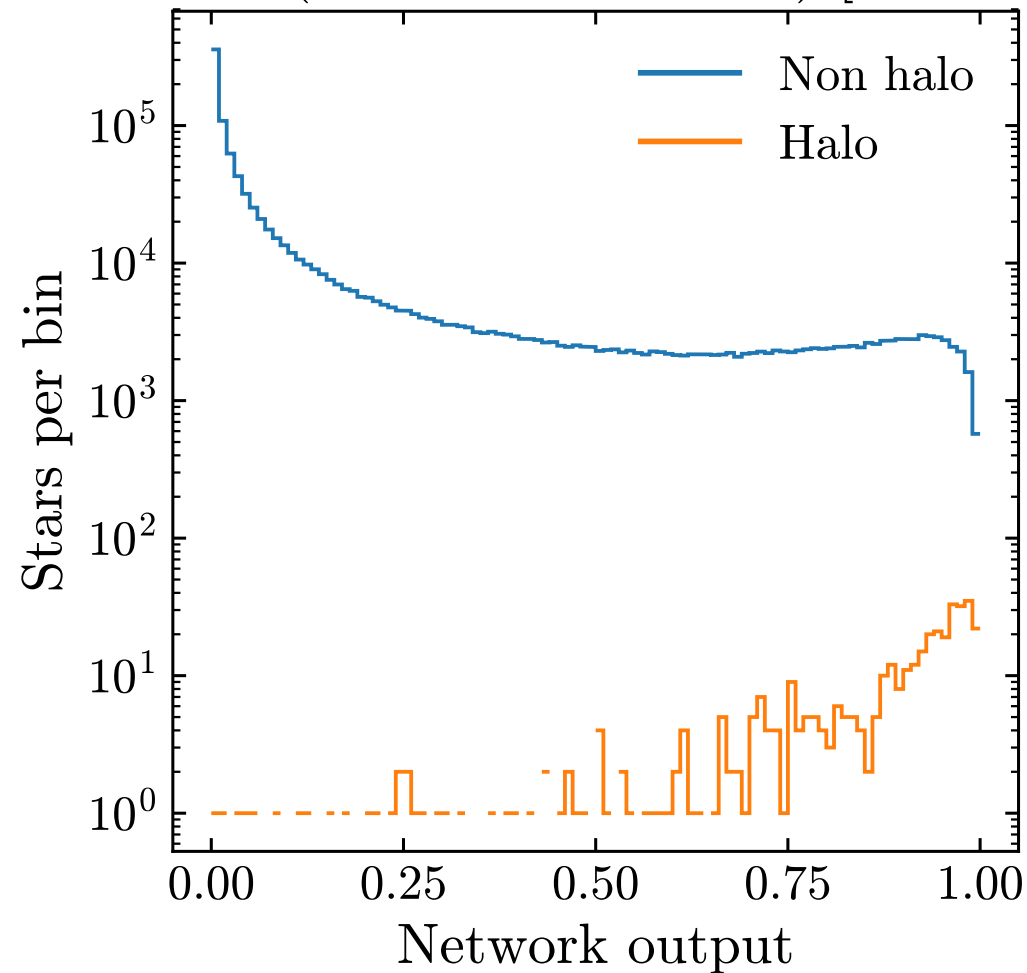
- Not smooth distributions
- Very large dataset
- Expect this to be more challenging
- How do deal with “measurement” errors



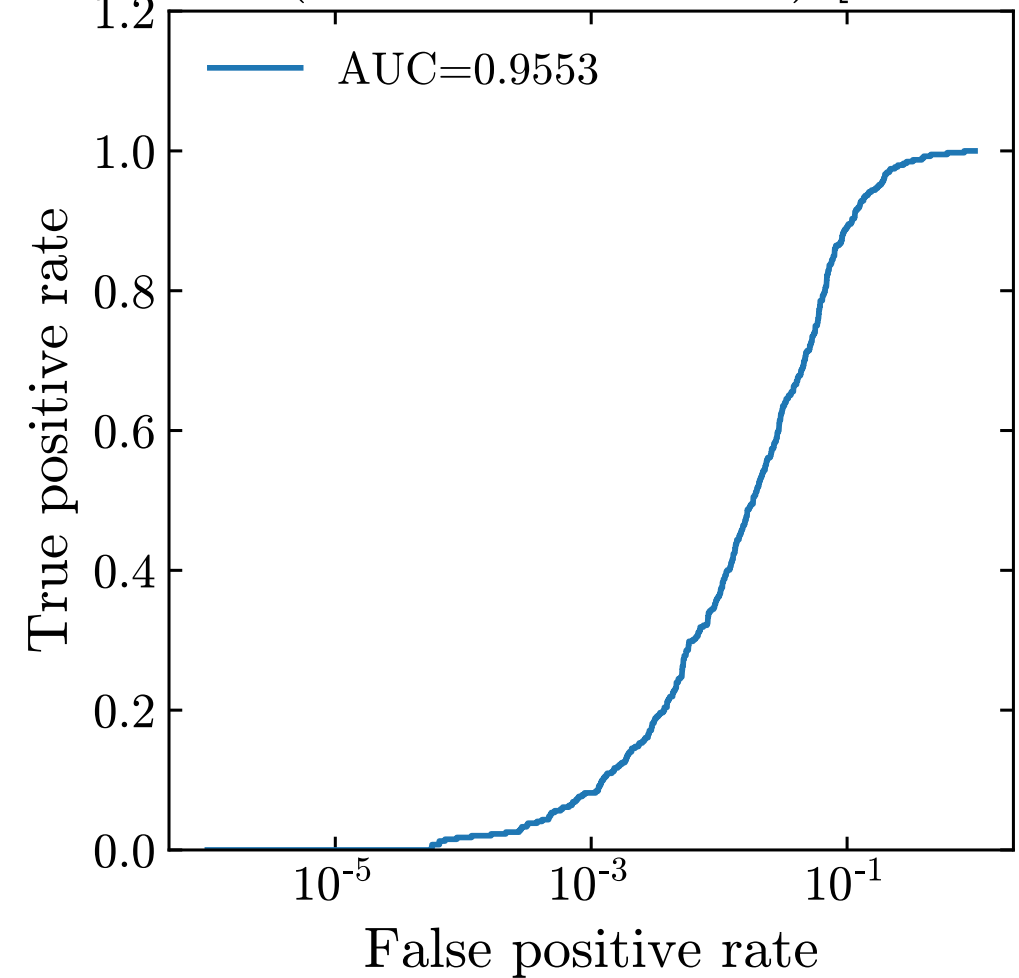
# Learning the halo

## Simulation

Test data (Measured Parallax) [small errors]

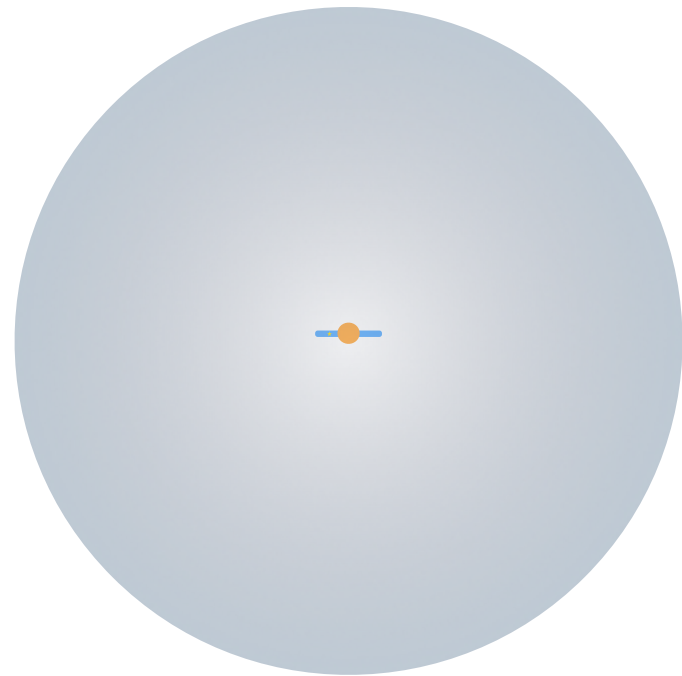


Test data (Measured Parallax) [small errors]



Looks promising, still have issues to deal with

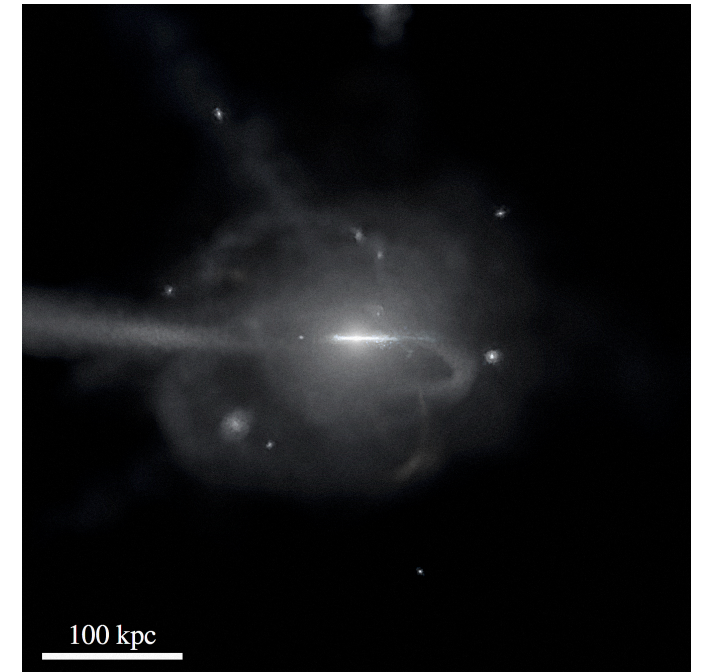
# Conclusion



Hierarchical  
Merger Model

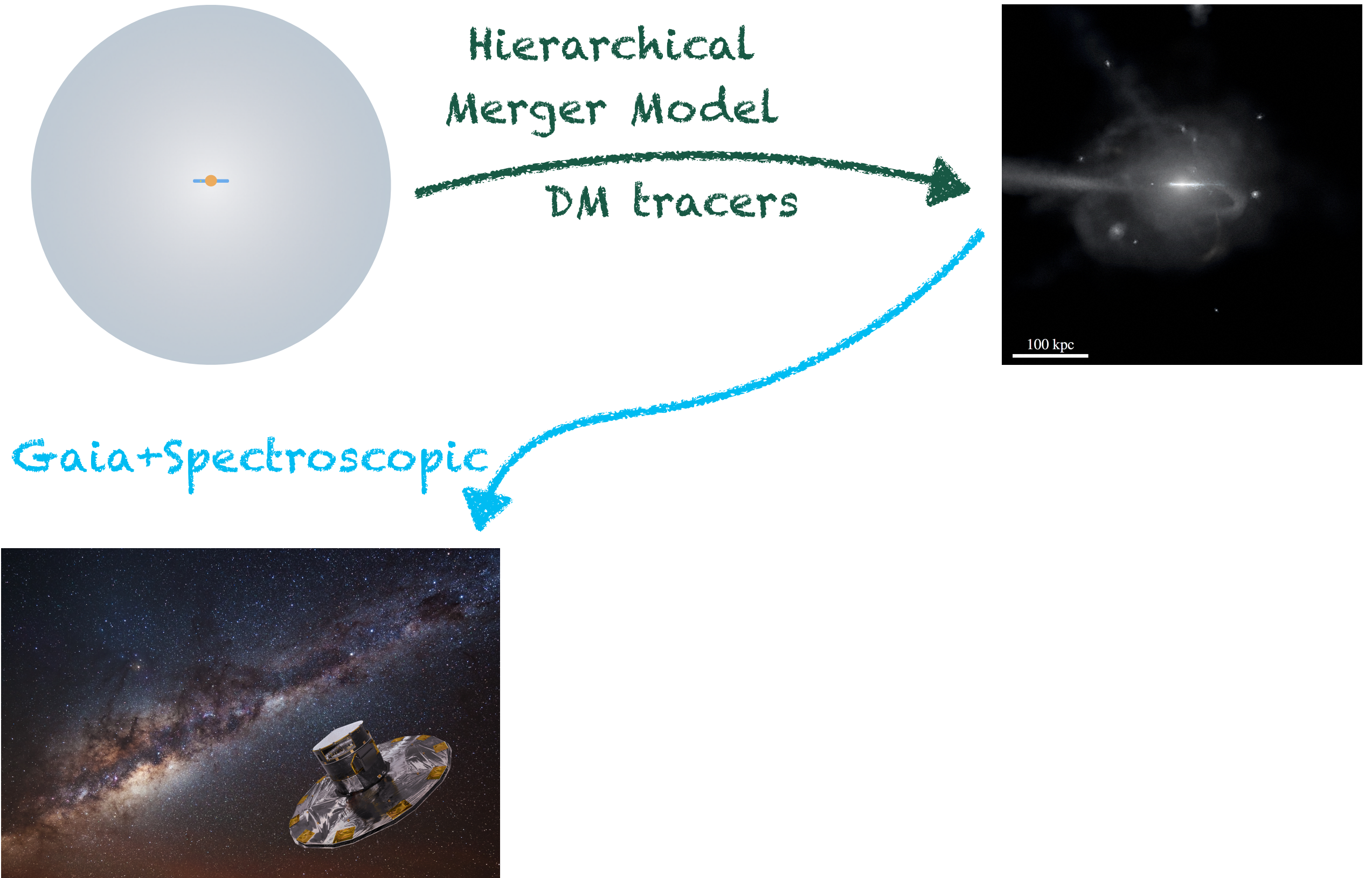


DM tracers



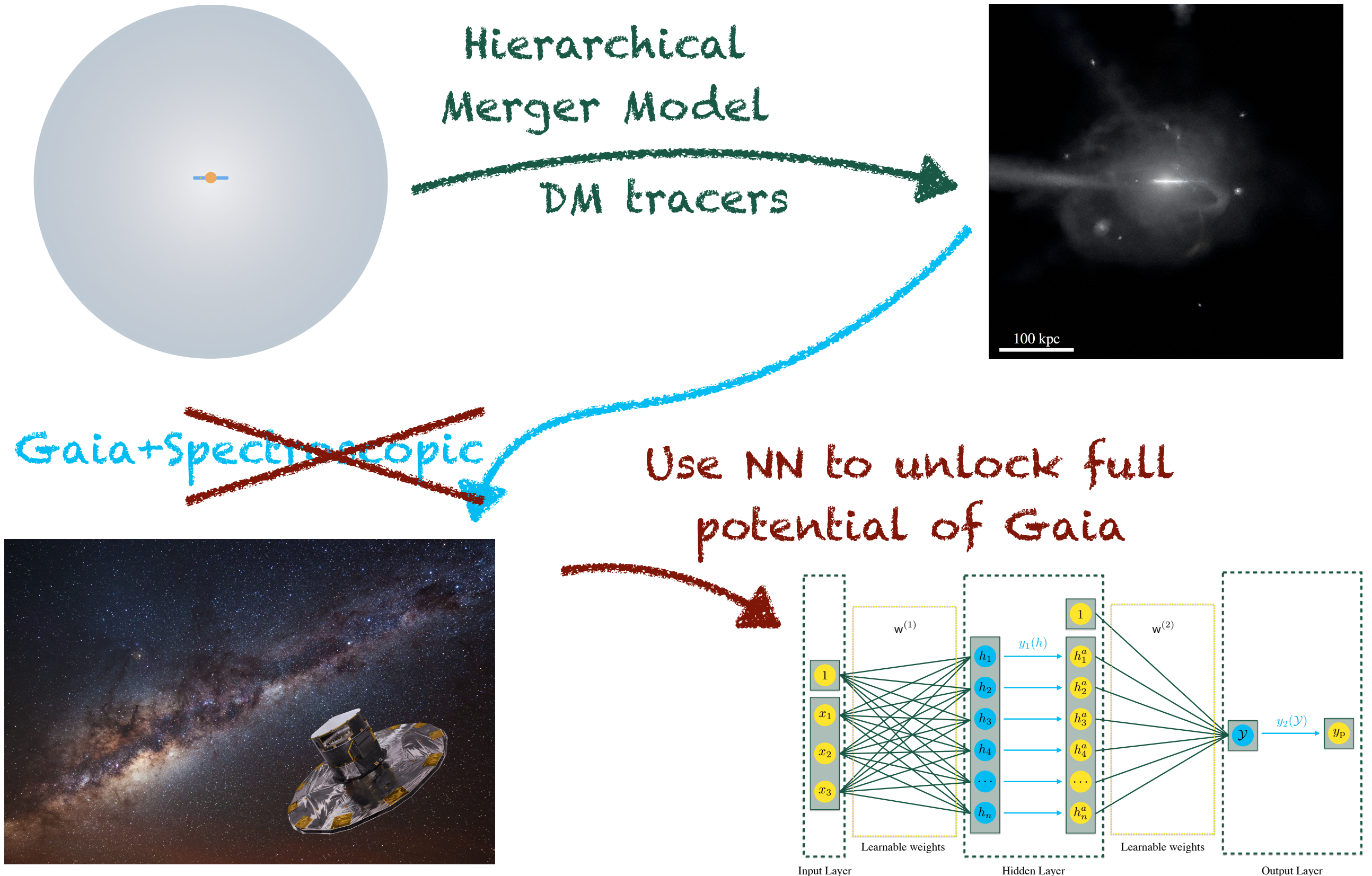


# Conclusion





# Conclusion



# Backup

# Toy model of spiral galaxy

Examine the phase space distribution of the halo:  $f(\mathbf{x}, \mathbf{v})$

$$\int f(\mathbf{x}, \mathbf{v}) d^3\mathbf{x} d^3\mathbf{v} = 1 \quad (\text{probability})$$

Conservation of  
probability

$$\frac{\partial f}{\partial t} + \dot{\mathbf{x}} \frac{\partial f}{\partial \mathbf{x}} + \dot{\mathbf{v}} \frac{\partial f}{\partial \mathbf{v}} = 0$$

Boltzmann equation

- Non-relativistic
- Collisionless

# Toy model of spiral galaxy

Examine the phase space distribution of the halo:  $f(\mathbf{x}, \mathbf{v})$

$$\int f(\mathbf{x}, \mathbf{v}) d^3\mathbf{x} d^3\mathbf{v} = 1 \quad (\text{probability})$$

Conservation of  
probability

$$\frac{\partial f}{\partial t} + \dot{\mathbf{x}} \frac{\partial f}{\partial \mathbf{x}} + \dot{\mathbf{v}} \frac{\partial f}{\partial \mathbf{v}} = 0$$

Boltzmann equation

- Non-relativistic
- Collisionless

Steady state /  
Virialized / Equilibrium

$$f(\mathbf{x}, \mathbf{v}) = f(\mathcal{E})$$
$$\mathcal{E} = \phi - \frac{1}{2}v^2$$

must be function of  
integrals of motion

$$f(\mathbf{x}, \mathbf{v}) \propto e^{\frac{\phi - v^2/2}{\sigma^2}}$$



# Toy model of spiral galaxy

---

Use the phase space density to get derive the particle density

$$\rho(\mathbf{x}) = \int d^3v \, f(\mathbf{x}, \mathbf{v}) = \int 4\pi v^2 f(\mathbf{x}, \mathbf{v}) \, dv \propto e^{\phi/\sigma^2}$$

$$\phi \propto \sigma^2 \log \rho(\mathbf{x})$$

# Toy model of spiral galaxy

Use the phase space density to get derive the particle density

$$\rho(\mathbf{x}) = \int d^3v \, f(\mathbf{x}, \mathbf{v}) = \int 4\pi v^2 f(\mathbf{x}, \mathbf{v}) \, dv \propto e^{\phi/\sigma^2}$$

$$\phi \propto \sigma^2 \log \rho(\mathbf{x})$$

Use Gauss' Law:

$$\nabla^2 \phi = -4\pi G \rho(\mathbf{x}) \propto \nabla^2 (\sigma^2 \log \rho(\mathbf{x}))$$

# Toy model of spiral galaxy

Use the phase space density to get derive the particle density

$$\rho(\mathbf{x}) = \int d^3v \, f(\mathbf{x}, \mathbf{v}) = \int 4\pi v^2 f(\mathbf{x}, \mathbf{v}) \, dv \propto e^{\phi/\sigma^2}$$

$$\phi \propto \sigma^2 \log \rho(\mathbf{x})$$

Use Gauss' Law:

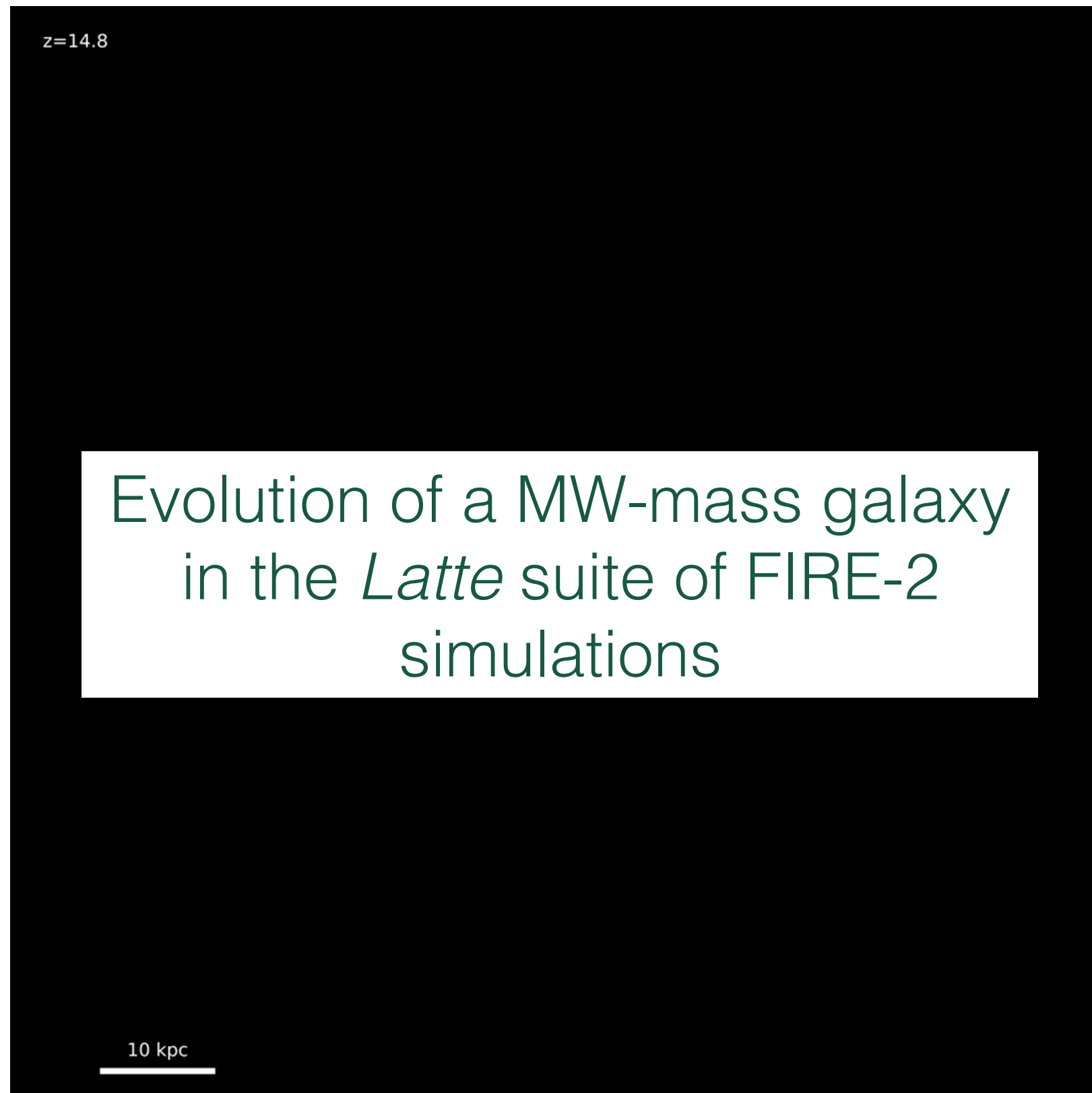
$$\nabla^2 \phi = -4\pi G \rho(\mathbf{x}) \propto \nabla^2 (\sigma^2 \log \rho(\mathbf{x}))$$

- collisionless
- self-gravitating
- isotropic
- isothermal gas

$$\rho(\mathbf{x}) \propto \frac{\sigma^2}{2\pi G r^2}$$

$$f(\mathbf{v}) \propto e^{\frac{-v^2}{2\sigma^2}}$$

# NOT a toy model of spiral galaxy



<http://www.tapir.caltech.edu/~sheagk/starvids.html>

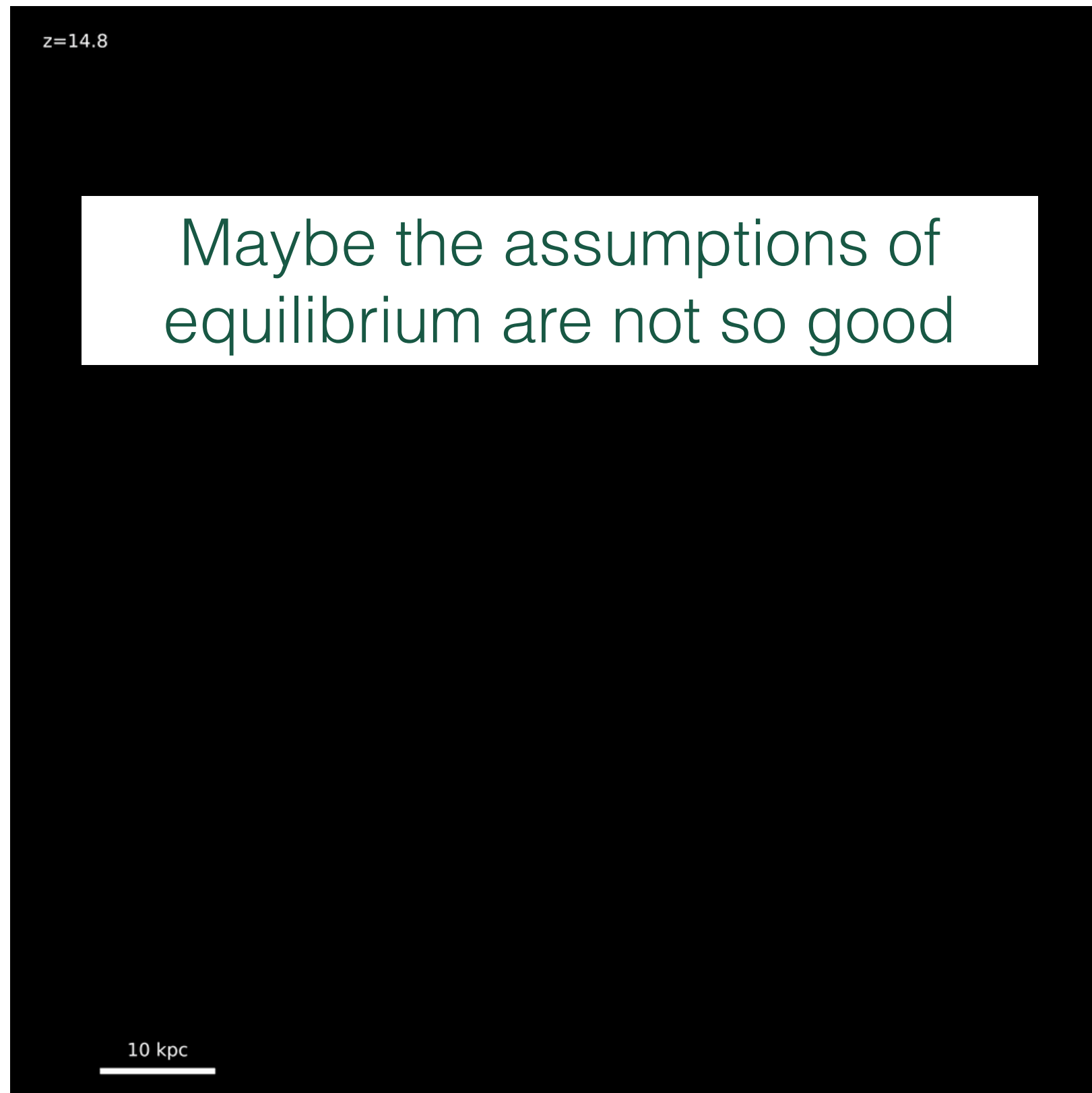


# NOT a toy model of spiral galaxy



<http://www.tapir.caltech.edu/~sheagk/starvids.html>

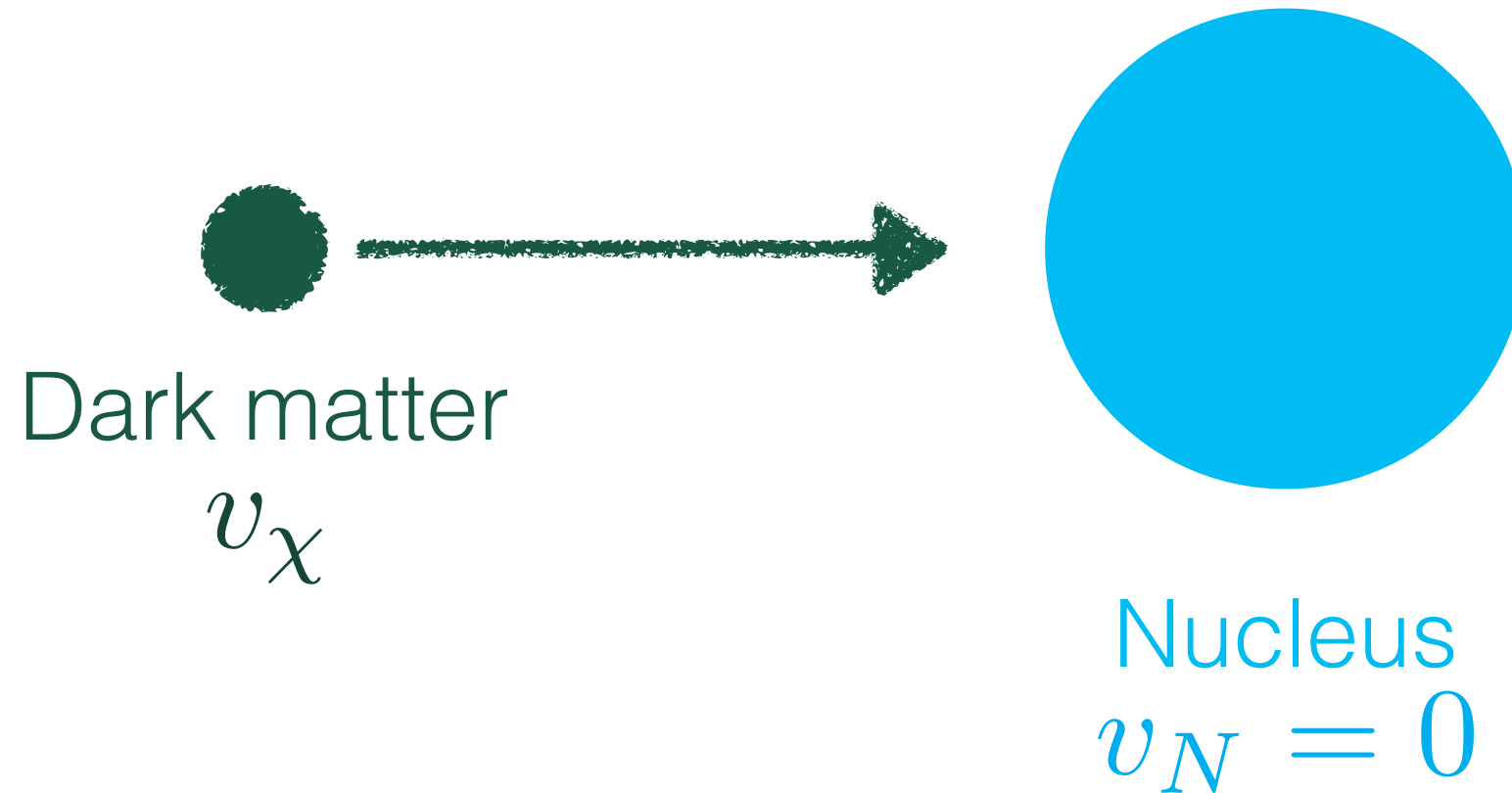
# NOT a toy model of spiral galaxy



<http://www.tapir.caltech.edu/~sheagk/starvids.html>

# Dark matter direct detection

---



# Dark matter direct detection



Kinetic energy of recoiling nucleus:  $E_{R,\text{max}} = \frac{2\mu^2 v_\chi^2}{M_N}$

Only detect recoils above threshold energy

$$v_{\chi,\text{min}} = \sqrt{\frac{M_N E_{R,\text{threshold}}}{2\mu^2}}$$

Small mass needs more velocity



# Dark matter direct detection

---


The rate of nuclear recoils:

$$\frac{dR}{dE_R} = \frac{1}{m_N} \frac{\rho_\chi}{m_\chi} \int_{v_{\min}}^{v_{\max}} d^3v \, v \tilde{f}(\mathbf{v}) \frac{d\sigma(v)}{dE_R}$$

# Dark matter direct detection

The rate of nuclear recoils:

$$\frac{dR}{dE_R} = \frac{1}{m_N} \boxed{\frac{\rho_\chi}{m_\chi}} \int_{v_{\min}}^{v_{\max}} d^3v \, v \tilde{f}(\mathbf{v}) \frac{d\sigma(v)}{dE_R}$$

  $\frac{\rho_\chi}{m_\chi} = n_\chi$ : how many dark matter particles around

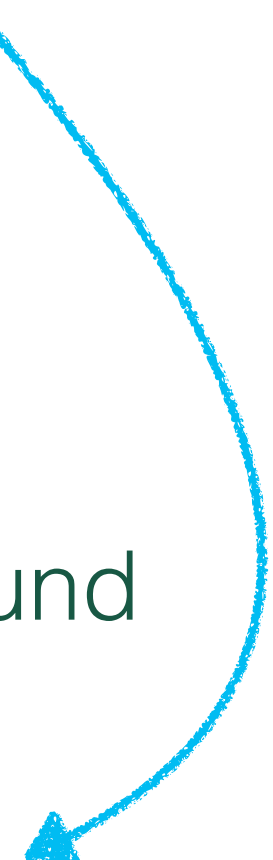
# Dark matter direct detection

The rate of nuclear recoils:

$$\frac{dR}{dE_R} = \frac{1}{m_N} \boxed{\frac{\rho_\chi}{m_\chi}} \int_{v_{\min}}^{v_{\max}} d^3v \, v \tilde{f}(\mathbf{v}) \boxed{\frac{d\sigma(v)}{dE_R}}$$

$\frac{\rho_\chi}{m_\chi} = n_\chi$ : how many dark matter particles around

$\frac{d\sigma(v)}{dE_R}$ : how likely to scatter given the velocity



# Dark matter direct detection

The rate of nuclear recoils:

$$\frac{dR}{dE_R} = \frac{1}{m_N} \boxed{\frac{\rho_\chi}{m_\chi}} \int_{v_{\min}}^{v_{\max}} d^3v \, v \, \boxed{\tilde{f}(\mathbf{v})} \boxed{\frac{d\sigma(v)}{dE_R}}$$

$\frac{\rho_\chi}{m_\chi} = n_\chi$ : how many dark matter particles around

$\frac{d\sigma(v)}{dE_R}$ : how likely to scatter given the velocity

$\tilde{f}(\mathbf{v})$ : the probability to have certain velocity



# Dark matter direct detection

The rate of nuclear recoils:

$$\frac{dR}{dE_R} = \frac{1}{m_N} \left[ \frac{\rho_\chi}{m_\chi} \right] \int_{v_{\min}}^{v_{\max}} d^3v \, v \, \tilde{f}(\mathbf{v}) \left[ \frac{d\sigma(v)}{dE_R} \right]$$

galaxy escape velocity

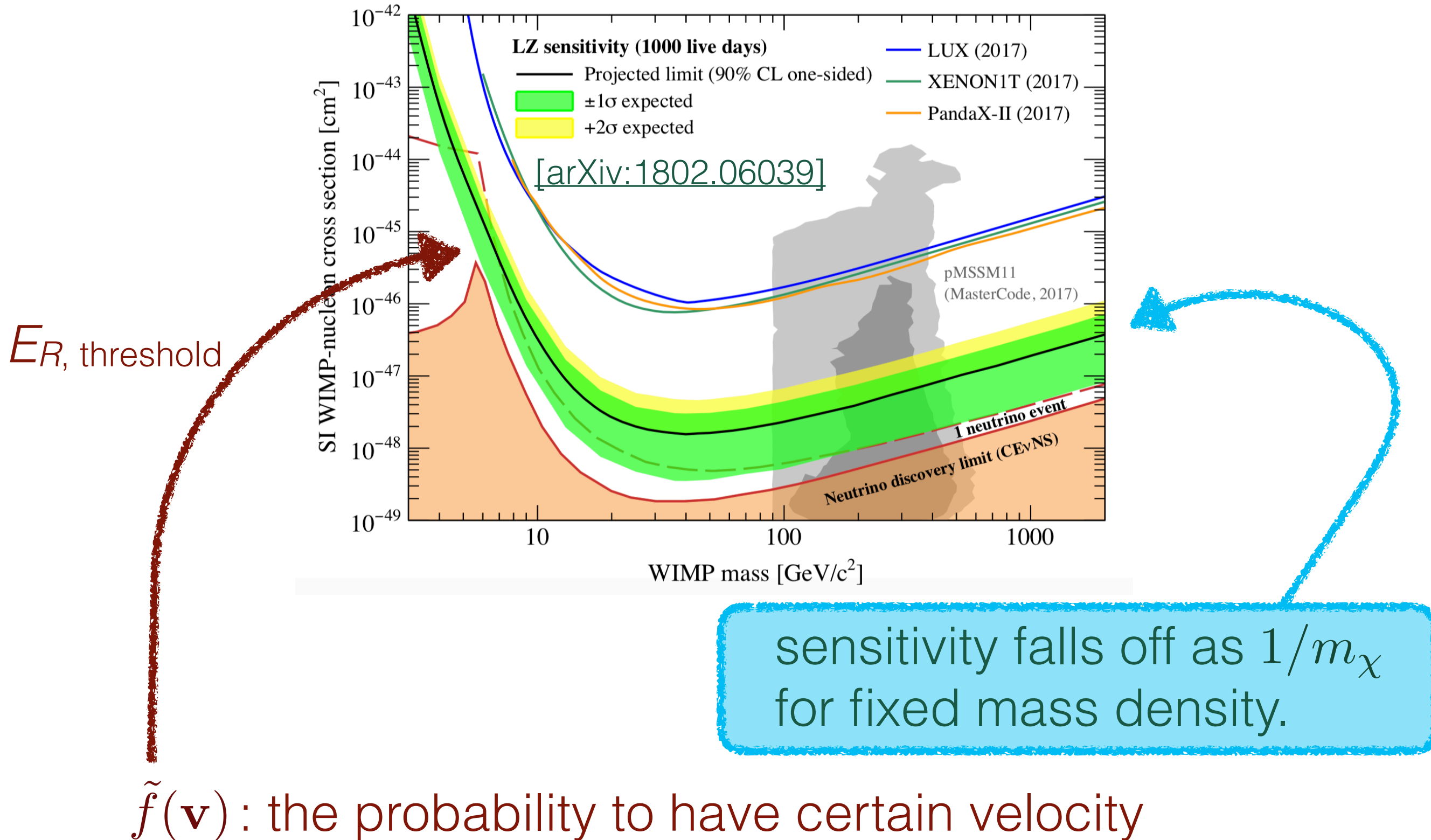
minimum velocity to achieve  $E_R$

$\frac{\rho_\chi}{m_\chi} = n_\chi$ : how many dark matter particles around

$\frac{d\sigma(v)}{dE_R}$ : how likely to scatter given the velocity

$\tilde{f}(\mathbf{v})$ : the probability to have certain velocity

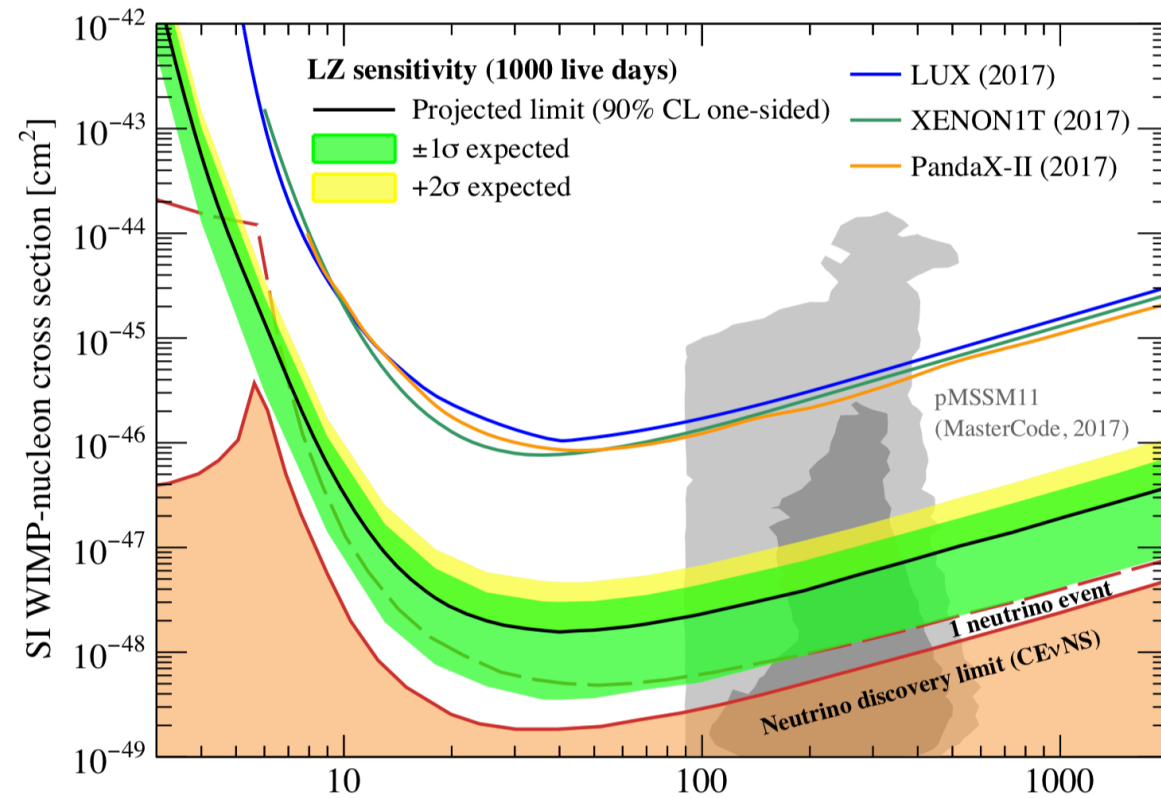
# Dark matter direct detection



	# sources in Gaia DR2	# sources in Gaia DR1
<b>Total number of sources</b>	<b>1,692,919,135</b>	<b>1,142,679,769</b>
Number of 5-parameter sources	1,331,909,727	2,057,050
Number of 2-parameter sources	361,009,408	1,140,622,719
Sources with mean G magnitude	1,692,919,135	1,142,679,769
Sources with mean G <sub>BP</sub> -band photometry	1,381,964,755	-
Sources with mean G <sub>RP</sub> -band photometry	1,383,551,713	-
Sources with radial velocities	7,224,631	-
Variable sources	550,737	3,194
Known asteroids with epoch data	14,099	-
Gaia-CRF sources	556,869	2,191
Effective temperatures (T <sub>eff</sub> )	161,497,595	-
Extinction (A <sub>G</sub> ) and reddening (E(G <sub>BP</sub> -G <sub>RP</sub> ))	87,733,672	-
Sources with radius and luminosity	76,956,778	-

<https://www.cosmos.esa.int/web/gaia/dr2>

# Toy model of spiral galaxy



[arXiv:1802.06039]

$$f(\mathbf{v}) = \begin{cases} \frac{1}{N} \left( e^{-v^2/v_0^2} - e^{-v_{esc}^2/v_0^2} \right) & v < v_{esc} \\ 0 & v > v_{esc} \end{cases}$$