

# Mixing and CPV in $D^0$ and $B_s^0$

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- Introduction
  - ... Formalism — differences between neutral mesons
- $D^0 - \bar{D}^0$  mixing
  - ... Measurements and their interpretations
  - ... Calculations of  $\Delta\Gamma$  and  $\Delta m$
- $B_s^0 - \bar{B}_s^0$  mixing
  - ... Constraints on new physics
  - ... Implications for LHC(b)
- Conclusions

# Neutral meson mixings

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Q: If you asked someone last year when  $D^0$  mixing would be observed...?

A: Probably not to be discovered for at least another decade...



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2006,  $B_s^0 - \bar{B}_s^0$ : measurement of  $\Delta m_s$

2007,  $D^0 - \bar{D}^0$ : growing evidence for  $\Delta\Gamma = \mathcal{O}(0.01)$

What do the last two pieces of data tell us?



# Mixing as a probe of NP

- NP flavor problem: TeV scale (hierarchy problem)  $\ll$  flavor &  $CP$  violation scale

$$\epsilon_K: \frac{(s\bar{d})^2}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^4 \text{ TeV}, \quad B_{d,s} \text{ mixing: } \frac{(b\bar{q})^2}{\Lambda^2} \Rightarrow \Lambda \gtrsim \begin{cases} 10^3 \text{ TeV}, & B_d \\ 10^2 \text{ TeV}, & B_s \end{cases}$$

- Almost all extensions of the SM have new sources of CPV & flavor conversion
    - Originate at much higher scale than EWSB and are decoupled (MFV)?
    - Originate from EWSB-related NP, with non-trivial structure?
- 

- Non-SM  $B_s^0$  mixing: many models with new TeV-scale flavor physics; e.g., NMFV: Top may have special role in EWSB, strong coupling to NP, assume NP quasi-aligned with Yukawas (to suppress FCNC's) [Agashe, Papucci, Perez, Pirjol, hep-ph/0509117]

- Large  $D^0$  mixing: quark-squark alignment ( $m_{\tilde{g},\tilde{q}} \lesssim 1\text{TeV}$ ) predicts  $\Delta m/\Gamma \sim \mathcal{O}(\lambda^2)$  (To not violate  $\Delta m_K$  bound,  $\theta_C$  mostly from up sector, predicts sizable  $D$  mixing)



# Neutral meson mixing

- Time evolution of two flavor eigenstates:

$$i \frac{d}{dt} \begin{pmatrix} |P^0(t)\rangle \\ |\bar{P}^0(t)\rangle \end{pmatrix} = \left( M - \frac{i}{2} \Gamma \right) \begin{pmatrix} |P^0(t)\rangle \\ |\bar{P}^0(t)\rangle \end{pmatrix}$$

$M$  and  $\Gamma$  are  $2 \times 2$  Hermitian matrices,  $CPT$  implies  $M_{11} = M_{22}$  and  $\Gamma_{11} = \Gamma_{22}$

- Mass eigenstates are eigenvectors of  $\mathcal{H}$ :  $|P_{L,H}\rangle = p |P^0\rangle \pm q |\bar{P}^0\rangle$

Time dependence involves mixing and decay:  $|P_{L,H}(t)\rangle = e^{-(im_{L,H} + \Gamma_{L,H}/2)t} |P_{L,H}\rangle$

- Decay amplitudes:  $A_f = \langle f | \mathcal{H} | P^0 \rangle$ ,  $\bar{A}_f = \langle f | \mathcal{H} | \bar{P}^0 \rangle$

- Mass and width differences:  $\Delta m = m_H - m_L (> 0)$ ,  $\Delta \Gamma = \Gamma_H - \Gamma_L$

Other phase convention independent observables:

$$\left| \frac{\bar{A}_f}{A_f} \right|, \quad \left| \frac{q}{p} \right|, \quad \lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}, \quad \phi_{12} = \arg \left( \frac{M_{12}}{\Gamma_{12}} \right), \quad \text{Im} \frac{\Gamma_{12}}{M_{12}} = \frac{1 - |q/p|^4}{1 + |q/p|^4}$$

(CPV in decay, mixing, interference) (NP can easily modify) (a.k.a.  $A_{SL}$ ; or  $-2A_m$  if  $|q/p| \approx 1$ )



# Not all neutral mesons are born equal

- General solution for eigenvalues:

$$(\Delta m)^2 - \frac{(\Delta\Gamma)^2}{4} = 4|M_{12}|^2 - |\Gamma_{12}|^2, \quad \Delta m\Delta\Gamma = 4\text{Re}(M_{12}\Gamma_{12}^*), \quad \frac{q^2}{p^2} = \frac{2M_{12}^* - i\Gamma_{12}^*}{2M_{12} - i\Gamma_{12}}$$

- If  $|\Delta\Gamma| \ll \Delta m$  ( $|\Gamma_{12}/M_{12}| \ll 1$ ) — Holds for  $B_{d,s}^0$  mixings (in the SM and beyond)

$$\Delta m = 2|M_{12}|(1 + \dots), \quad \Delta\Gamma = 2|\Gamma_{12}| \cos\phi_{12}(1 + \dots) \quad [\Rightarrow \text{NP cannot enhance } \Delta\Gamma_{B_s}]$$

$$\frac{q^2}{p^2} = \frac{(M_{12}^*)^2}{|M_{12}|^2}(1 + \dots) \Rightarrow \arg\frac{q}{p} \propto \phi_{12} \quad \Rightarrow \text{Good sensitivity to NP in } M_{12}$$

- If  $|\Delta\Gamma| \gg \Delta m$  ( $|M_{12}/\Gamma_{12}| \ll 1$ ) — Is this applicable for  $D^0 - \bar{D}^0$  mixing?

$$\Delta\Gamma = 2|\Gamma_{12}|(1 + \dots), \quad \Delta m = 2|M_{12}| \cos\phi_{12}(1 + \dots) \quad [\text{Bergmann et al., hep-ph/0005181}]$$

$$\frac{q^2}{p^2} = \frac{(\Gamma_{12}^*)^2}{|\Gamma_{12}|^2}(1 + \dots) \Rightarrow \text{sensitivity to } M_{12} \text{ suppressed. If no CPV in } D \text{ decay } \Rightarrow$$

$$\arg\frac{q}{p} [\sim \arg(\lambda_{K+K-})] \propto 2\left|\frac{M_{12}}{\Gamma_{12}}\right|^2 \sin(2\phi_{12}) \quad \Rightarrow \text{Weak sensitivity to NP in } M_{12}$$

- If  $|\Delta\Gamma| \gg \Delta m$  then sensitivity to NP in  $M_{12}$  is suppressed by  $\Delta m/\Delta\Gamma$



# New physics effects on mixing

- New physics modifies  $M_{12}$ ; CPV in mixing observable via  $\phi = \arg(q/p)$  or  $|q/p| \neq 1$   
Observing  $\phi \neq$  SM prediction may be the best hope to find NP
- Mixing parameters:  $B_{d,s}$ :  $\Delta\Gamma \ll \Delta m$ ,  $K$ :  $\Delta\Gamma \approx -2\Delta m$ ,  $D$ :  $\Delta\Gamma \gtrsim$  or  $\gg \Delta m$ 
  - If  $\Delta m \gg$  or  $\ll \Delta\Gamma$  then  $|q/p| \approx 1$  — If  $\Delta\Gamma \sim \Delta m$  then  $|q/p|$  may be far from 1
  - If  $\Delta m \gg \Delta\Gamma$ , the CPV phase can be **LARGE**:  $\phi = \arg(M_{12}) + \mathcal{O}(\Gamma_{12}^2/M_{12}^2)$
  - If  $\Delta m \ll \Delta\Gamma$ , the CPV phase becomes **SMALL**:  $\phi = \mathcal{O}(M_{12}^2/\Gamma_{12}^2) \times \sin(2\phi_{12})$

$\Rightarrow$  It is of prime importance to determine relative magnitudes of  $\Delta m_D$  and  $\Delta\Gamma_D$
- Since  $\Delta m_D$  not yet measured, use  $|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$  instead of  $|D_{L,H}\rangle$



$D^0 - \bar{D}^0$  mixing

# Special features of the $D^0 - \bar{D}^0$ system

- Of the neutral meson systems  $D^0 - \bar{D}^0$  mixing is unique in that:
  - The only meson where mixing is generated by the down type quarks
  - It involves only the first two generations:  $\text{CPV} > 10^{-3}$  would signal new physics
  - Expected to be small in the SM:  $\Delta m, \Delta\Gamma \lesssim 10^{-2} \Gamma$ , since they are DCS and vanish in the flavor  $SU(3)$  symmetry limit
  - Sensitive to new physics: NP can easily enhance  $\Delta m$  but unlikely to affect  $\Delta\Gamma$   
If  $\Delta\Gamma \gtrsim \Delta m$ : probably large  $SU(3)$  breaking — If  $\Delta m > \Delta\Gamma$ : probably NP
  - Mixing has finally been observed!



# Time dependence of decay rates

- Interplay of mixing and decay — Allow CPV in mixing (not in decay)

Denote:  $x = \Delta m / \Gamma$      $y = \Delta \Gamma / (2\Gamma)$      $R = \left| \frac{\lambda_{K^-\pi^+}}{\lambda_{K^+\pi^-}} \right| = \mathcal{O}(\tan^4 \theta_C)$      $x' = x \cos \delta + y \sin \delta$   
 $y' = y \cos \delta - x \sin \delta \leftarrow$  strong phase

## DCS:

$$\Gamma[D^0(t) \rightarrow K^+\pi^-] \propto e^{-\Gamma t} \left[ R + \sqrt{R} \left| \frac{q}{p} \right| (y' \cos \phi - x' \sin \phi) \Gamma t + \left| \frac{q}{p} \right|^2 \frac{y^2 + x^2}{4} (\Gamma t)^2 \right]$$

$$\Gamma[\bar{D}^0(t) \rightarrow K^-\pi^+] \propto e^{-\Gamma t} \left[ R + \sqrt{R} \left| \frac{q}{p} \right|^{-1} (y' \cos \phi + x' \sin \phi) \Gamma t + \left| \frac{q}{p} \right|^{-2} \frac{y^2 + x^2}{4} (\Gamma t)^2 \right]$$

## SCS:

$$\Gamma[D^0(t) \rightarrow K^+K^-] \propto e^{-\Gamma t} \left[ 1 - \left| \frac{q}{p} \right| (y \cos \phi - x \sin \phi) \Gamma t \right]$$

$$\Gamma[\bar{D}^0(t) \rightarrow K^+K^-] \propto e^{-\Gamma t} \left[ 1 - \left| \frac{q}{p} \right|^{-1} (y \cos \phi + x \sin \phi) \Gamma t \right]$$

## CF:

$$\Gamma[D^0(t) \rightarrow K^-\pi^+] = \Gamma[\bar{D}^0(t) \rightarrow K^+\pi^-] \propto e^{-\Gamma t}$$

- Setting  $\phi = 0$ : no CPV in mixing and choosing  $|D_1\rangle = CP\text{-odd}$  ( $|D_2\rangle = CP\text{-even}$ )



# Mixing parameters from lifetimes

- Measure lifetimes, fitting exponential time dependences in decays to flavor and  $CP$  eigenstates (e.g.,  $K^+K^-$  and  $\pi^+K^-$ )

$$y_{CP} = \frac{\hat{\tau}(D^0 \rightarrow K^- \pi^+)}{\hat{\tau}(D^0 \rightarrow K^+ K^-)} - 1 = \frac{y \cos \phi}{2} \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right) - \frac{x \sin \phi}{2} \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right)$$

$$A_\Gamma = \frac{\hat{\tau}(\bar{D}^0 \rightarrow K^+ K^-) - \hat{\tau}(D^0 \rightarrow K^+ K^-)}{\hat{\tau}(\bar{D}^0 \rightarrow K^+ K^-) + \hat{\tau}(D^0 \rightarrow K^+ K^-)} = \frac{y \cos \phi}{2} \left( \left| \frac{q}{p} \right| - \left| \frac{p}{q} \right| \right) - \frac{x \sin \phi}{2} \left( \left| \frac{q}{p} \right| + \left| \frac{p}{q} \right| \right)$$

If  $CP$  is conserved:  $A_\Gamma = 0$  and  $y_{CP} = \pm y$

- **Results:**  $y_{CP} = 0.011 \pm 0.003$  ( $3.5\sigma$ ) [HFAG — Belle, BaBar, E791, FOCUS, CLEO]  
 $A_\Gamma = 0.0001 \pm 0.0034$  [Belle, hep-ex/0703036]

- If  $y \cos \phi$  dominates  $y_{CP}$ :  $\frac{A_\Gamma}{y_{CP}} \approx \frac{|q/p|^2 - 1}{|q/p|^2 + 1} - \frac{x}{y} \tan \phi$  (smaller error?) [Nir, hep-ph/0703235]

- Observed value of  $y_{CP}$  could be explained by  $y \approx 0.01$  or large  $x$ ,  $|q/p| - 1$ , and  $\phi$



# Mixing parameters from $D \rightarrow K^\pm \pi^\mp$

- Measure time dependence of “wrong sign” DCS decays

Fit to:  $e^{-\Gamma t} \{ (\text{dir-DCS}) + (\Gamma t)(\text{int-SCS}) + (\Gamma t)^2(\text{mix-CF}) \}$

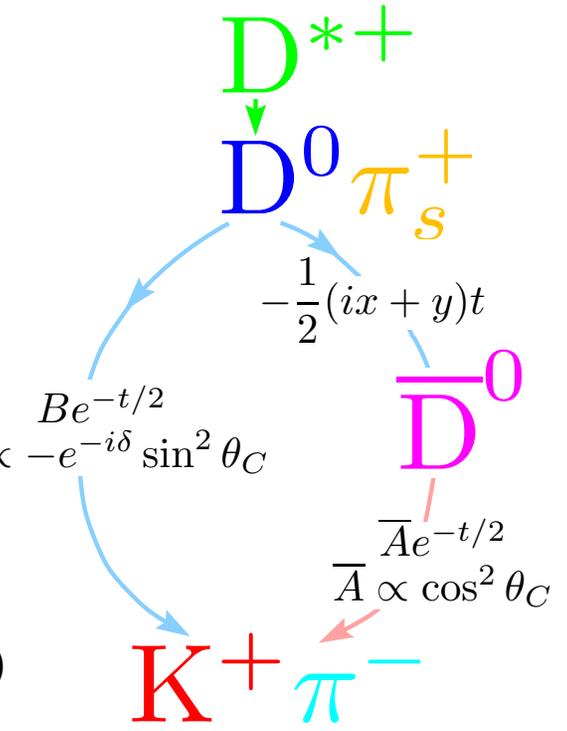
Neglecting CPV, 3 fit parameters:  $R(\equiv R_D), x', y'$

$$\left. \begin{aligned} y' &= 0.0097 \pm 0.0054 \\ x'^2 &= (-2.2 \pm 3.7) \times 10^{-4} \end{aligned} \right\} \text{3.9}\sigma \text{ evidence for mixing}$$

[BaBar, hep-ex/0703020]  $B \propto -e^{-i\delta} \sin^2 \theta_C$

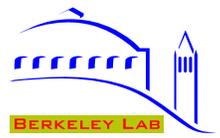
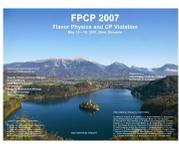
- Fits allowing CPV:  $R^\pm, x'^\pm, y'^\pm$  [BaBar + Belle + FOCUS + CLEO]

$$x'^\pm = \left| \frac{q}{p} \right|^{\pm 1} (x' \cos \phi \pm y' \sin \phi), \quad y'^\pm = \left| \frac{q}{p} \right|^{\pm 1} (y' \cos \phi \mp x' \sin \phi)$$



- If  $y'$  dominates  $y'^\pm$ :  $\frac{y'^+ - y'^-}{y'^+ + y'^-} \approx \frac{|q/p|^2 - 1}{|q/p|^2 + 1} - \frac{x'}{y'} \tan \phi$  (smaller error?) [Nir, hep-ph/0703235]

- Unless there is CPV in decay,  $R^+ = R^-$  ! — Please do 5 param fit with  $A_D \rightarrow 0$  (Early days of  $B \rightarrow \psi K_S$ : quote  $S_{\psi K}$  with  $|\lambda_{\psi K}| = 0$ ; maybe bigger impact here?)



# Mixing parameters from $D \rightarrow K_S \pi^+ \pi^-$

- Study interference in  $m_{K\pi^+} - m_{K\pi^-}$  Dalitz plot — sensitive directly to  $x$  and  $y$

Models well-tuned for measurement of CKM angle  $\gamma$  from  $B^\pm \rightarrow D_{(K_S \pi \pi)} K^\pm$

Some strong phases are known & vary on smaller scales than others ( $\Gamma_{K^*} \ll m_D$ )

- Assuming  $CP$  cons.:  $x = (0.80 \pm 0.29_{-0.12}^{+0.09+0.15})\%$ ,  $y = (0.33 \pm 0.28_{-0.12}^{+0.07+0.08})\%$

[Belle, arXiv:0704.1000]

(I'm a bit concerned about uncertainties related to the fact that we need the amplitude across the Dalitz plot, but have mostly tested its modelling with rates... [maybe it's only me...]  $CP$  tagged  $D$  decays will help.)

- Measurements of wrong sign semileptonic rate ( $D^0 \rightarrow K^+ \ell \bar{\nu}$ ) sensitive to  $x^2 + y^2$

Weaker bounds at present:  $x^2 + y^2 = 0.0010 \pm 0.0009$

[Belle, BaBar, CLEO, E791]

- In the limit of larger data sets: measurements with linear sensitivity to  $x, y$



## Some tensions in data?

- Summary of measurements:

Lifetimes:  $y_{CP} = 0.011 \pm 0.003$

$$A_{\Gamma} = 0.0001 \pm 0.0034$$

BaBar  $K\pi$ :  $y' = 0.0097 \pm 0.0054$

$$x'^2 = -0.00022 \pm 0.00037 \quad x' < 0.023 (2\sigma)$$

Belle  $K\pi\pi$ :  $x = 0.0080 \pm 0.0034$

$$y = 0.0033 \pm 0.0028$$

- It seems to me that  $1\sigma$  ranges of  $x, y, y_{CP}, A_{\Gamma}$  have no solution for  $|q/p|, \cos \phi$  ( $y'$  also depends on  $\delta$ , and  $x'^2$  alone not very restrictive)

Not very significant, but there is room for better consistency

- There is lot to be learned from more precise measurements



## Calculations of $\Delta\Gamma$ and $\Delta m$

# OPE analysis ( $m_c \gg \Lambda$ )

- $D^0 - \bar{D}^0$  mixing only arises at order  $m_s^2/\Lambda_{\chi\text{SB}}^2$  (if  $SU(3)$  violation is perturbative) [Falk et al., hep-ph/0110317]

$SU(3)$  suppression & DCS  $\Rightarrow$  hard to estimate  $x, y$  in the SM:  $x, y \sim \sin^2 \theta_C \epsilon_{SU(3)}^2$

- Short distance box diagram:  $x \propto \frac{m_s^2}{m_W^2} \times \frac{m_s^2}{m_c^2} \rightarrow 10^{-5}$   
 $y$  has additional  $m_s^2/m_c^2$  helicity suppression

- Higher order terms in the OPE are suppressed by fewer powers of  $m_s$  [Georgi '92]

	4-quark	6-quark	8-quark
$\frac{\Delta m}{\Delta m_{\text{box}}}$	1	$\frac{\Lambda^2}{m_s m_c}$	$\frac{\Lambda^4}{m_s^2 m_c^2} \frac{\alpha_s}{4\pi}$
$\frac{\Delta \Gamma}{\Delta m}$	$\frac{m_s^2}{m_c^2}$	$\frac{\alpha_s}{4\pi}$	$\frac{\alpha_s}{4\pi} \beta_0$



[Bigi & Uraltsev ('00) claimed that  $x, y \propto m_s$  is possible]

- Obtain  $x, y \lesssim 10^{-3}$ , with some assumptions about the matrix elements ( $\Lambda \sim 4\pi f_\pi$ )



# Long distance analysis (few final states)

- May be large, but extremely hard to estimate:  $y \sim \frac{1}{2\Gamma} \sum_n \rho_n \langle \bar{D}^0 | H_w | n \rangle \langle n | H_w | D^0 \rangle$

$SU(3)$  breaking has been argued to be  $\mathcal{O}(1)$  based on  $\frac{\mathcal{B}(D^0 \rightarrow K^+ K^-)}{\mathcal{B}(D^0 \rightarrow \pi^+ \pi^-)} \approx 2.8$

Contribution to  $y$ : large cancellations possible, sensitive to strong phase:

$$y_{PP} = \mathcal{B}(D \rightarrow \pi^+ \pi^-) + \mathcal{B}(D \rightarrow K^+ K^-) - 2 \cos \delta \sqrt{\mathcal{B}(D \rightarrow K^- \pi^+) \mathcal{B}(D \rightarrow K^+ \pi^-)}$$
$$\approx (5.76 - 5.29 \cos \delta) \times 10^{-3} \quad (\text{from measured rates})$$

- Assuming  $\cos \delta \sim 1$  [ $SU(3)$  limit] and that these states are representative (many other DCS rates poorly known), it was often stated that  $x \lesssim y < \text{few} \times 10^{-3}$

- The most important long distance effect may be due to phase space:
  - Contrary to  $SU(3)$  breaking in matrix elements, this  $SU(3)$  violation is calculable model independently with mild assumptions
  - Negligible for lightest  $PP$  final states; important for states with mass near  $m_D$



# $\Delta\Gamma$ from $SU(3)$ breaking in phase space

- Phase space difference between final states containing fewer or more strange quarks is a calculable source of  $SU(3)$  breaking — these are “threshold effects”

[Falk *et al.*, hep-ph/0110317]

- For any final state  $F$  in any  $SU(3)$  representation  $R$  (e.g.,  $PP$  can be in 8 or 27), we can calculate the “would-be” value of  $y$ , if  $D$  only decayed to the states in  $F_R$

$$y_{F,R} = \frac{\sum_{n \in F_R} \langle \bar{D}^0 | H_w | n \rangle \rho_n \langle n | H_w | D^0 \rangle}{\sum_{n \in F_R} \Gamma(D^0 \rightarrow n)}$$

- E.g.:  $D \rightarrow PP$  with  $U$ -spin:  $s_1^2 [\Phi(\pi^+, \pi^-) + \Phi(K^+, K^-) - 2\Phi(K^+, \pi^-)] / \Phi(K^+, \pi^-)$

Result is explicitly proportional to  $s_1^2 \equiv \sin^2 \theta_C$  and vanishes in  $SU(3)$  limit as  $m_s^2$

- If decay rates to all representations were known, we could reconstruct  $y$  from  $y_{F,R}$

$$y = \frac{1}{\Gamma} \sum_{F,R} y_{F,R} \left[ \sum_{n \in F_R} \Gamma(D^0 \rightarrow n) \right]$$



# Our estimate of $\Delta\Gamma$

- The 2-, 3-, and 4-body final states account for sizable fraction of the  $D$  width

Small contribution from two- and three-body final states (the  $PP$  contribution is “anomalously” small)

- Large  $SU(3)$  breaking when some states are not allowed at all ( $4m_K > m_D$ ) in heavier multiplets:  $y_{4P} = \mathcal{O}(s_1^2)$   
(Only studied smallest symmetric representations for  $4P$ )

rounded to nearest 5%	
final state	fraction
$PP$	5%
$PV$	10%
$(VV)_{s\text{-wave}}$	5%
$(VV)_{d\text{-wave}}$	5%
$3P$	5%
$4P$	10%

- There are other large rates near threshold, e.g.:  $\mathcal{B}(D^0 \rightarrow K^- a_1^+) = (7.5 \pm 1.1)\%$   
Sizable contributions likely, but are untractable

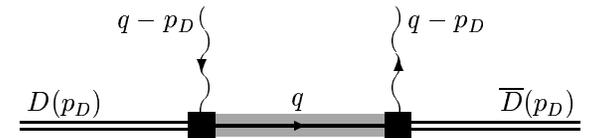
- **Morals:** There are final states that can contribute to  $y$  near the 1% level  
It would require cancellations to suppress  $y_{CP}$  much below 1%



# Connecting $\Delta\Gamma$ with $\Delta m$

- A dispersion relation in HQET relates  $\Delta m$  to an integral of  $\Delta\Gamma$  over the mass  $M$  of a heavy “would-be  $D$  meson”

$$\Delta m = -\frac{1}{2\pi} \text{P} \int_{2m_\pi}^{\infty} dM \frac{\Delta\Gamma(M)}{M - m_D} + \dots$$



[Falk et al., hep-ph/0402204]

(Dispersion relations used before; I don't know how to justify them in full QCD)

- Assuming that phase space is only source of  $SU(3)$  breaking, hadronic matrix elements cancel in  $y$  but not in  $x$  (need to know  $M$ -dependence of decay rates)

**2-body:** Many interesting subtleties (chiral, intermediate, heavy mass regions)

Most guidance for  $PP$  from theory on modelling  $M$ -dependence  $\Rightarrow$  obtain small  $x$

**4-body:** can get sizable contributions to  $x$ , but typically  $x \lesssim y$

- **Conclusion was:** if  $y \sim 1\%$  then we expect  $10^{-3} < |x| < 10^{-2}$   
Uncertainties much larger than for the estimate of  $y$



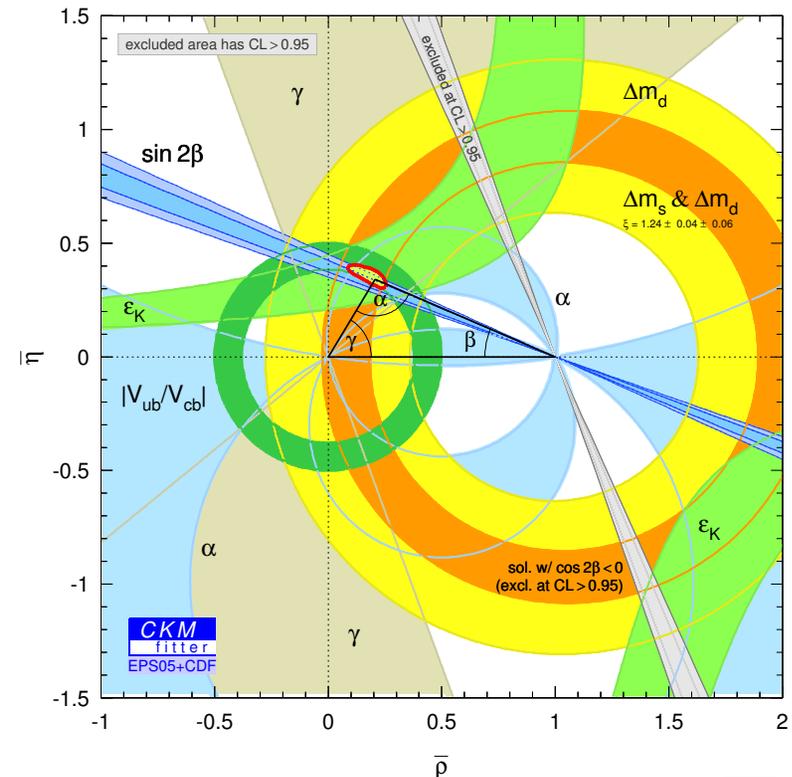
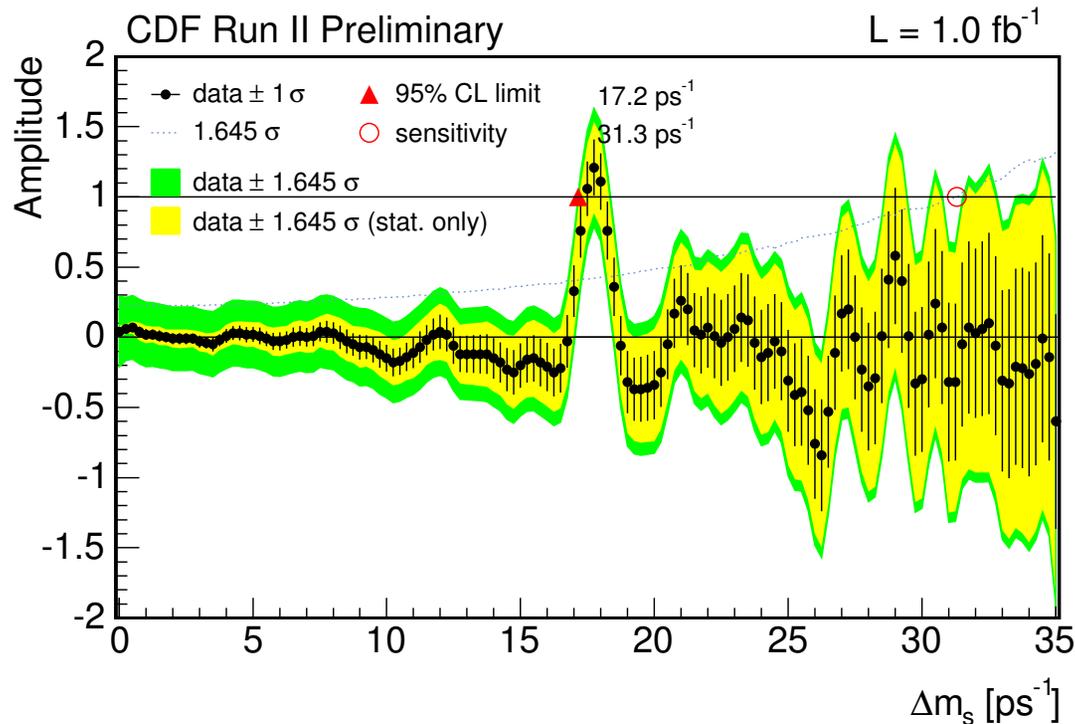
# Summary for $D^0 - \bar{D}^0$ mixing

- It is possible that  $\Delta\Gamma/\Gamma \sim 1\%$  in the SM (calculation w/o ad hoc assumptions)
- It is likely that  $x < y$  in the SM (with some assumptions, predict  $x \lesssim y$ )
- If this is the case then sensitivity to NP is reduced, even if NP dominates  $M_{12}$
- The central values of recent experimental results may be due to SM physics
- SM predictions of  $\Delta m$  and  $\Delta\Gamma$  remain uncertain  $\Rightarrow$  measurements of  $\Delta m$  and  $\Delta\Gamma$  alone (especially since  $\Delta m \lesssim \Delta\Gamma$ ) cannot be interpreted as new physics
- Important to improve constraints on both  $\Delta\Gamma$  and  $\Delta m$ , and continue to look for  $CP$  violation, which remains a potentially robust signal of new physics



$B_s^0 - \bar{B}_s^0$  mixing

# The news of 2006: $\Delta m_{B_s}$ measured



•  $\Delta m_s = (17.77 \pm 0.10 \pm 0.07) \text{ ps}^{-1}$

A  $5.4\sigma$  measurement [CDF, hep-ex/0609040]

Uncertainty  $\sigma(\Delta m_s) = 0.7\%$  is already smaller than  $\sigma(\Delta m_d) = 0.8\%$ !

Largest uncertainty:  $\xi = \frac{f_{B_s} \sqrt{B_s}}{f_{B_d} \sqrt{B_d}}$

Lattice QCD:  $\xi = 1.24 \pm 0.04 \pm 0.06$

Chiral logs:  $\xi \sim 1.2$

SM CKM fit:  $\xi = 1.158^{+0.096}_{-0.064}$



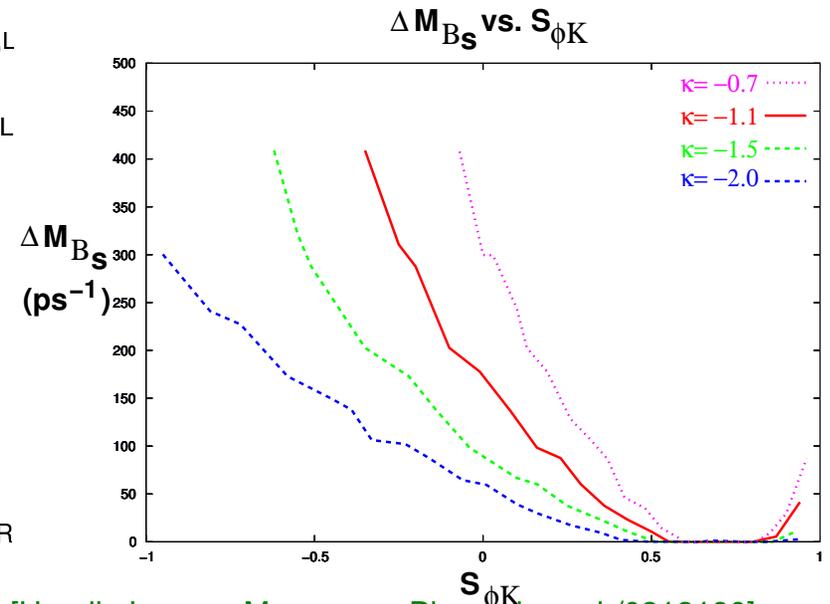
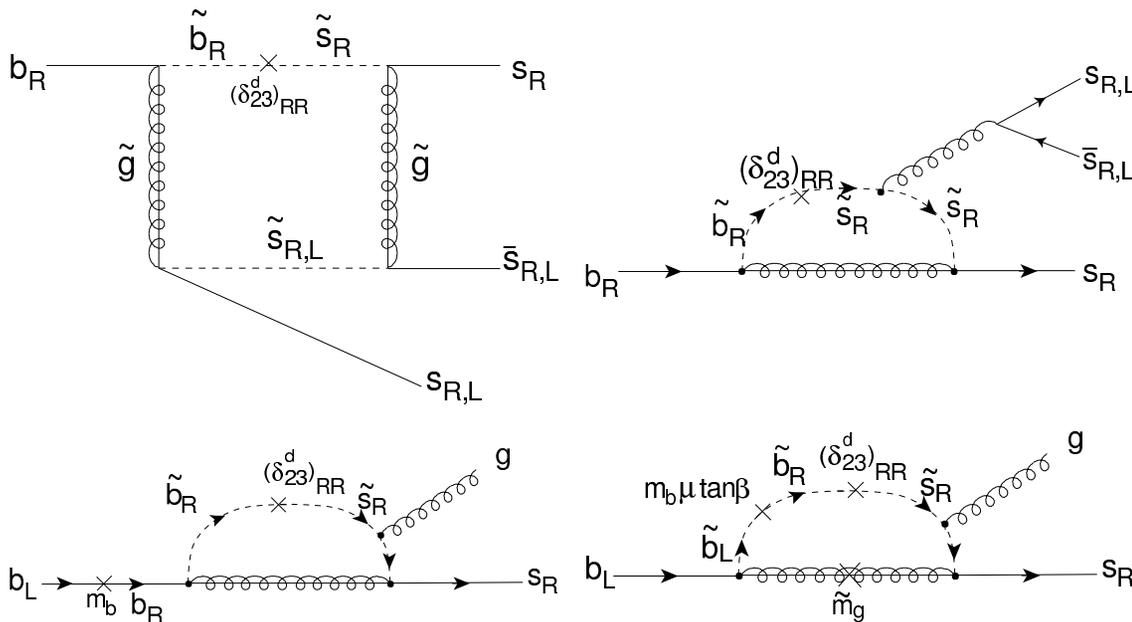
# Some models to enhance $\Delta m_s$

- SUSY GUTs: near-maximal  $\nu_\mu - \nu_\tau$  mixing may imply large mixing between  $s_R$  and  $b_R$ , and between  $\tilde{s}_R$  and  $\tilde{b}_R$

Mixing among right-handed quarks drop out from CKM matrix, but among right-handed squarks it is physical

$$\begin{pmatrix} \tilde{s}_R \\ \tilde{s}_R \\ \tilde{s}_R \\ \tilde{\nu}_\mu \\ \tilde{\mu} \end{pmatrix} \longleftrightarrow \begin{pmatrix} \tilde{b}_R \\ \tilde{b}_R \\ \tilde{b}_R \\ \tilde{\nu}_\tau \\ \tilde{\tau} \end{pmatrix}$$

$\mathcal{O}(1)$  effects in  $b \rightarrow s$  possible



[Harnik, Larson, Murayama, Pierce, hep-ph/0212180]



# Some models to suppress $\Delta m_s$

- Neutral Higgs mediated FCNC in the large  $\tan \beta$  region:

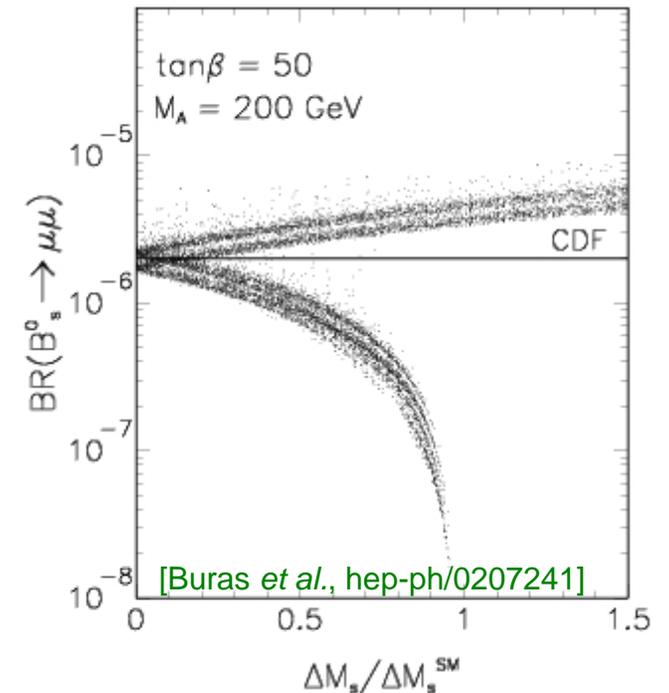
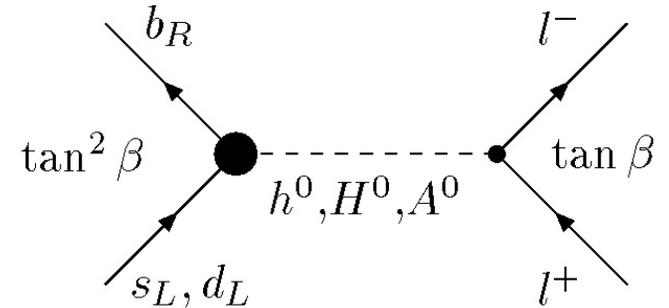
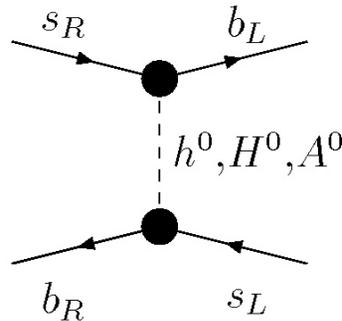
Enhancement of  $\mathcal{B}(B_{d,s} \rightarrow \mu^+ \mu^-) \propto \tan^6 \beta$  up to two orders of magnitude above the SM

CDF & DØ:  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 5.8 \times 10^{-8}$  (95% CL)

[Bernhard, yesterday]

SM:  $3.4 \times 10^{-9}$  — measurable at LHC

- Suppression of  $\Delta m_s \propto \tan^4 \beta$  in a correlated way



# New physics in $B$ mixing

- $B_{d,s}$  mixings are short distance dominated, so: theory errors  $\ll$  measured values  
(For  $\Delta m_D$  and  $\epsilon'/\epsilon$  we only know NP  $<$  measurement;  $\Delta\Gamma_s$  ( $\Delta\Gamma_s^{CP}$ ) in between)

Assume: (i)  $3 \times 3$  CKM matrix is unitary

(ii) Tree-level decays dominated by SM

- Concentrate on NP in  $\Delta F = 2$ : two parameters for each meson mixing amplitude

$$M_{12} = \underbrace{M_{12}^{\text{SM}} r^2 e^{2i\theta}}_{\text{easy to relate to data}} \equiv \underbrace{M_{12}^{\text{SM}} (1 + h e^{2i\sigma})}_{\text{easy to relate to models}}$$

- $B\bar{B}$  mixing dependent observables sensitive to  $h, \sigma$ :  $\Delta m_{d,s}$ ,  $S_{f_i}$ ,  $A_{\text{SL}}^{d,s}$ ,  $\Delta\Gamma_s^{CP}$   
(Hadronic uncertainty sizable in  $A_{\text{SL}}^{d,s}$  and  $\Delta\Gamma_s^{CP}$ , but in SM  $A_{\text{SL}}^{d,s} \ll$  current bound)
- Tree-level CKM constraints unaffected:  $|V_{ub}/V_{cb}|$  and  $\gamma$  (or  $\pi - \beta - \alpha$ )  
(neglect NP in  $\Delta F = 1$ , and possible correlations between  $b \rightarrow d$  and  $b \rightarrow s$ )

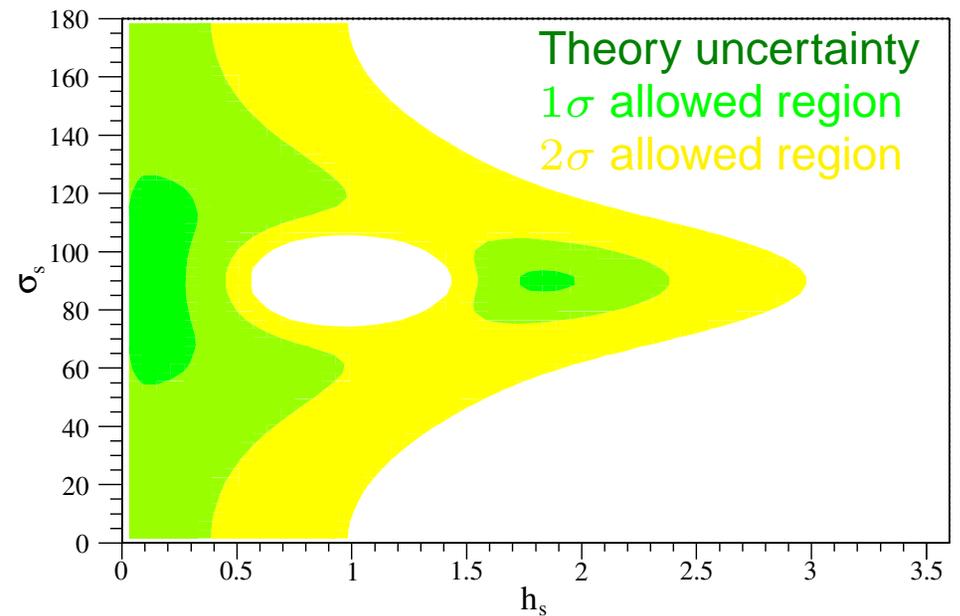
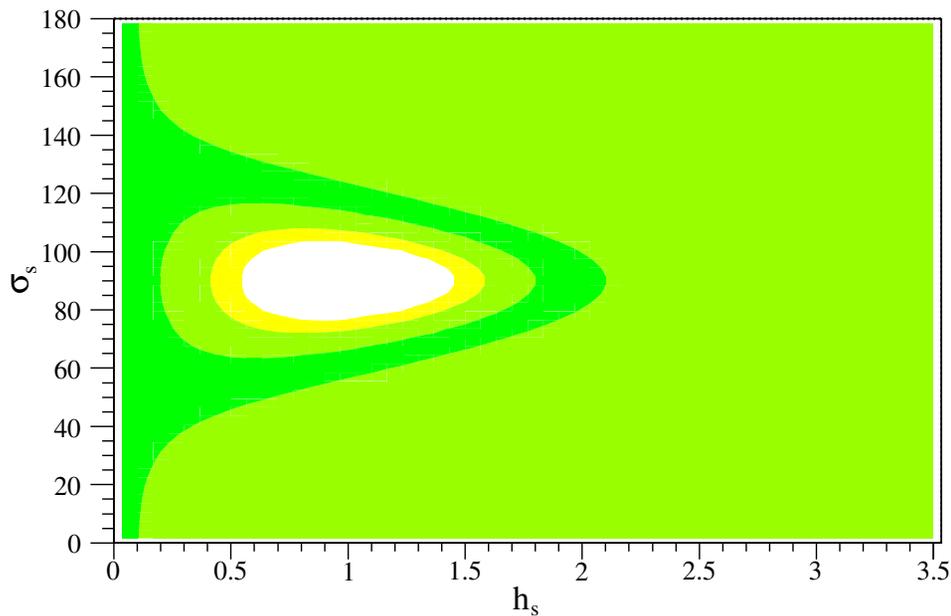


# New physics in $B_s^0 - \bar{B}_s^0$ mixing

- Constraints before (left) and after (right) measurement of  $\Delta m_s$  and  $\Delta\Gamma_s^{CP}$

Recall parameterization:  $M_{12} = M_{12}^{\text{SM}} (1 + h_s e^{2i\sigma_s})$

[ZL, Papucci, Perez, hep-ph/0604112]



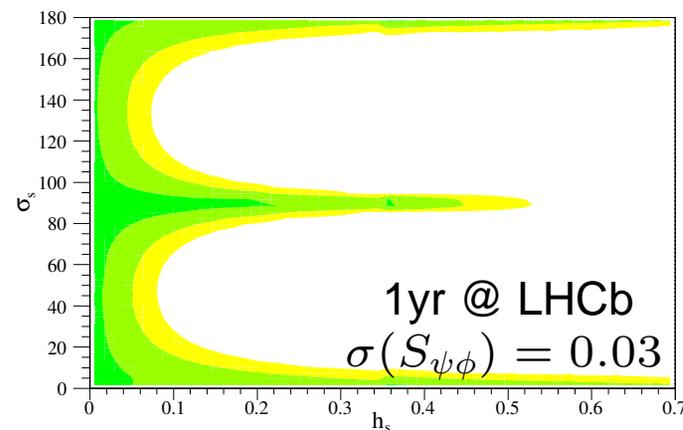
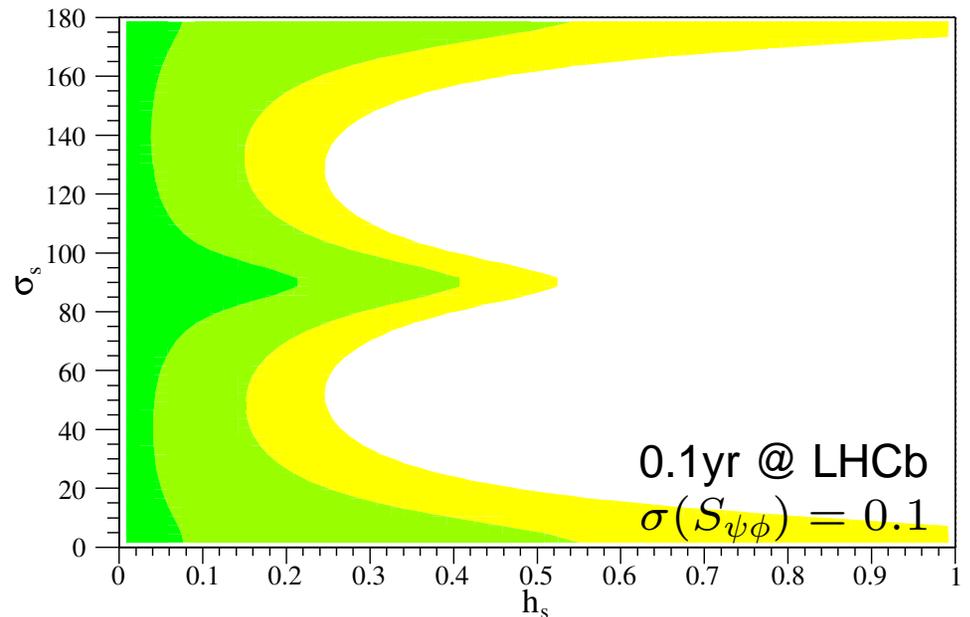
- To learn more about the  $B_s$  system, need data on  $CP$  asymmetry in  $B_s \rightarrow J/\psi \phi$

- $h$  measures “tuning”:  $h \sim (4\pi v/\Lambda)^2$ , so  $\begin{cases} h \sim 1 & \Rightarrow \Lambda_{\text{flavor}} \sim 2 \text{ TeV} \sim \Lambda_{\text{EWSB}} \\ h < 0.1 & \Rightarrow \Lambda_{\text{flavor}} > 7 \text{ TeV} \gg \Lambda_{\text{EWSB}} \end{cases}$



# Next milestone in $B_s$ : $S_{B_s \rightarrow \psi\phi, \psi\eta}^{(')}$

- $S_{\psi\phi}$  ( $\sin 2\beta_s$  for  $CP$ -even) analog of  $S_{\psi K}$   
CKM fit predicts:  $\sin 2\beta_s = 0.0346^{+0.0026}_{-0.0020}$
- 2000: Is  $\sin 2\beta$  consistent with  $\epsilon_K$ ,  $|V_{ub}|$ ,  $\Delta m_B$  and other constraints?  
2009: Is  $\sin 2\beta_s$  consistent with ... ?
- Plot  $S_{\psi\phi} = \text{SM value} \pm 0.10 / \pm 0.03$   
0.1/1 yr of nominal LHCb data  $\Rightarrow$
- With relatively little data, huge impact on our understanding; maybe one of the most interesting early measurements



Notice scales!



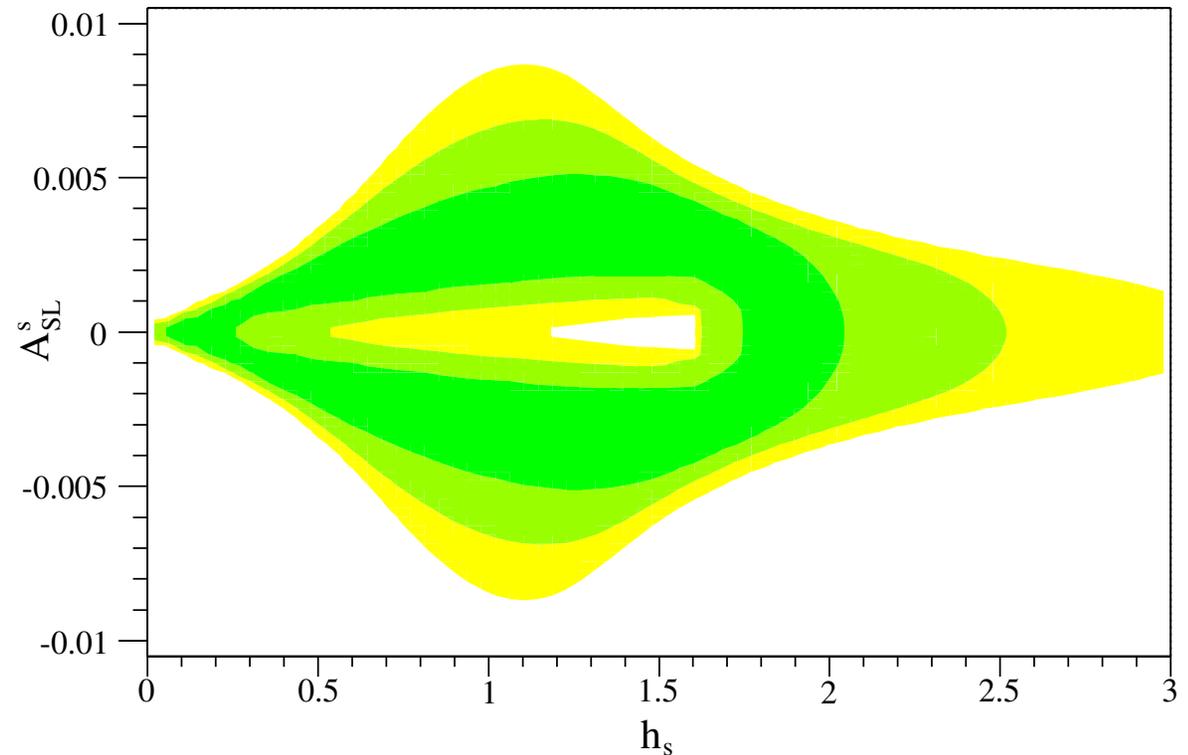
# Another observable: $A_{\text{SL}}^s$

- Difference of  $B \rightarrow \bar{B}$  vs.  $\bar{B} \rightarrow B$  probability

$$A_{\text{SL}} = \frac{\Gamma[\bar{B}_{\text{phys}}^0(t) \rightarrow \ell^+ X] - \Gamma[B_{\text{phys}}^0(t) \rightarrow \ell^- X]}{\Gamma[\bar{B}_{\text{phys}}^0(t) \rightarrow \ell^+ X] + \Gamma[B_{\text{phys}}^0(t) \rightarrow \ell^- X]} = \frac{1 - |q/p|^4}{1 + |q/p|^4} \approx -2 \left( \left| \frac{q}{p} \right| - 1 \right)$$

- Can be  $\mathcal{O}(10^3)$  times SM
- $|A_{\text{SL}}^s| > |A_{\text{SL}}^d|$  possible (contrary to SM)
- In SM:  $A_{\text{SL}}^s \sim 3 \times 10^{-5}$  is unobservably small

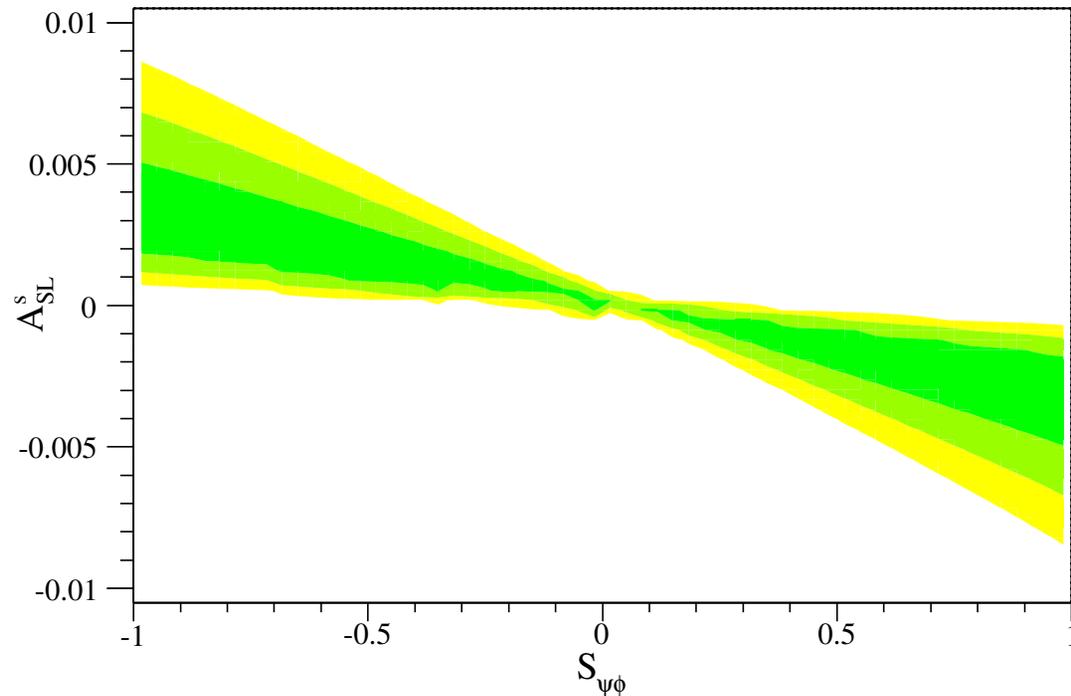
[see also: Buras *et al.*, hep-ph/0604057;  
Grossman, Nir, Raz, hep-ph/0605028]



# Correlation between $S_{\psi\phi}$ and $A_{\text{SL}}^s$

- $A_{\text{SL}}^s$  and  $S_{\psi\phi}$  are strongly correlated in  $h_s, \sigma_s \gg \beta_s$  region [ZL, Papucci, Perez, hep-ph/0604112]

$$A_{\text{SL}}^s = - \left| \frac{\Gamma_{12}^s}{M_{12}^s} \right|^{\text{SM}} S_{\psi\phi} + \mathcal{O}\left(h_s^2, \frac{m_c^2}{m_b^2}\right)$$



- Correlation only if NP does not alter tree level processes — test assumptions



# Summary for $B_s^0 - \bar{B}_s^0$ mixing

- Measurements @ Tevatron started to constrain NP in  $(b \rightarrow s)_{\Delta F=2}$  transitions
- Significant NP contributions are possible nevertheless
- Need measurements of more observables:  $S_{\psi\phi}$  &  $A_{\text{SL}}^s$   
(Don't need sensitivity to SM prediction to have important implications!)
- LHCb can distinguish between MFV and non-MFV scenarios in the early LHC era
- If deviations found, correlations between  $S_{\psi\phi}$  and  $A_{\text{SL}}^s$  can help understand the nature of NP



# Conclusions

# Some things we do know

- We learned a lot about meson mixings in the past 1.5 years

	$x = \Delta m / \Gamma$		$y = \Delta \Gamma / (2\Gamma)$		$A = 1 -  q/p ^2$	
	SM theory	data	SM theory	data	SM theory	data
$B_d$	$\mathcal{O}(1)$	0.78	$y_s  V_{td}/V_{ts} ^2$	$-0.005 \pm 0.019$	$-(5.5 \pm 1.5)10^{-4}$	$(-4.7 \pm 4.6)10^{-3}$
$B_s$	$x_d  V_{ts}/V_{td} ^2$	25.8	$\mathcal{O}(-0.1)$	$-0.05 \pm 0.04$	$-A_d  V_{td}/V_{ts} ^2$	$(0.3 \pm 9.3)10^{-3}$
$K$	$\mathcal{O}(1)$	0.948	-1	$-0.998$	$4 \operatorname{Re} \epsilon$	$(6.6 \pm 1.6)10^{-3}$
$D$	$\lesssim 0.01$	$< 0.016$	$\mathcal{O}(0.01)$	$y_{CP} = 0.011 \pm 0.003$	$< 10^{-4}$	$\mathcal{O}(1)$ bound only

- Identities, neglecting CPV in mixing (not the most interesting info, but amusing):

	$CP$		lifetime		comments
	even	odd	short	long	
$B_s$	even	odd	even	odd	In SM even = light, odd = heavy
$B_d$	heavy quark limit: same as for $B_s$				Not directly known yet
$K$	light	heavy	light	heavy	Known before the SM ; -)
$D$	even	odd	even	odd	Unknown which is heavy / light

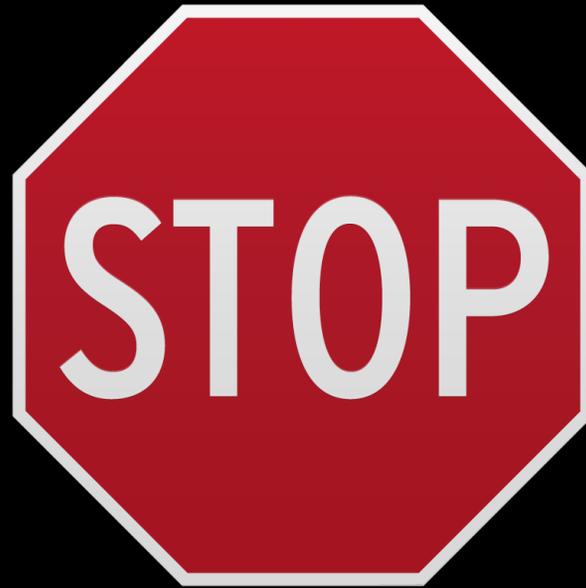
Before 2006, we only knew experimentally the Kaon line of this table!



# Some things I'd like to know

- $D^0 - \bar{D}^0$  mixing:
  - Values of  $\Delta m$  and  $\Delta\Gamma$
  - Result of  $K\pi$  fit with 5 parameters (allowing CPV in mixing, but not in decay)
  - Will CPV be observed? Is  $|q/p|$  near 1?
- $B_s^0 - \bar{B}_s^0$  mixing:
  - Better constraint on / measurement of  $S_{B_s \rightarrow \psi\phi}$
  - Improved bounds on  $A_{SL}$
  - Better lattice QCD results for  $\Delta m$  and  $\Delta\Gamma$
- We can learn a lot more from improved measurements





**Backup slides**

# $SU(3)$ analysis of $D$ mixing

- Want to study:  $\langle \bar{D}^0 | T \{ H_w, H_w \} | D^0 \rangle = \langle 0 | D T \{ H_w, H_w \} D | 0 \rangle$

the field operator  $D \in 3$  creates a  $D^0$  or annihilates a  $\bar{D}^0$

$$H(\Delta C = -1) = (\bar{q}_i c)(\bar{q}_j q_k) \in 3 \times \bar{3} \times \bar{3} = \underbrace{\bar{15} + 6}_{\text{If 3rd gen. neglected}} + \bar{3} + \bar{3}$$

$SU(3)$  breaking is introduced by  $\mathcal{M}_j^i = \text{diag}(m_u, m_d, m_s) \sim \text{diag}(0, 0, m_s)$

- A pair of  $D$  operators or a pair of  $H$ 's is symmetric, so  $D_i D_j \in 6$  and

$$H_k^{ij} H_n^{lm} \in [(\bar{15} + 6) \times (\bar{15} + 6)]_S \rightarrow \bar{60} + 42 + 15'$$

0. Since there is no  $\bar{6}$  in  $H_w H_w \Rightarrow$  mixing vanishes in  $SU(3)$  limit

1.  $DDM \in 6 \times 8 = 24 + \bar{15} + 6 + \bar{3} \Rightarrow$  no invariants with  $H_w H_w$  at order  $m_s$

2.  $DDMM \in 6 \times (8 \times 8)_S = 6 \times (27 + 8 + 1) = 60 + \bar{24} + \bar{15}' + \dots$

- $D^0 - \bar{D}^0$  mixing only arises at order  $m_s^2 / \Lambda_{\chi\text{SB}}^2$  (if  $SU(3)$  violation is perturbative)

[Falk et al., hep-ph/0110317]



# Parameterization of NP in mixing

- Assume: (i)  $3 \times 3$  CKM matrix is unitary; (ii) Tree-level decays dominated by SM
- Concentrate on NP in mixing amplitude; two new param's for each neutral meson:

$$M_{12} = \underbrace{M_{12}^{\text{SM}} r_q^2 e^{2i\theta_q}}_{\text{easy to relate to data}} \equiv \underbrace{M_{12}^{\text{SM}} (1 + h_q e^{2i\sigma_q})}_{\text{easy to relate to models}}$$

- Observables sensitive to  $\Delta F = 2$  new physics:

$$\Delta m_{B_q} = r_q^2 \Delta m_{B_q}^{\text{SM}} = |1 + h_q e^{2i\sigma_q}| \Delta m_q^{\text{SM}}$$

$$S_{\psi K} = \sin(2\beta + 2\theta_d) = \sin[2\beta + \arg(1 + h_d e^{2i\sigma_d})]$$

$$S_{\rho\rho} = \sin(2\alpha - 2\theta_d)$$

$$S_{B_s \rightarrow \psi\phi} = \sin(2\beta_s - 2\theta_s) = \sin[2\beta_s - \arg(1 + h_s e^{2i\sigma_s})]$$

$$A_{\text{SL}}^q = \text{Im} \left( \frac{\Gamma_{12}^q}{M_{12}^q r_q^2 e^{2i\theta_q}} \right) = \text{Im} \left[ \frac{\Gamma_{12}^q}{M_{12}^q (1 + h_q e^{2i\sigma_q})} \right]$$

$$\Delta\Gamma_s^{CP} = \Delta\Gamma_s^{\text{SM}} \cos^2(2\theta_s) = \Delta\Gamma_s^{\text{SM}} \cos^2[\arg(1 + h_s e^{2i\sigma_s})]$$

- Tree-level constraints unaffected:  $|V_{ub}/V_{cb}|$  and  $\gamma$  (or  $\pi - \beta - \alpha$ )

